

Comparison of analytical and Monte Carlo calculations for heterogeneity corrections in LDR prostate brachytherapy

PURPOSE

- Heterogeneities have a significant influence on low energy (LDR) brachytherapy
- Develop algorithm for dose calculation in prostate with calcifications
 - accounts for effect of heterogeneities
 - based on TG-43 reference data
 - real-time calculation speed
- Compare performance of algorithm vs Monte Carlo (MC) simulation
 - dose reliability
 - computing speed
- Assess suitability of algorithm inclusion in clinical commercial treatment planning system (TPS)

MATERIALS & METHODS

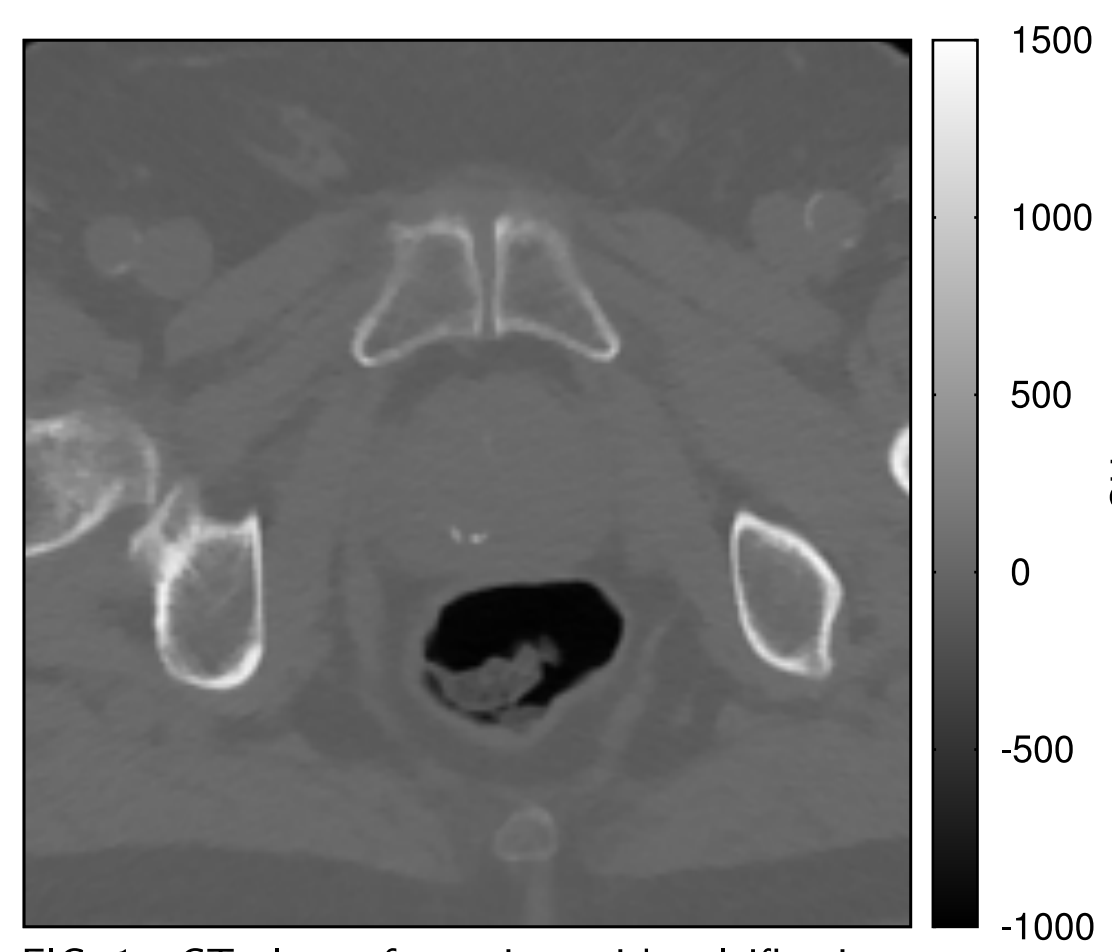


FIG. 1 - CT plane of a patient with calcifications inside the prostate (La Fe-Hospital).

