

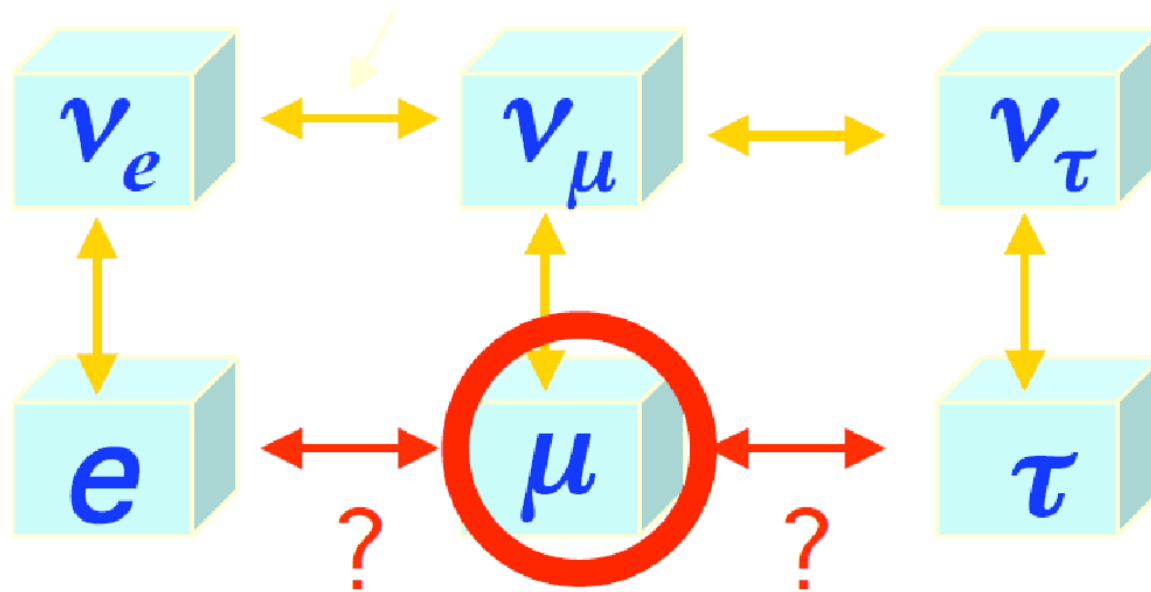
Lepton Flavour Violation

M. Hirsch

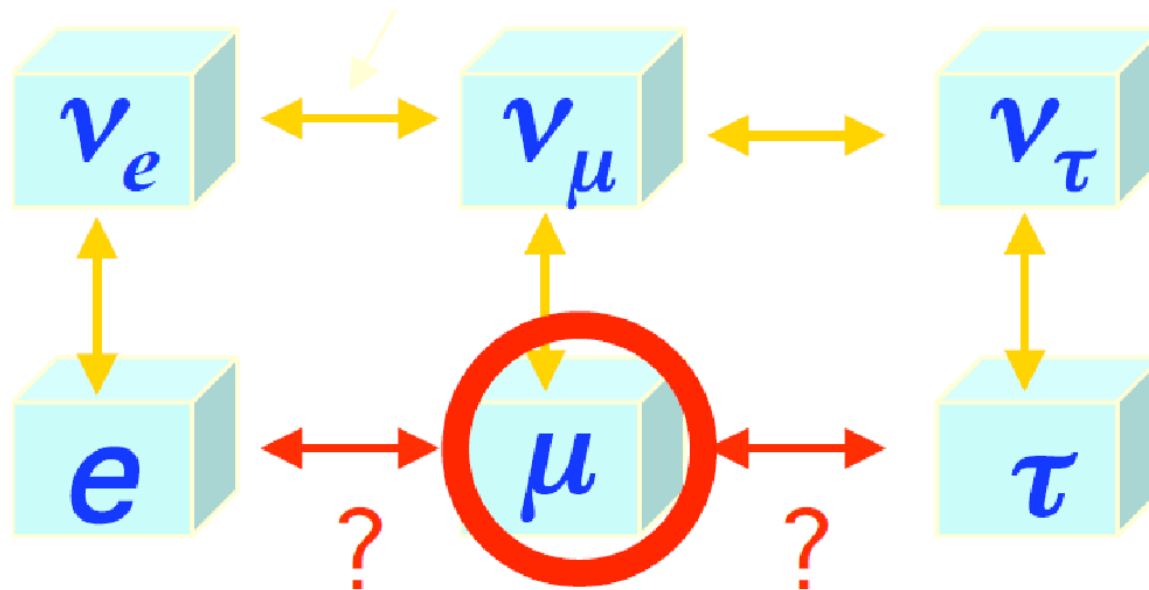
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Instituto de Fisica Corpuscular - CSIC
Universidad de Valencia
Valencia - Spain

Motivation



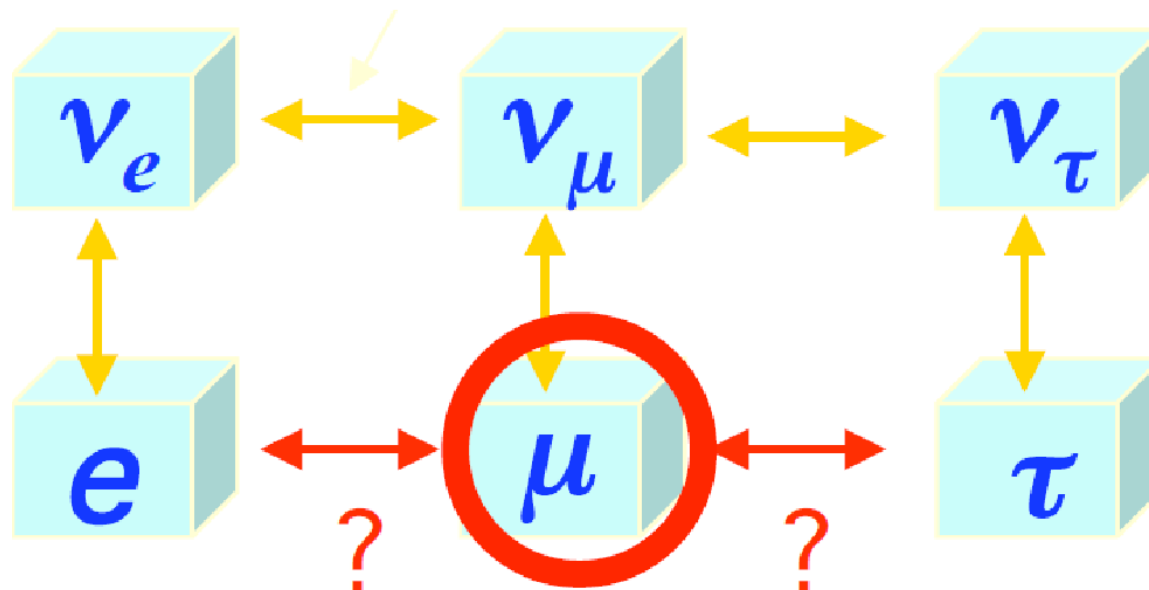
Motivation



Neutrinos oscillate!

Confirmed by
many experiments:
SuperK, SNO, KamLAND,
T2K, MINOS ...

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Charged leptons?

... only
upper limits!



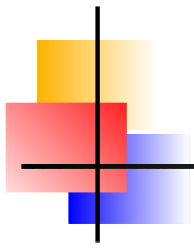
Outline

I. Neutrinos - experiment

II. Short aside on neutrino mass

III. Charged lepton flavour violation

IV. Conclusions



I.

Neutrinos - experiment



Neutrino oscillations

Consider simplified **two generation** example:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \cdot \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

A neutrino created as $|\nu_e\rangle$ at $x = (t, \vec{x}) = (0, \vec{0})$ with energy E will evolve as:

$$|\nu_e(x)\rangle = e^{ip_1 x} |\nu_1\rangle + e^{ip_2 x} |\nu_2\rangle$$

The probability of ν_μ *appearance* at a distance $\vec{x} = (0, 0, L)$ is

$$P(\nu_e \rightarrow \nu_\mu) = |\langle \nu_\mu | \nu(L) \rangle|^2 \simeq \sin^2(2\theta) \sin^2\left(\frac{\Delta m_{12}^2 L}{4E}\right)$$

⇒ oscillations in vacuum



3-generation mixing

For 3 generations of leptons, 2 independent Δm_{ij}^2 , mixing has 3 θ_{ij} :

$$\begin{aligned}
 U &= \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \cdot P \\
 &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot P
 \end{aligned}$$

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 \end{aligned}$$

atmospheric
and long-baseline
experiments

reactor &
long-baseline
experiments

solar &
reactor
experiments

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atmospheric
and long-baseline
experiments