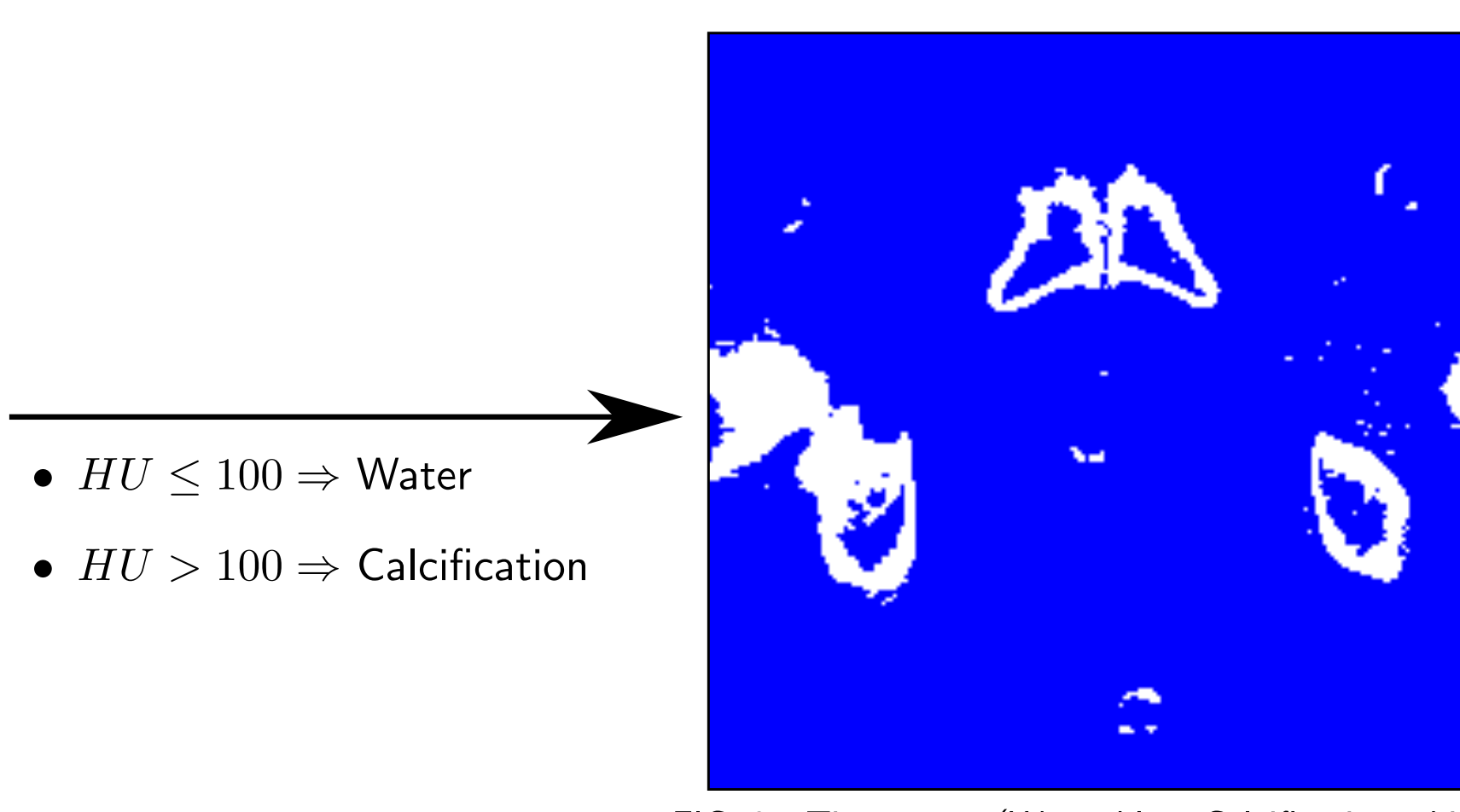


FIG. 2 - Tissue type (Water-blue, Calcification-white) according to the calcification threshold at 100 HU.

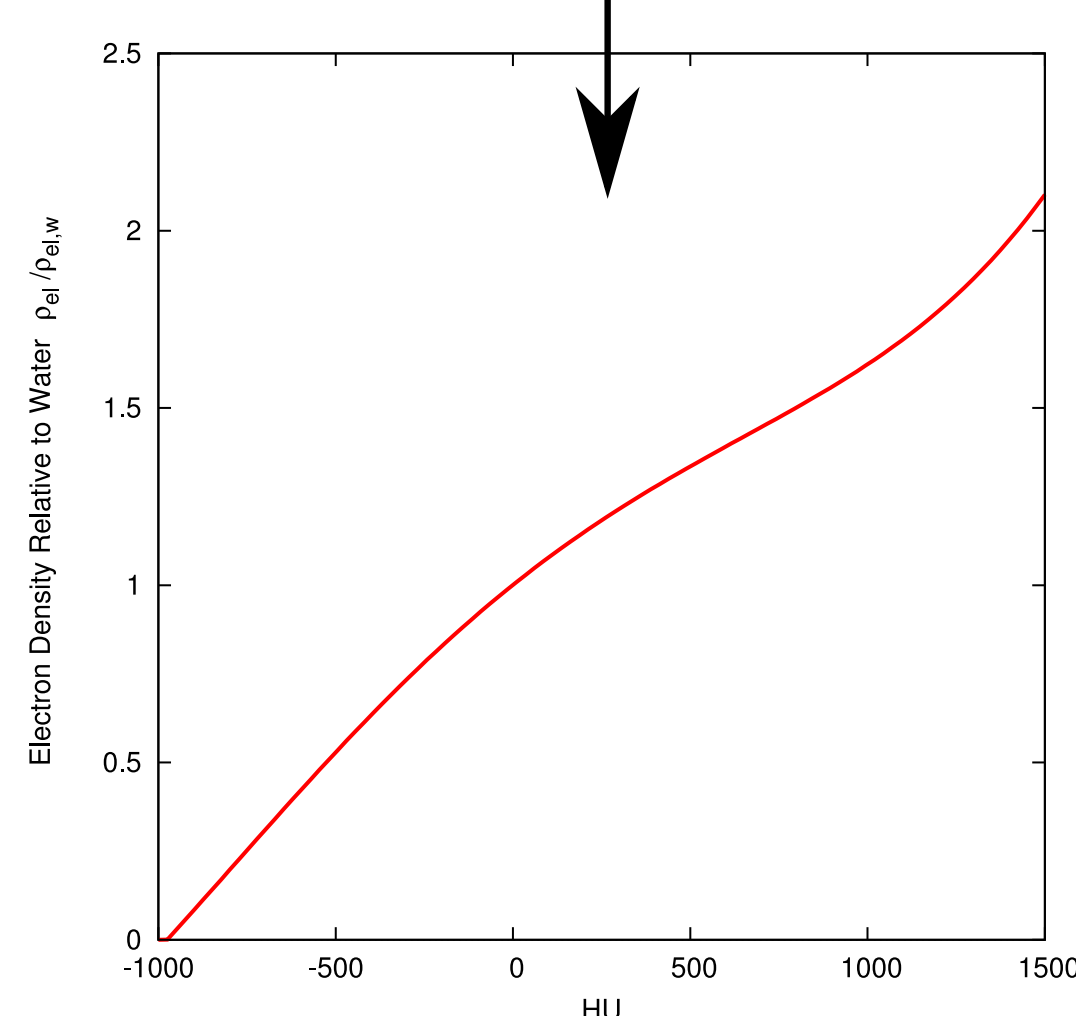


FIG. 3 - Calibration curve of HU number to relative electron density (La Fe-Hospital).

$$\text{Mass Density} = \frac{\rho_{el}}{\rho_{el,w}} * \begin{cases} 1.0 \frac{g}{cm^3} & \text{if Tissue = Water} \\ 0.9 \frac{g}{cm^3} & \text{if Tissue = Calcification} \end{cases}$$

Voxelized phantom characterized by $\begin{cases} \text{Tissue type} \\ \text{Mass Density} \end{cases}$

Monte Carlo Simulation (PENelope2009)