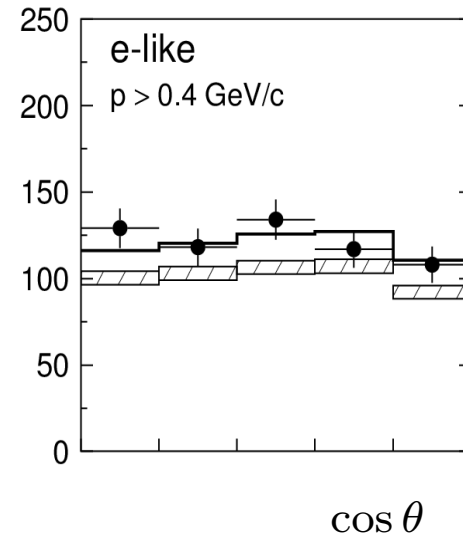
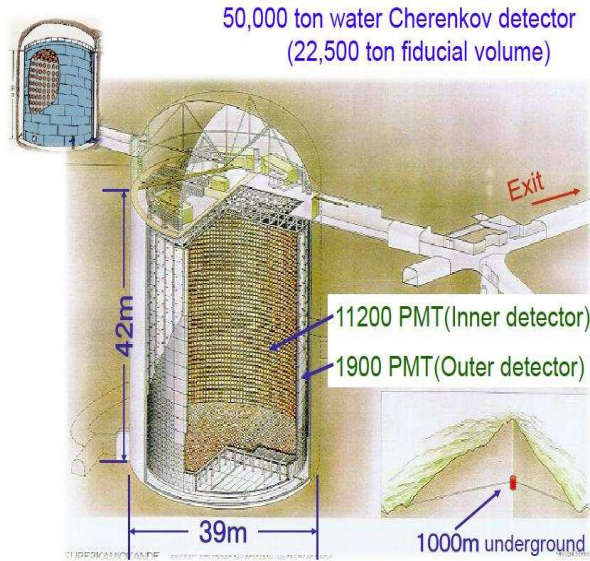
reactor &
long-baseline
experiments

solar &
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$\Rightarrow P$ - diagonal matrix of Majorana phases
observable only in $\Delta L = 2$ processes

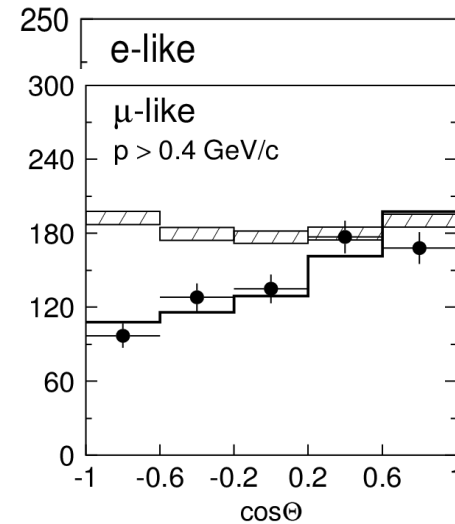
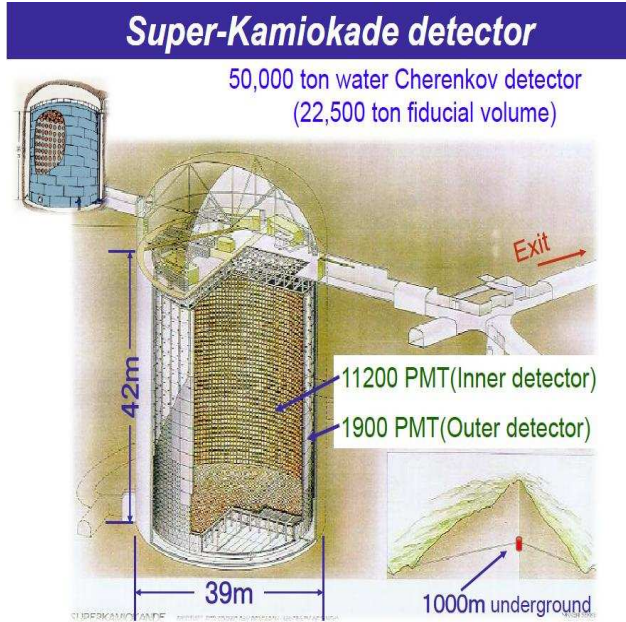
Atmospheric oscillations

Super-Kamiokade detector



SuperK, 1998:

Atmospheric oscillations

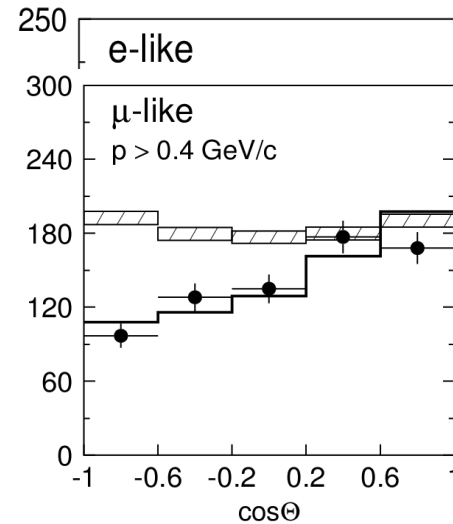
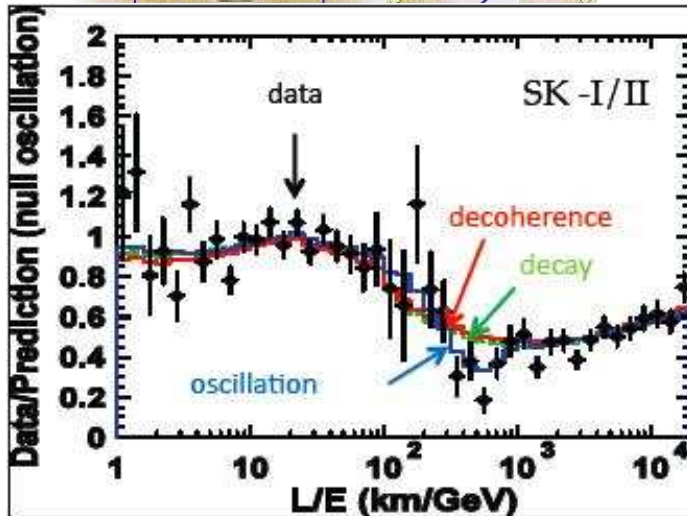
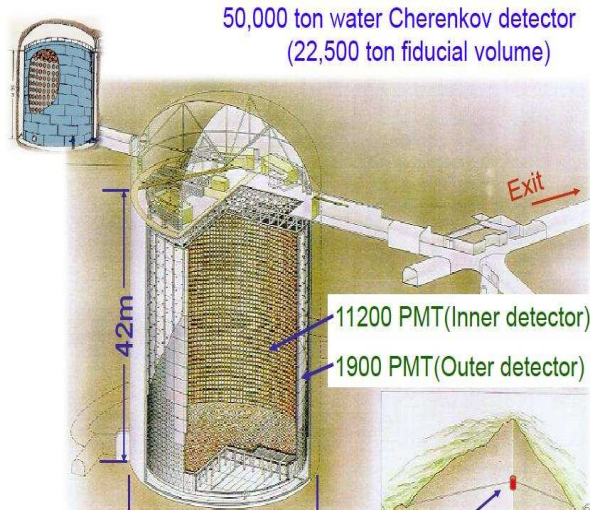


SuperK, 1998:

angular
dependent
deficit of ν_μ
 $\Rightarrow \nu_\mu$ oscillate!

Atmospheric oscillations

Super-Kamiokade detector



SuperK, 1998:

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deficit of ν_μ
 $\Rightarrow \nu_\mu$ oscillate!

Super-K, 2004:

L/E dependence favours
oscillation solution!

Atmospheric oscillations

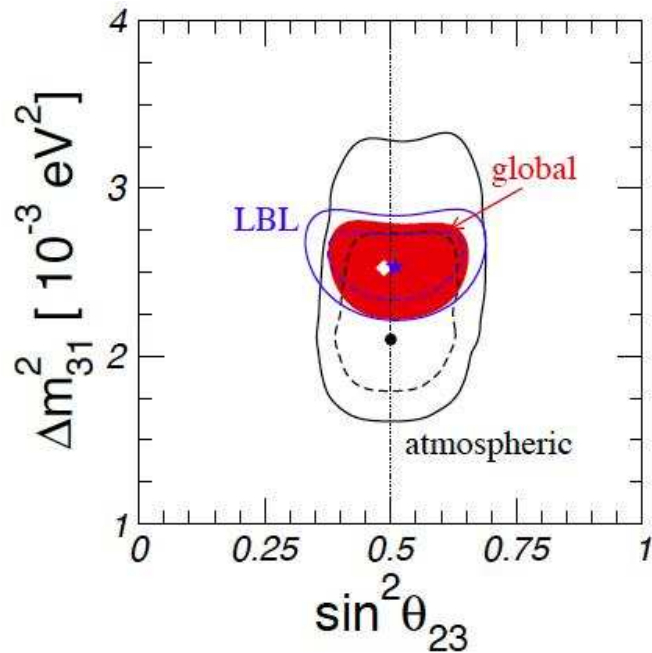


Fig from:
Forero, Tortola
& Valle, 2012

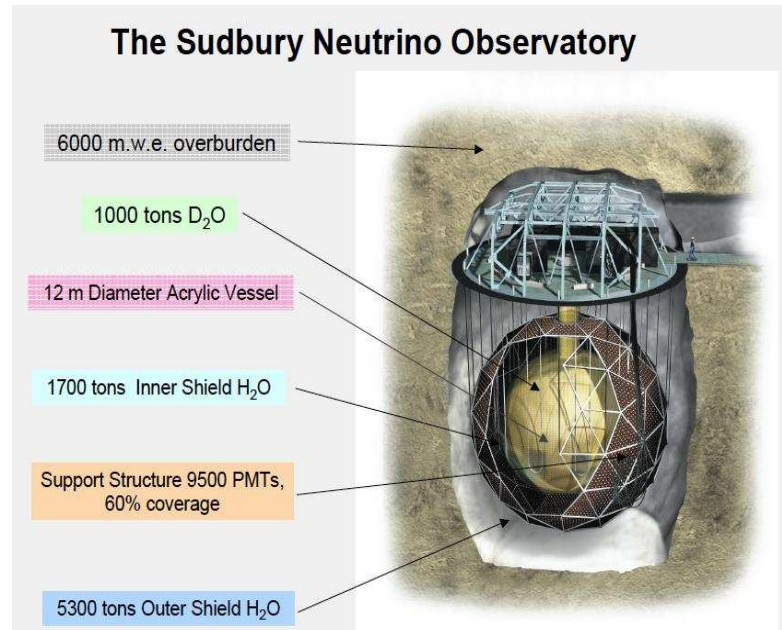
LBL - long baseline experiments (mostly [MINOS](#))

ATM - atmospheric neutrino data, [Super-Kamiokande](#)

$$\Delta m_{\text{Atm}}^2 = (2.2 - 2.74) \times 10^{-3} \text{ eV}^2$$

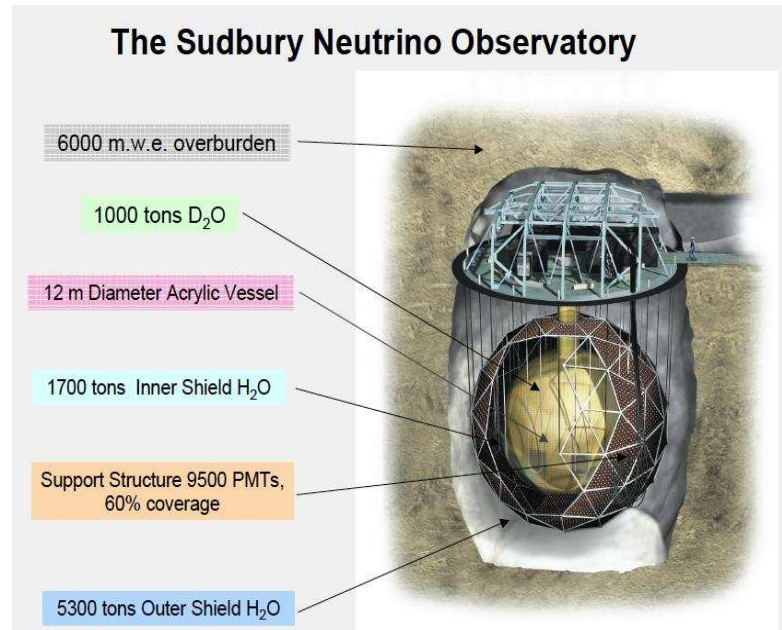
$$\sin^2 \theta_{\text{Atm}} = (0.36 - 0.68) - \text{consistent with maximal mixing}$$

Solar oscillations

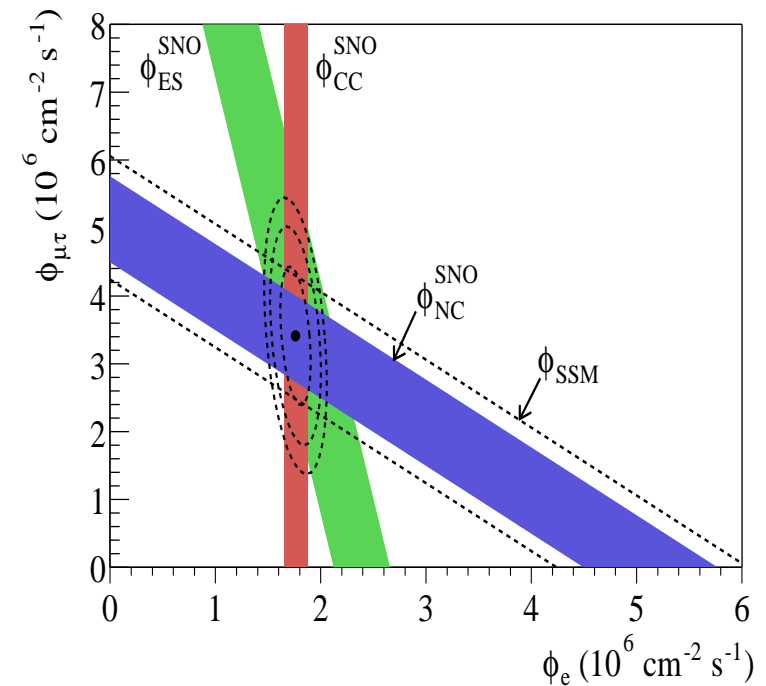


SNO, 2000 & 2002:

Solar oscillations



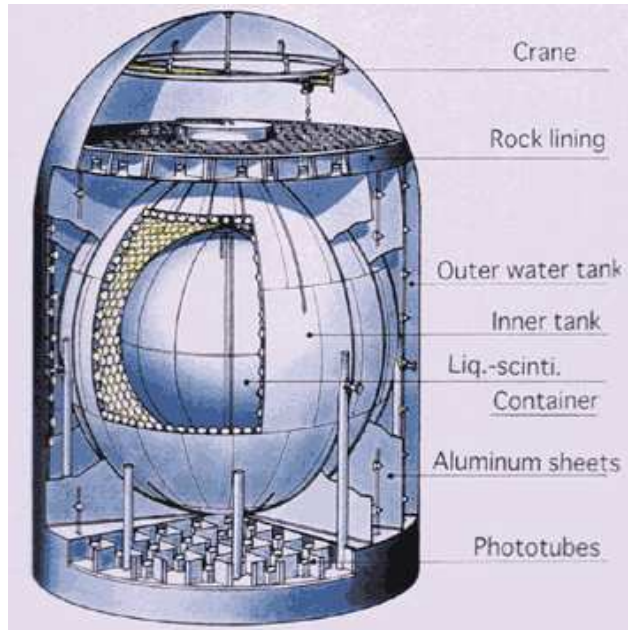
SNO, 2000 & 2002:



⇒ Measurement of **NC** confirms flavour conversion of ν_{\odot}

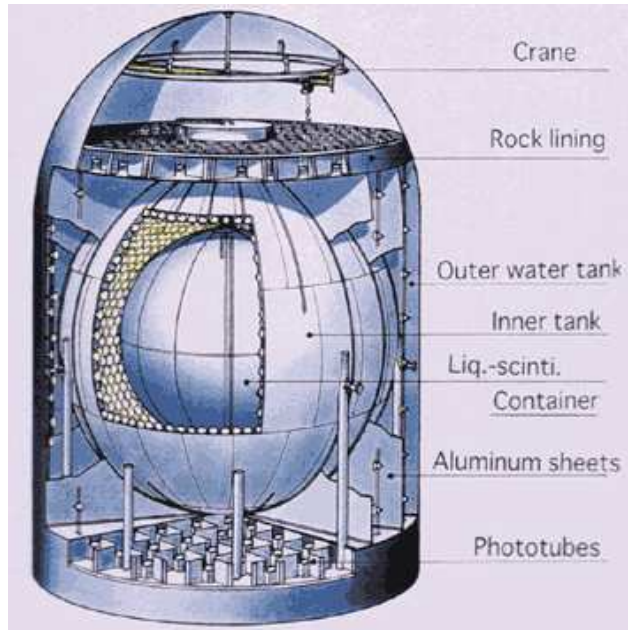
⇒ Oscillations as explanation likely, but not proven

Solar oscillations

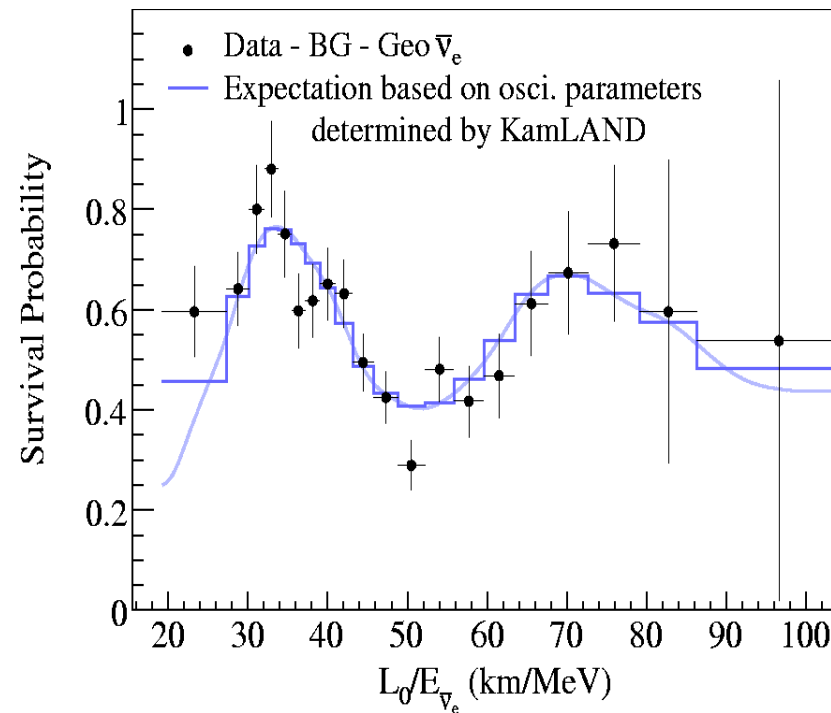


KamLAND 2002, & 2008:

Solar oscillations



KamLAND 2002, & 2008:



⇒ Measurement of **LE proves neutrino oscillations**

⇒ LA-MSW Oscillations as only explanation for ν_{\odot}

Solar neutrinos - fit

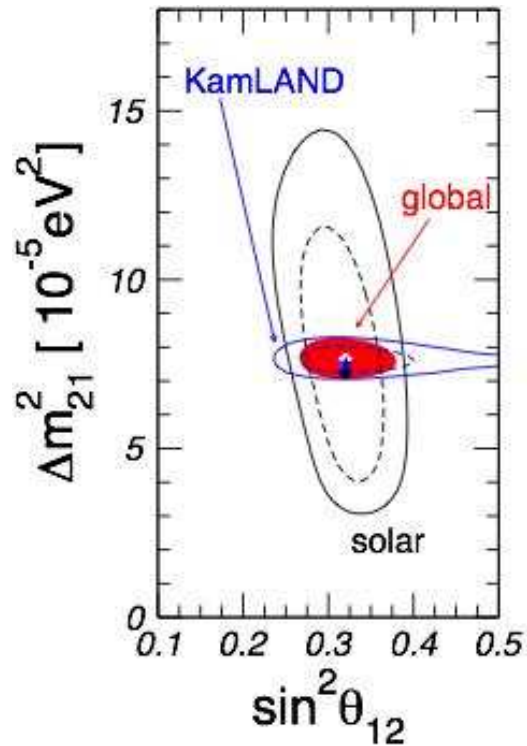


Fig from:
Forero, Tortola
& Valle, 2012

KamLAND - reactor data

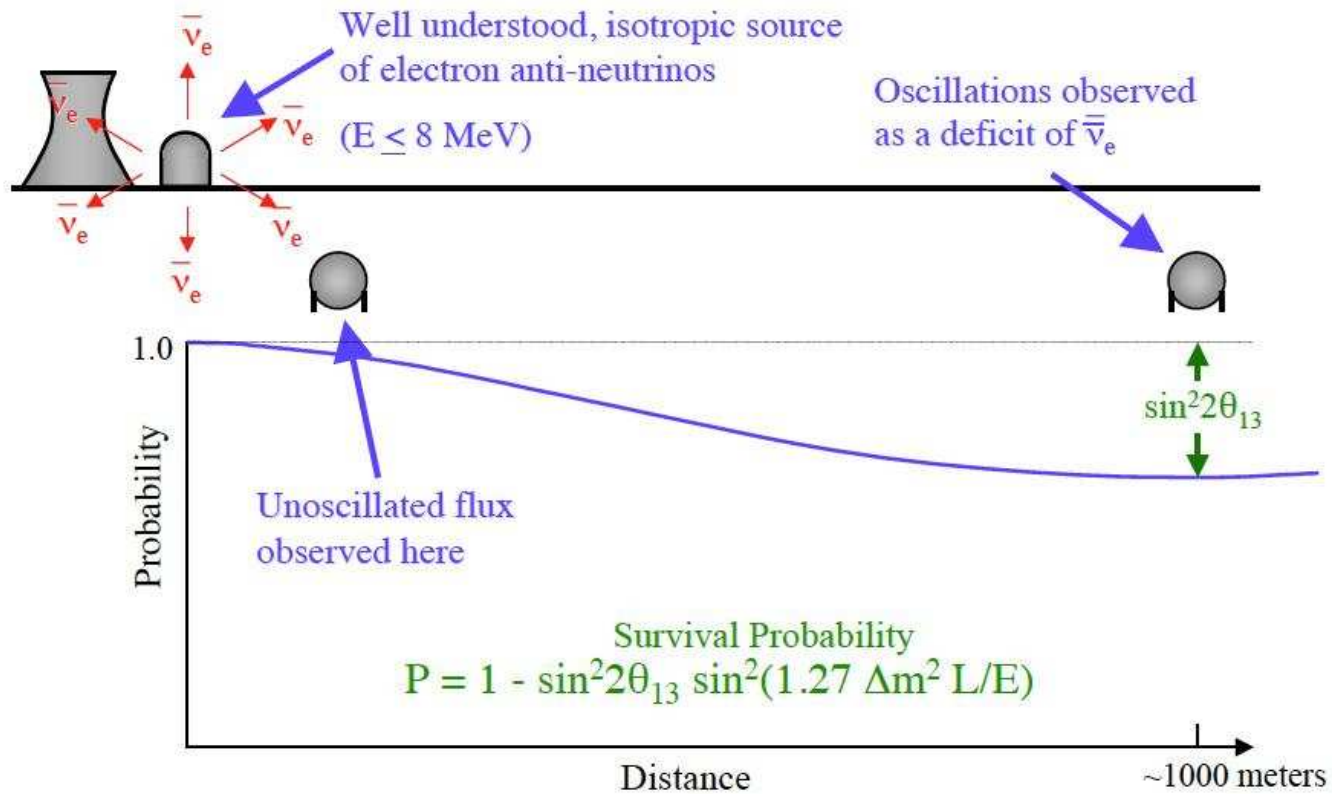
solar - SNO, SuperK, GALLEX, CL, etc ...

global - combination of all data

$$\Delta m_{\odot}^2 = (7.27 - 8.01) \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{\odot} = (0.27 - 0.37) - \text{consistent with } 1/3.$$

Reactor neutrinos



Reactor neutrinos



PRL 108 (2012) (arXiv:1112.6353)

$$\sin^2(2\theta_{13}) = 0.086 \pm 0.041(\text{stat}) \pm (0.030)(\text{syst})$$

Non-zero @ 2 σ c.l.



PRL 108 (2012) (arXiv:1203.1669)

$$\sin^2(2\theta_{13}) = 0.092 \pm 0.016(\text{stat}) \pm (0.005)(\text{syst})$$

Non-zero @ 5.2 σ c.l.

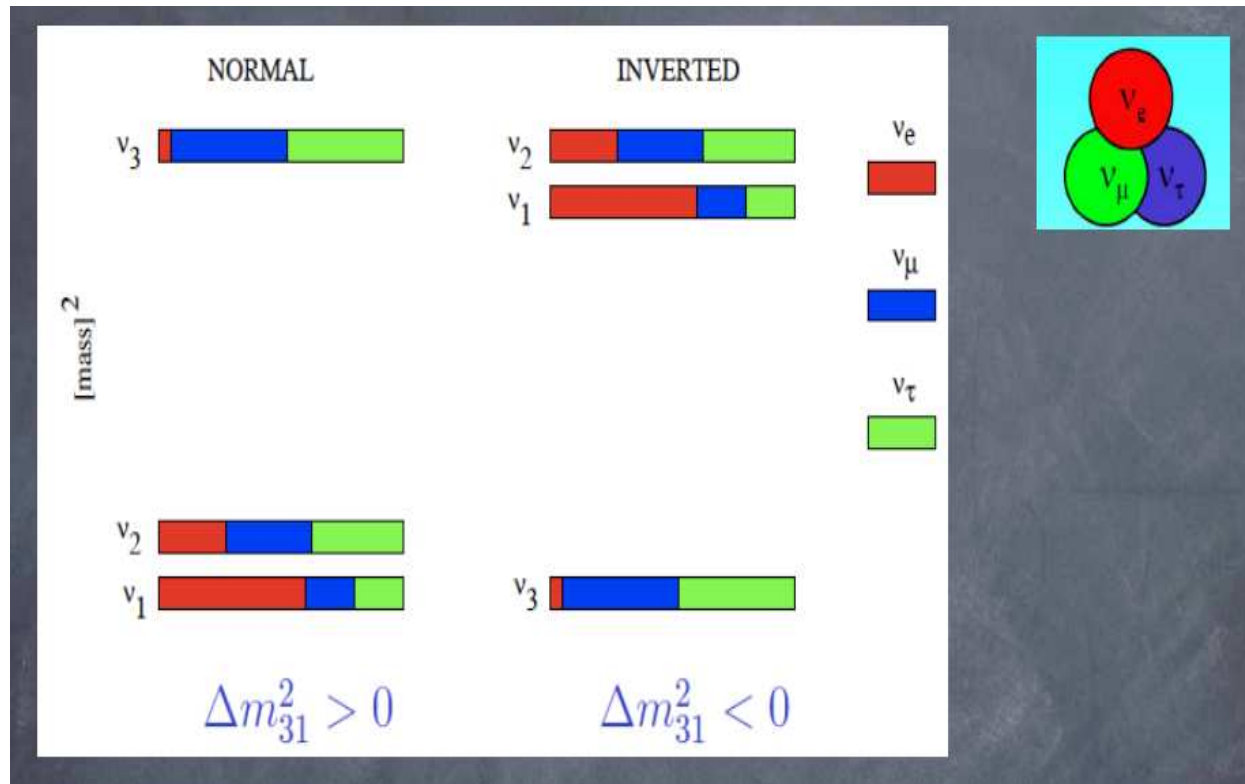


PRL 108 (2012) (arXiv:1204.0626)

$$\sin^2(2\theta_{13}) = 0.113 \pm 0.013(\text{stat}) \pm (0.019)(\text{syst})$$

Non-zero @ 4.9 σ c.l.