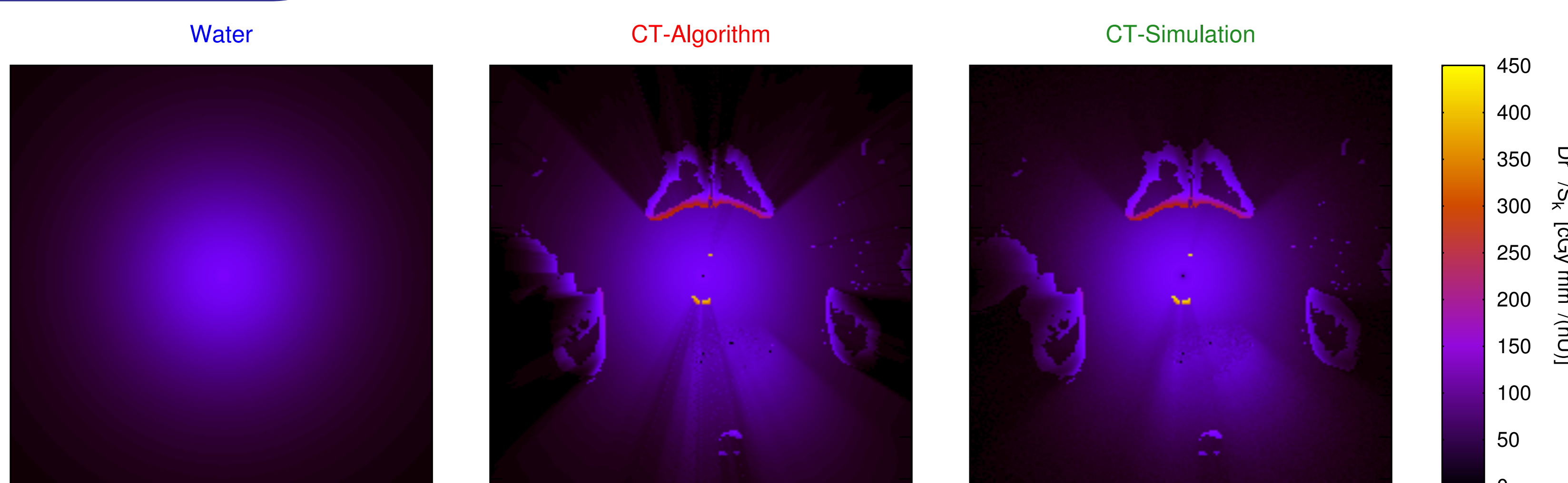
- At the center of the plane, one ¹²⁵I seed is simulated
 - ↪ Model 6711-OncoSeed™, manufactured by Amersham-Health
- For each voxel:
 - ↪ The mass density ρ is specified
 - ↪ A composition is defined depending on tissue type

Analytical algorithm

- Input: Radial dose function $g(r)$, Dose rate constant Λ , Air-kerma strength S_k
- For each voxel:
 - ↪ The mass density ρ is specified
 - ↪ A mass absorption coefficient (μ/ρ) is defined depending on tissue type
 - ↪ The distance r to the radioactive seed is computed
- Based on the water-equivalent path method: $\Delta r_{eq} \propto \Delta r \frac{\rho}{\rho_w} \frac{(\mu/\rho)}{(\mu/\rho)_w}$
- Fundamental idea: released energy $E \Big|_r^{r+\Delta r} = E_w \Big|_{r_{eq}}^{r_{eq}+\Delta r_{eq}}$; $E \propto \int g(r') dr'$
- Ray-tracing across the phantom is required (length of intersections)

RESULTS

FIG. 4 - Dose rate by air-kerma strength times the squared distance to the radioactive seed, which is placed at the center of the imaging plane. Heat maps for the homogeneous/Water and heterogeneous/CT cases (Algorithm and Simulation) are shown in a common color scale range for a reliable comparison.