Don't know ν 's



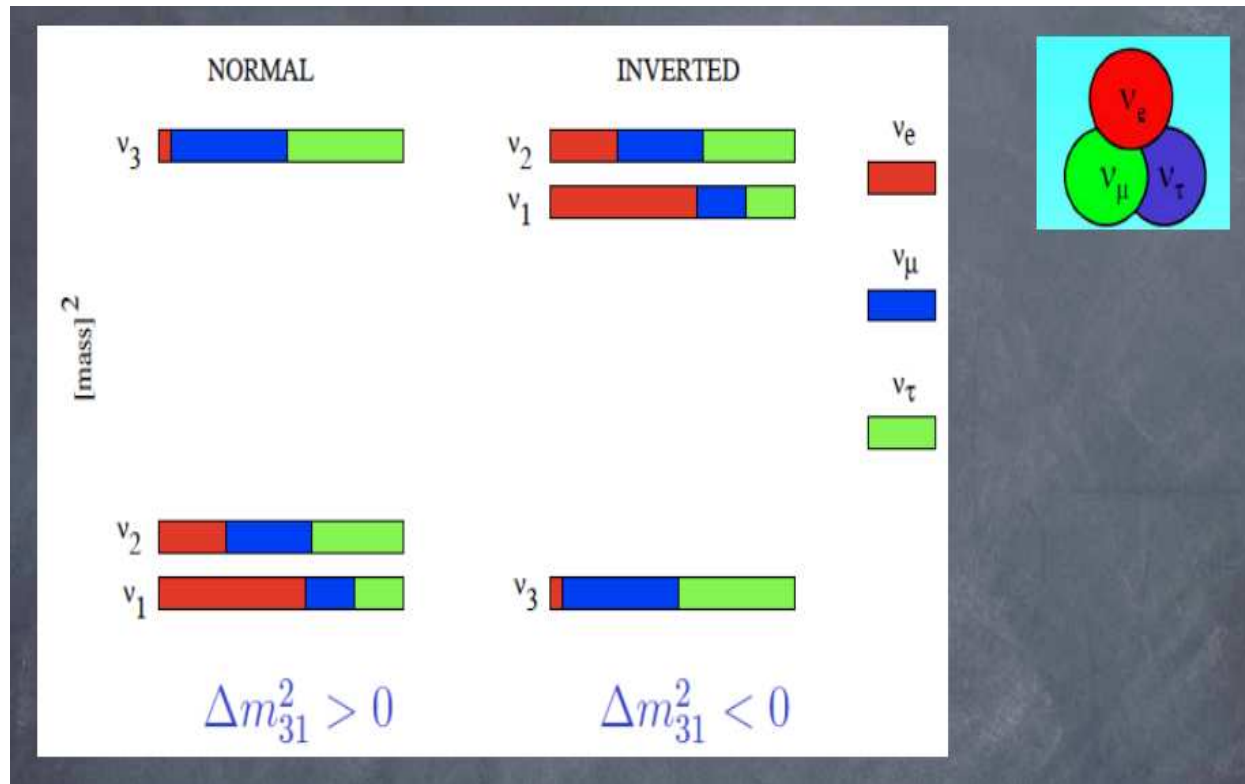
Open questions:

Which hierarchy: Normal or inverted?

What is the absolute neutrino mass scale?

Is there CP violation in the lepton sector?

Don't know ν 's



Open questions:

Which hierarchy: Normal or inverted?

What is the absolute neutrino mass scale?

Is there CP violation in the lepton sector?

Is lepton number violated???



Absolute mass scale

Tritium decay end point searches:

$$m_\nu^\beta = \sqrt{\sum_i |U_{ei}|^2 m_i^2} \leq 2.2 \text{ eV}$$

KATRIN:
 $m_\nu^\beta \leq 0.2 \text{ eV}$
2017 (??)

Double beta decay:

$$m_\nu^{\beta\beta} = \sum_i U_{ei}^2 m_i \leq (0.25 - 0.5) \text{ eV}$$

Majorana neutrino!

KamLAND-Zen
& EXO-200

Cosmology (CMB **Planck** + LSS + ...):

depending on data set!

$$\sum_i m_{\nu_i} \leq (0.3 - 1.0) \text{ eV} \quad \Leftarrow$$

$$\sum_i m_{\nu_i} \leq 1.0 \text{ eV}$$

Planck+BAO:

$$\sum_i m_{\nu_i} \leq 0.3 \text{ eV}$$

⇒ Recall for hierarchical neutrinos:

$$\sqrt{\Delta m_{\text{Atm}}^2} \sim 50 \text{ meV}$$

and

$$\sqrt{\Delta m_{\odot}^2} \sim 9 \text{ meV}$$



Future experiments

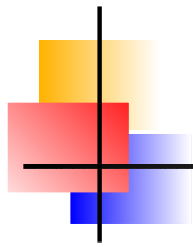
Currently running / under construction / commissioning:

	EXO-200	GERDA-I/II	CUORE	KamLAND-Zen
A^Z	^{136}Xe	^{76}Ge	^{130}Te	^{136}Xe
Mass	160 kg	35 kg	200 kg	400 kg
Method	liquid TPC	ionization	bolometer	scint.
Location	WIPP	LNGS	LNGS	Kamioka
Starts (?)	2010	2010	2012	2011
$T_{1/2}^{0\nu\beta\beta}$ (est.)	6.4×10^{25}	$3 \times 10^{25} - 1.5 \times 10^{26}$ *	$(2-6.5) \times 10^{26}$	6×10^{26}
$\langle m_\nu \rangle$ (est.) eV	0.19	0.28-0.12	0.03-0.05 *	0.02-0.06 **

Assumptions:

* - Background level $10^{-2} - 10^{-3} e/(\text{y} \cdot \text{kg} \cdot \text{keV})$, i.e. improvement $\simeq 20 - 200$

** - Phase II with 1 ton: 0.020 @ 5 years, BG with MC simulation



II.

Short aside on neutrino mass

or

Why is m_ν so small?



Dirac \mathcal{M}_ν

If Lepton Number is Conserved:

$$\mathcal{L} = \mathcal{L}^{SM} + Y_{ij}^\nu L_i H \nu_{R,j}$$

Experimental data requires: $|Y_\nu| \simeq 10^{-12}$

Fit to all oscillation data possible and simple, but ...

⇒ Any “predictions” of this scenario???



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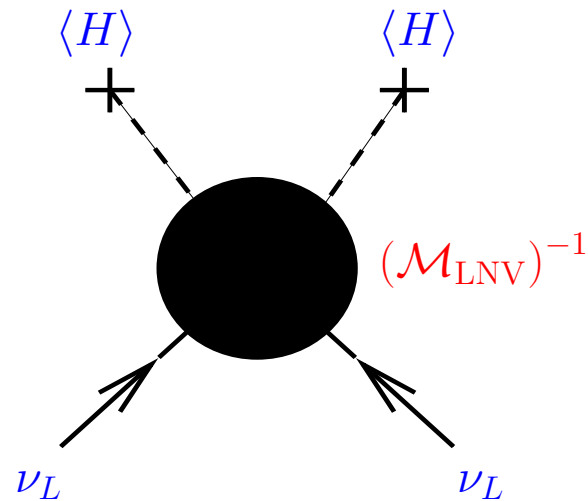
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⇒ Any “predictions” of this scenario???

- (i) No double beta decay
- (ii) No charged lepton flavour violation

Majorana \mathcal{M}_ν

If **L**epton **N**umber is **V**iolated:



Many realizations:

- (i) Seesaw mechanism: Type-I, Type-II, Type-III, Inverse seesaw, etc ...
- (ii) Radiative models: Zee, Babu, LQs ...
- (iii) SUSY neutrino masses: \tilde{H}_p
- (iv) ...

Weinberg, 1979

$$m_\nu = \frac{1}{\mathcal{M}_{LNV}} (LH)(LH)$$

Which scale?

$$\mathcal{M}_{LNV} \simeq M_{GUT}$$

or

$$\mathcal{M}_{LNV} \simeq M_{EW}$$

Seesaw mechanism

Seesaw type-I, right-handed neutrinos:

$$m_{1/2} \simeq \left(-\frac{Y_\nu^2 v^2}{M_M}, M_M \right)$$

⇒ For $M_M \sim 10^{15} \text{ GeV}$ $h_\nu \sim 1$

Seesaw type-II, scalar triplet:

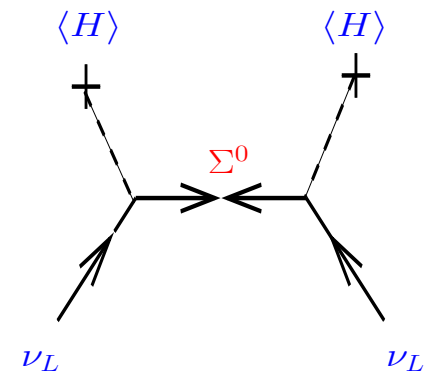
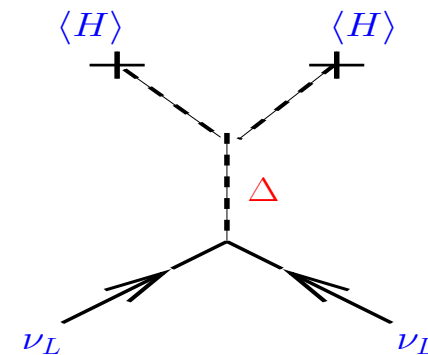
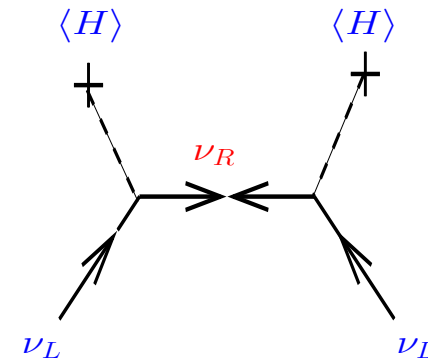
$$m_\nu \simeq Y_T \langle \Delta_L^0 \rangle \simeq Y_T \frac{v^2}{m_\Delta}$$

⇒ For $M_T \sim 10^{15} \text{ GeV}$ $Y_T \sim 1$

Type-III: Replace ν_R by $\Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$:

$$m_{1/2} \simeq \left(-\frac{Y_\Sigma^2 v^2}{M_\Sigma}, M_\Sigma \right)$$

⇒ Similar to type-I, but $\Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$





Linear & inverse seesaw

Inverse seesaw, basis (ν, ν^c, S) :

$$M_\nu = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix},$$

Mohapatra &
Valle, 1986

After EWSB the effective light neutrino mass matrix is given by

$$M_\nu = m_D M^{T^{-1}} \mu M^{-1} m_D^T.$$

Linear seesaw:

$$M_\nu = \begin{pmatrix} 0 & m_D & M_L \\ m_D^T & 0 & M \\ M_L^T & M^T & 0 \end{pmatrix}.$$

Akhmedov
et al., 1995

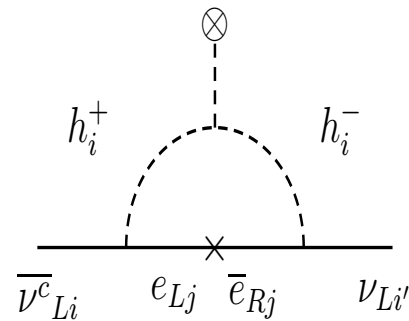
Light neutrino mass:

$$M_\nu = m_D (M_L M^{-1})^T + (M_L M^{-1}) m_D^T$$

Radiative models

Zee, 1981:

2 Higgs doublets
+ 1 charged singlet:

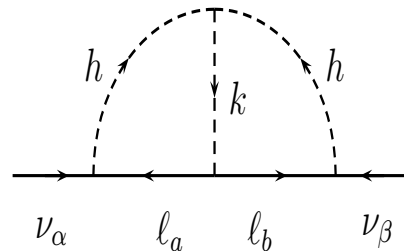


$$m_\nu \propto \frac{1}{16\pi^2} Y^2 \dots$$

Cheng & Li, 1980;

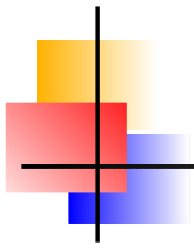
Zee, 1985; Babu, 1988:

1 singly charged singlet
+ 1 doubly charged singlet:



$$m_\nu \propto \left(\frac{1}{16\pi^2}\right)^2 Y^3 \mu \dots$$

+ many others $\dots \Rightarrow M_{LNV} \simeq M_{EW}$



III.

Charged lepton flavour violation

or

At which scale is the new physics?



Experimental status: LFV

Decay	Current Limit
$\tau \rightarrow \mu\gamma$	$4.4 \cdot 10^{-8}$
$\tau \rightarrow e\gamma$	$3.3 \cdot 10^{-8}$
$\mu \rightarrow e\gamma$	$2.4 \cdot 10^{-12}$
$\tau \rightarrow 3\mu$	$2.1 \cdot 10^{-8}$
$\tau^- \rightarrow e^- \mu^+ \mu^-$	$2.7 \cdot 10^{-8}$
$\tau^- \rightarrow e^+ \mu^- \mu^-$	$1.7 \cdot 10^{-8}$
$\tau^- \rightarrow \mu^- e^+ e^-$	$1.8 \cdot 10^{-8}$
$\tau^- \rightarrow \mu^+ e^- e^-$	$1.5 \cdot 10^{-8}$
$\tau \rightarrow 3e$	$2.7 \cdot 10^{-8}$
$\mu \rightarrow 3e$	$1 \cdot 10^{-12}$

Particle Data Group
2012

Updated MEG, 2013:
 $\text{Br}(\mu \rightarrow e\gamma) \lesssim 5.7 \cdot 10^{-13}$

Proposed MEG upgrade:
 $\text{Br}(\mu \rightarrow e\gamma) \lesssim 6 \cdot 10^{-14}$

Mu3E and MUSIC:
 $\text{Br}(\mu \rightarrow eee) \lesssim 10^{-16}$



Experimental status: LFV

Capture	Current Limit
$\mu^- \text{}^{32}\text{S} \rightarrow e^- \text{}^{32}\text{S}$	$7 \cdot 10^{-11}$
$\mu^- \text{}^{32}\text{S} \rightarrow e^+ \text{}^{32}\text{Si}$	$9 \cdot 10^{-10}$
$\mu^- \text{Ti} \rightarrow e^- \text{Ti}$	$4.3 \cdot 10^{-12}$
$\mu^- \text{Ti} \rightarrow e^+ \text{Ca}$	$3.6 \cdot 10^{-11}$
$\mu^- \text{Pb} \rightarrow e^- \text{Pb}$	$4.6 \cdot 10^{-11}$
$\mu^- \text{Au} \rightarrow e^- \text{Au}$	$7 \cdot 10^{-13}$

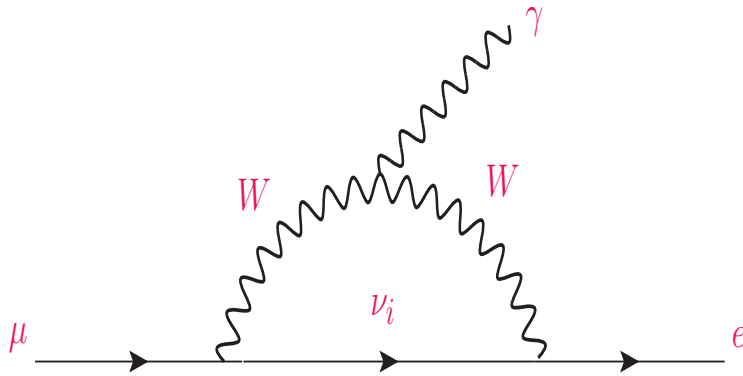
Particle Data Group
2012

Future sensitivity:
Mu2E (FermiLab)
& COMET (Japan):
 $\sim 10^{-16}$

2020+?
Prisme/Prime (J-Parc):
 $\sim 10^{-18}$

Guaranteed CLFV

Oscillations experiments have shown that $m_\nu \neq 0$:

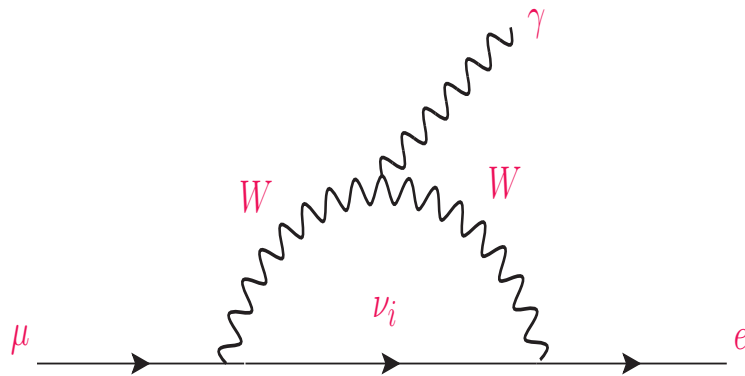


$$\text{Br}(\mu \rightarrow e \gamma) \sim \frac{3\alpha}{32\pi} \left(\sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{i1}^2}{m_W^2} \right)^2 \leq 10^{-53}$$

\Rightarrow GIM suppressed by small neutrino masses

Guaranteed CLFV

Oscillations experiments have shown that $m_\nu \neq 0$:



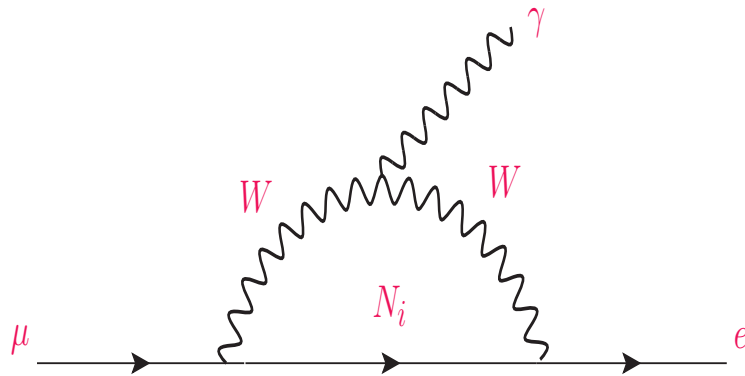
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\Rightarrow GIM suppressed by small neutrino masses

Any observation of **charged LFV**
points to **physics beyond** neutrino masses

CLFV beyond m_ν

Simple example: Heavy neutrinos (N) with $m_N \mathcal{O}(TeV)$:



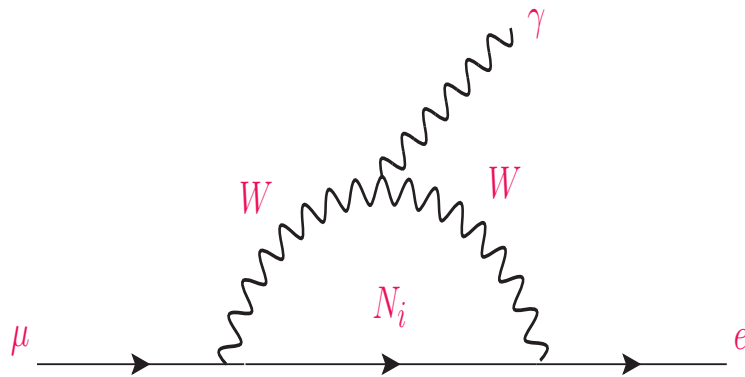
$$\text{Br}(\mu \rightarrow e \gamma) \sim \frac{\alpha^3 s_W^2}{256 \pi^2} \frac{m_\mu^5}{m_W^4 \Gamma_\mu} \left(\sum_i K_{\mu i}^* K_{e i} G\left(\frac{m_{N_k}^2}{m_W^2}\right) \right)^2$$

$$\leq 9 \times 10^{-6} \left(\sum_i K_{\mu i}^* K_{e i} G\left(\frac{m_{N_k}^2}{m_W^2}\right) \right)^2$$

- K_{ik} heavy neutrino - lepton mixing
- $G(x)$ loop function, $G(1) = 1/8$

CLFV beyond m_ν

Simple example: Heavy neutrinos (N) with $m_N \mathcal{O}(TeV)$:



$$\text{Br}(\mu \rightarrow e\gamma) \sim \frac{\alpha^3 s_W^2}{256\pi^2} \frac{m_\mu^5}{m_W^4 \Gamma_\mu} \left(\sum_i K_{\mu i}^* K_{ei} G\left(\frac{m_{N_k}^2}{m_W^2}\right) \right)^2$$

$$\leq 9 \times 10^{-6} \left(\sum_i K_{\mu i}^* K_{ei} G\left(\frac{m_{N_k}^2}{m_W^2}\right) \right)^2$$

- K_{ik} heavy neutrino - lepton mixing
- $G(x)$ loop function, $G(1) = 1/8$

Practically **any** extension of SM
with new states at TeV scale
generates **large charged LFV!**



(C)LFV - Models

⇒ Example models that produce sizeable CLFV:

- TeV scale seesaw: [Inverse seesaw](#), [linear seesaw](#), etc.
- Radiative neutrino mass models: [Zee-](#), [Babu-Zee model](#), etc.
- RPC [Supersymmetry](#)
- [RPV Supersymmetry](#)
- Practically any extended Higgs sector:
Little Higgs models, additional Higgs doublets, triplets, etc...
- Extra (large) dimensions
- etc ...