- Significant impact of calcifications in dosimetry with respect to homogeneous case
 - Higher dose in calcificated regions (hot spots) due to higher absorption coefficient
 - Lower dose behind calcificated regions (shadows) due to energy conservation
- Remarkable agreement Algorithm - Simulation (see FIG. 4 and FIG. 5)
 - 5A: Dose 'shadow' effect caused by two prostate calcifications between seed and calculation point
 - 5B: Dose 'hot spot' effect in a prostate calcification (first peak) and surrounding bones (last peaks)
 - 5C: Dose 'overflow' effect produced by an air cavity (see FIG. 1)
- Computation performance (1 seed, 201 × 201 voxels): **Algorithm 0.16 s** ⇔ **108 h Simulation** (10⁹ events)

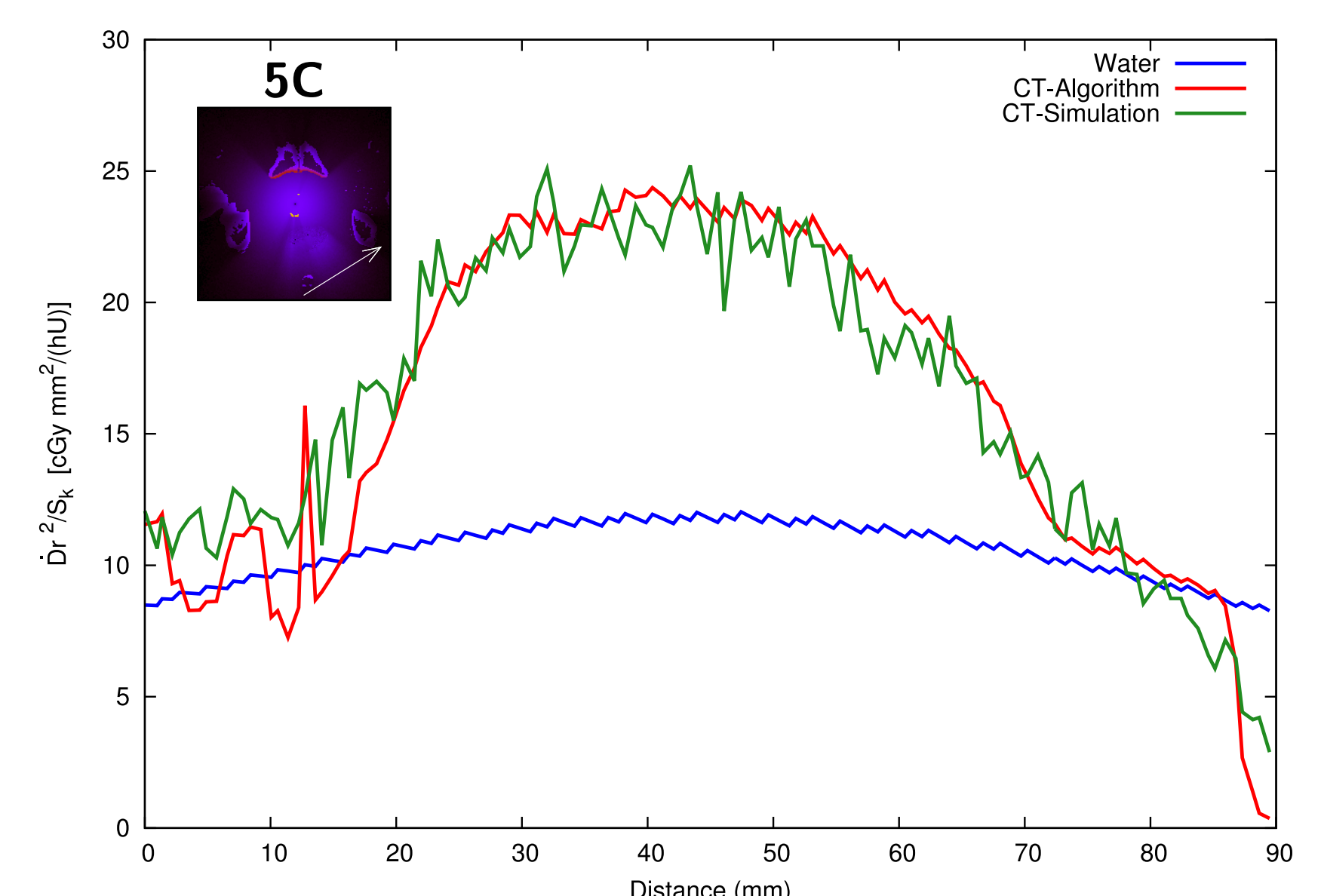
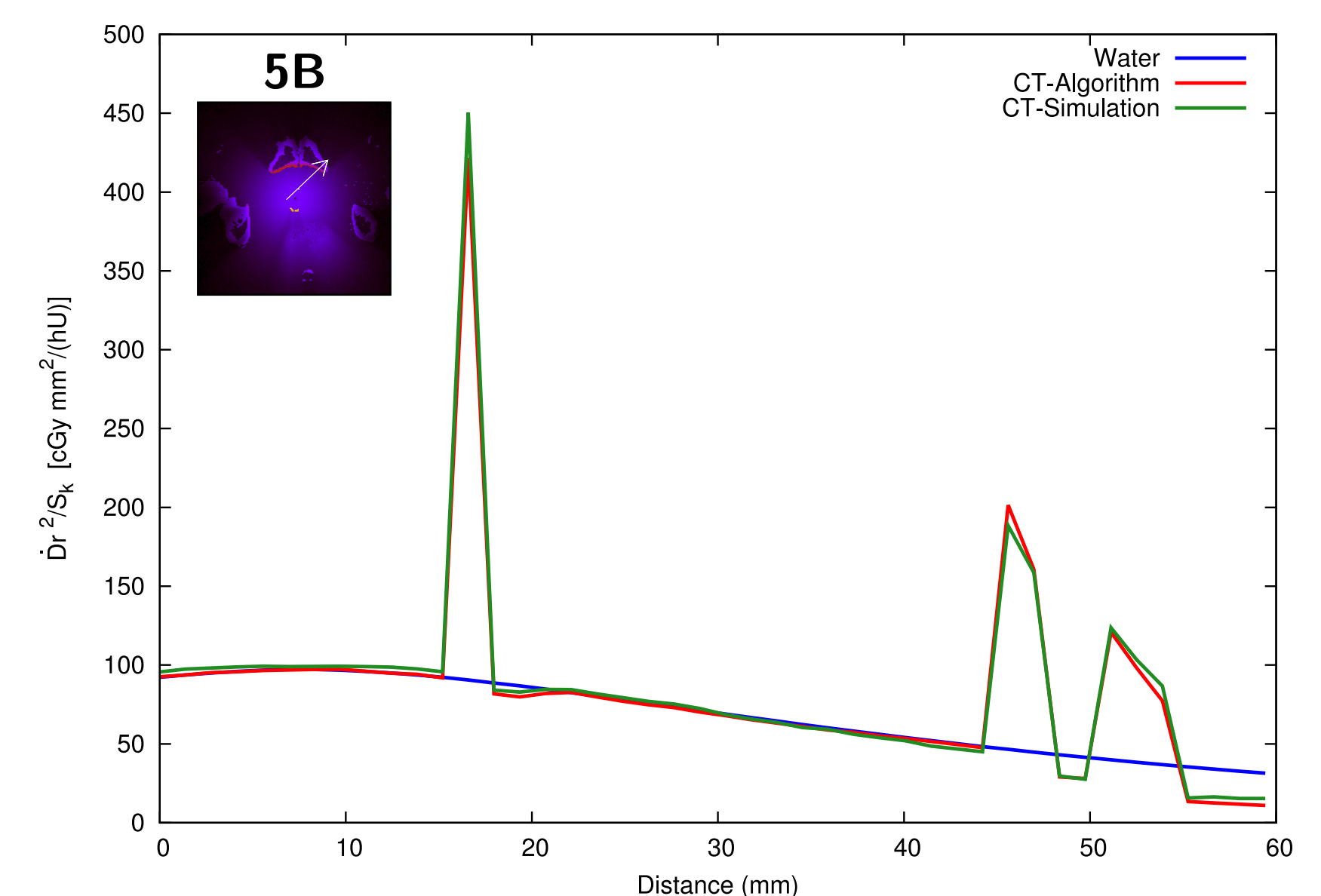
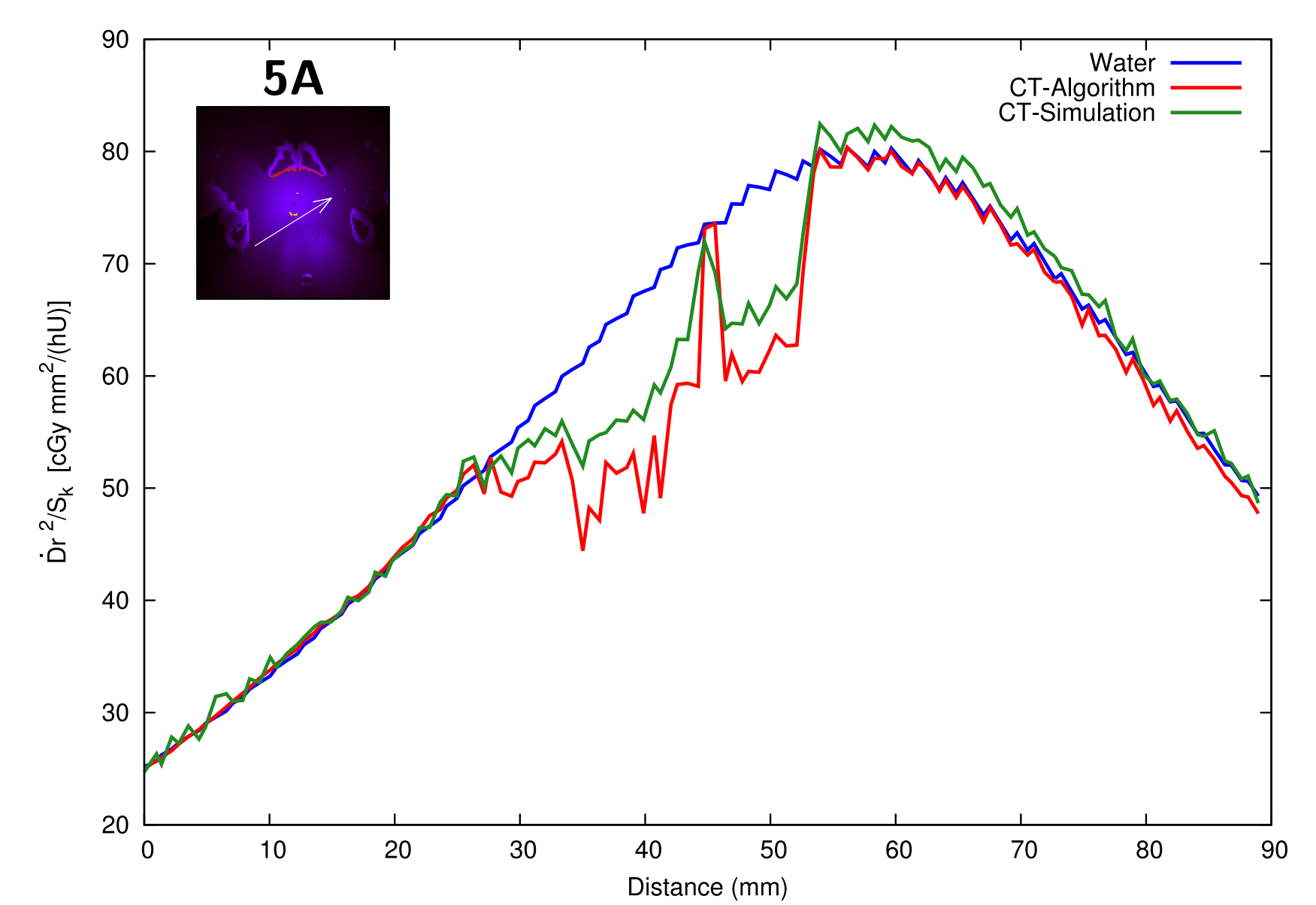


FIG. 5 - Line profiles of the dose rate by air-kerma strength times the squared distance, drawn across the imaging planes of FIG. 4 (white arrows in the insets) for three cases of interest.

TAB.1 - Conclusions about the weaknesses, strenghts, and challenges regarding the analytical dose calculation algorithm presented.

Weaknesses	Strengths	Challenges
<ul style="list-style-type: none"> • Non-scatter assumption • Ray-tracing artifacts 	<ul style="list-style-type: none"> • Simple, fast and robust • Agreement with simulation • Applicable to any heterogeneity 	<ul style="list-style-type: none"> • Accuracy of tissue classification • Energy dependent absorption coefficient

↪ **Improvement of treatment quality**
↪ **Suitable for clinical real-time TPS**

OUTLOOK