⇒ In fact, many models generate way to much CLFV:

“[Flavour problem](#)” of BSM



The MSSM: Superpartners

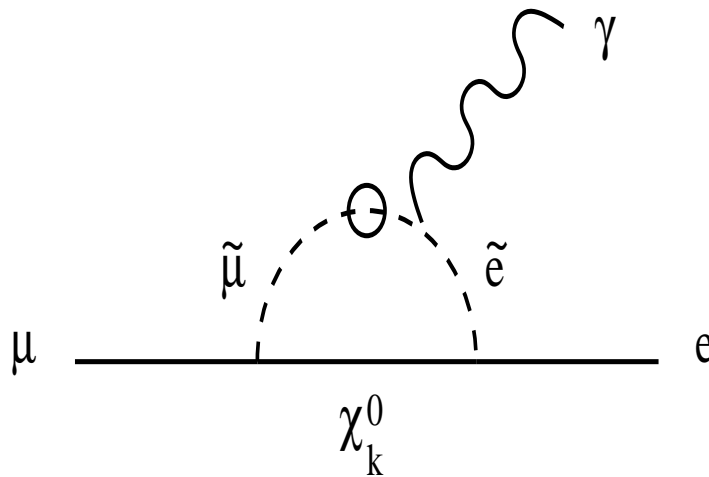
Superfield	Bosons	Fermions	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
Gauge Multiplets					
\widehat{G}	g	\widetilde{g}	8	0	0
\widehat{V}	W^a	\widetilde{W}^a	1	3	0
\widehat{V}'	B	\widetilde{B}	1	1	0
Matter Multiplets					
\widehat{L}	$(\widetilde{\nu}, \widetilde{e}_L^-)$	(ν, e_L^-)	1	2	-1
\widehat{E}^C	\widetilde{e}_R^+	e_L^c	1	1	2
\widehat{Q}	$(\widetilde{u}_L, \widetilde{d}_L)$	(u_L, d_L)	3	2	1/3
\widehat{U}^C	\widetilde{u}_R^*	u_L^c	3^*	1	-4/3
\widehat{D}^C	\widetilde{d}_R^*	d_L^c	3^*	1	2/3
Higgs Multiplets					
\widehat{H}_d	(H_d^0, H_d^-)	$(\widetilde{H}_d^0, \widetilde{H}_d^-)$	1	2	-1
\widehat{H}_u	(H_u^+, H_u^0)	$(\widetilde{H}_u^+, \widetilde{H}_u^0)$	1	2	1

Slepton mixing

Soft SUSY breaking:

$$V = (m_{\tilde{L}}^2)_{ij} \tilde{L}_i^* \tilde{L}_j + \dots$$

Off-diagonal elements induce decays,
such as:



$$\sim (m_{\tilde{L}}^2)_{21}$$

Example only!

$$\delta_{12} = \frac{(m_{\tilde{L}}^2)_{21}}{m_{SUSY}^2} \lesssim 10^{-4}$$



mSUGRA

Boundary conditions: **mSUGRA** (“minimal Supergravity”) :

$$M_1 = M_2 = M_3 = M_{1/2},$$

$$m_{H_u}^2 = m_{H_d}^2 = m_0^2,$$

$$M_{\tilde{Q}}^2 = M_{\tilde{U}}^2 = M_{\tilde{D}}^2 = M_{\tilde{L}}^2 = M_{\tilde{E}}^2 = m_0^2 \mathbf{1}_3,$$

$$A_d = A_0 Y_d, A_u = A_0 Y_u, A_e = A_0 Y_e.$$

⇐ Flavour blind SUSY breaking!

⇒ # of parameters: $4\frac{1}{2}$ ($m_0, M_{1/2}, A_0, \tan \beta, \text{sgn}(\mu)$)

⇒ Sometimes also called the **CMSSM** (C = constrained)

⇒ All low energy masses can then be calculated by **RGE**
 (“renormalization group equations”)

⇒ **No neutrino masses and no LFV**



mSugra and RGEs

Seesaw type-I:

Borzumati & Masiero, 1986

$$(\Delta M_{\tilde{L}}^2)_{ij} \sim -\frac{1}{8\pi^2} f(m_0, A_0, M_{1/2}, \dots) (Y_\nu^\dagger L Y_\nu)_{ij}$$

Hisano et al. 1996, 1999
Arganda & Herrero, 2006

...

Note: $L_i = \log[M_G/M_i]$.

⇒ 9 new independent parameters

Seesaw type-II:

Rossi, 2002

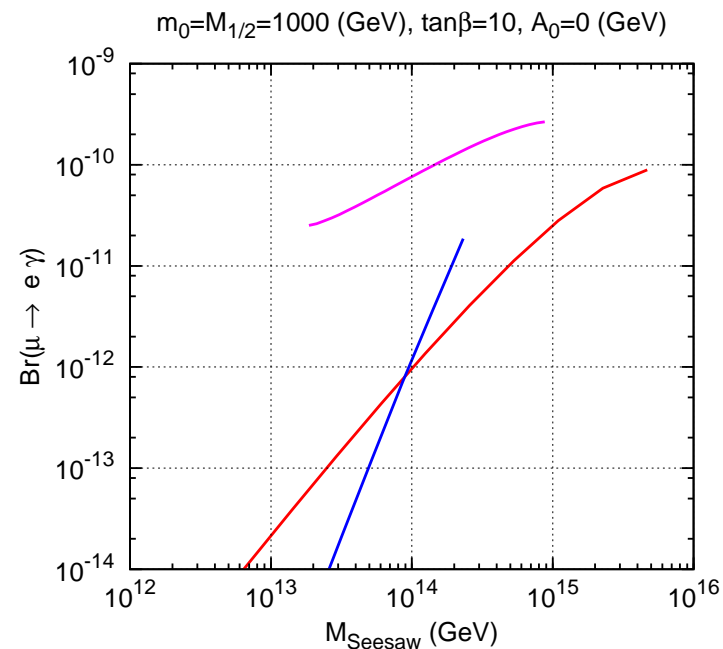
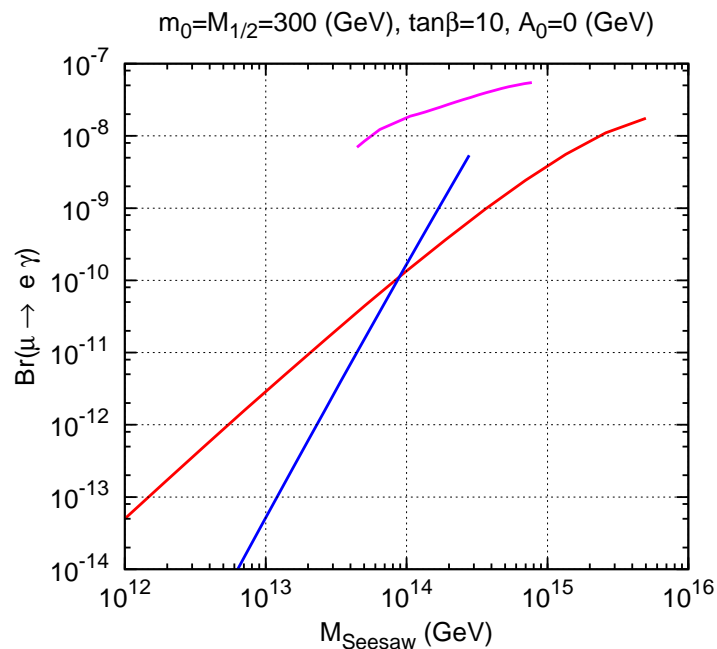
$$(\Delta M_{\tilde{L}}^2)_{ij} \sim -\frac{1}{8\pi^2} g(m_0, A_0, M_{1/2}, \dots) (Y_T^\dagger Y_T)_{ij} \log(M_G/M_T)$$

⇒ 9 entries, but proportional to Y_T^2

⇒ Measuring all entries in $(\Delta M_{\tilde{L}}^2)_{ij}$ “over-constrains” type-II seesaw!

Note: type-III equation as type-I, but larger LFV ... see below

$\mu \rightarrow e\gamma$ in $mSugra$ seesaw



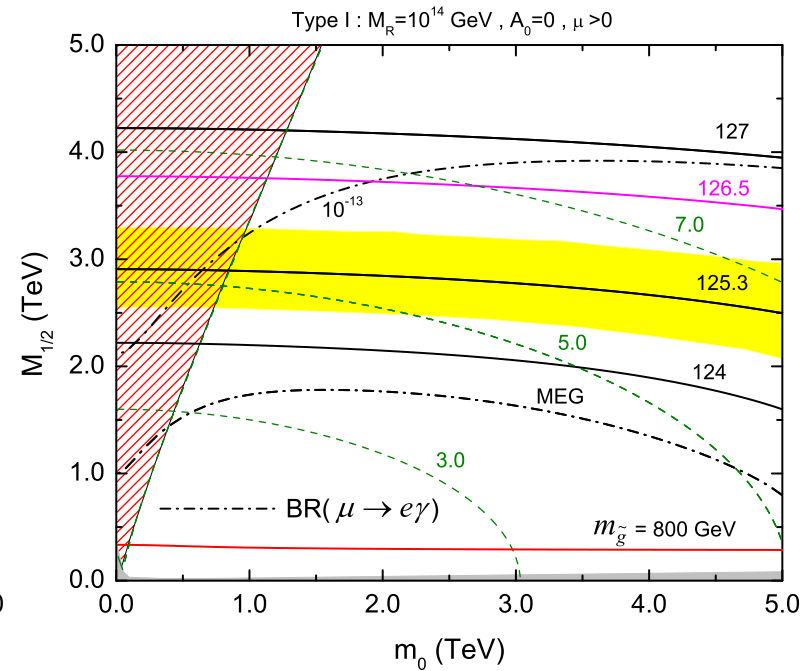
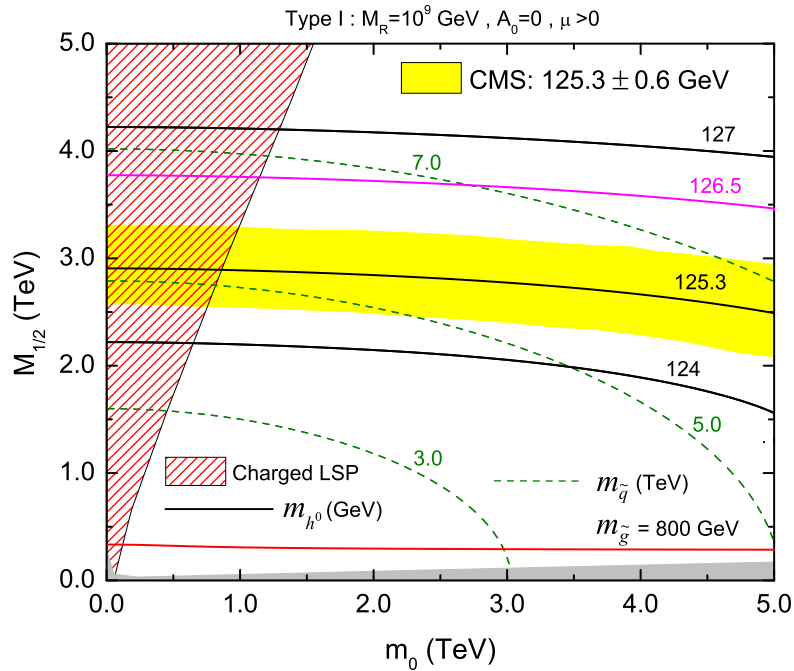
⇒ The three different seesaws are: **type-III**, **type-II** and **type-I**

⇒ General expectation: “Large” LFV for “large” M_{Seesaw}

⇒ General expectation LFV in **type-III** \gg **type-I**

m_{h^0} and LFV in SUSY seesaw

Seesaw type-I:



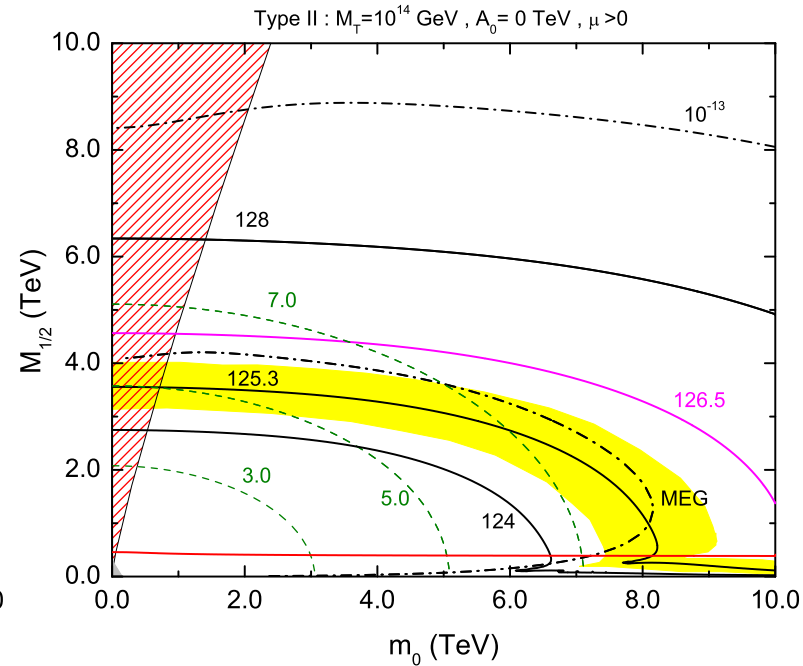
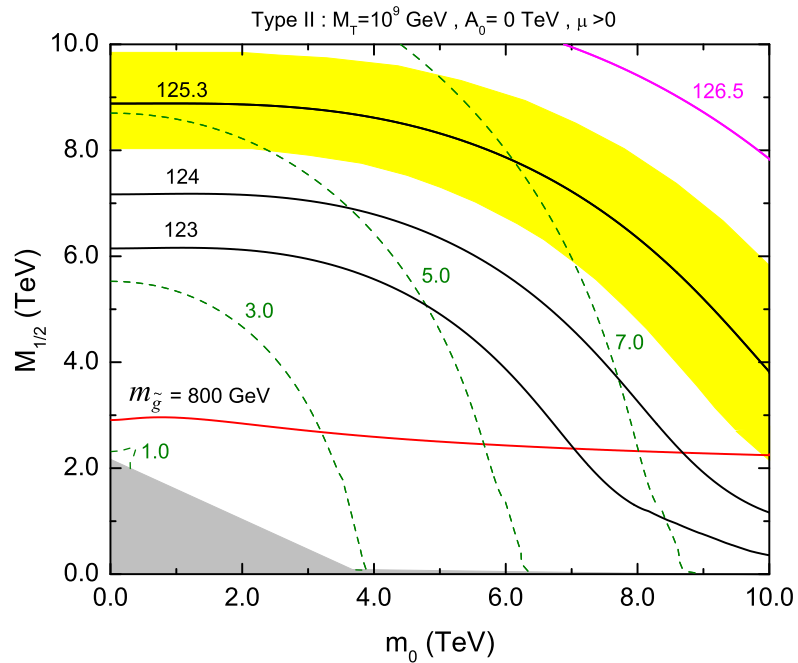
$\Rightarrow M_{\nu_R} = 10^9$ GeV (left) and $M_{\nu_R} = 10^{14}$ GeV (right)

\Rightarrow Yellow: Allowed band from $m_{h^0} = 125.3 \pm 0.6$ GeV

\Rightarrow CLFV constrains large M_{ν_R}

m_{h^0} and LFV in SUSY seesaw

Seesaw type-II:



$\Rightarrow M_T = 10^9$ GeV (left) and $M_T = 10^{14}$ GeV (right)

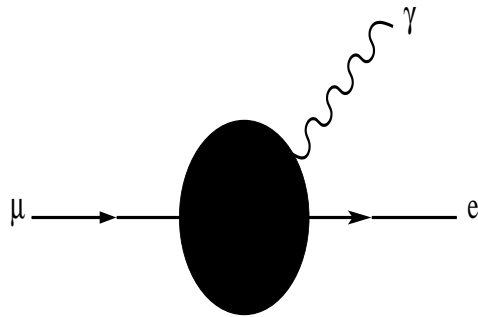
\Rightarrow Yellow: Allowed band from $m_{h^0} = 125.3 \pm 0.6$ GeV

\Rightarrow CLFV and m_{h^0} constrain large M_T

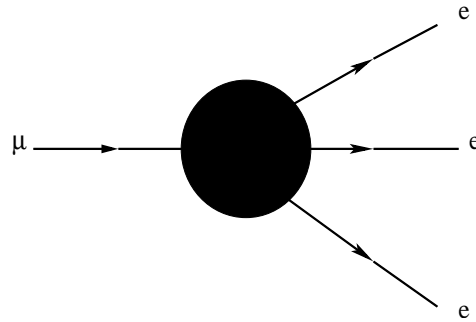


Schematically:

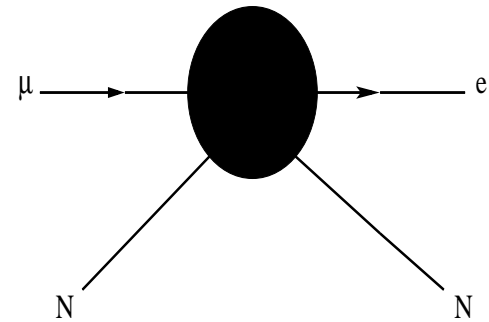
$\mu \rightarrow e\gamma$:



$\mu \rightarrow 3e$



μ -capture:



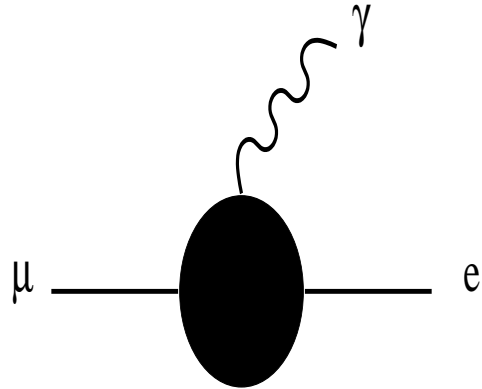
Can we learn about
different BSM models
from different LFV processes?



$\mu \rightarrow e\gamma$ *versus* $\mu \rightarrow 3e$

Consider $\mu \rightarrow e\gamma$:

Some physics
beyond SM
generates blob:

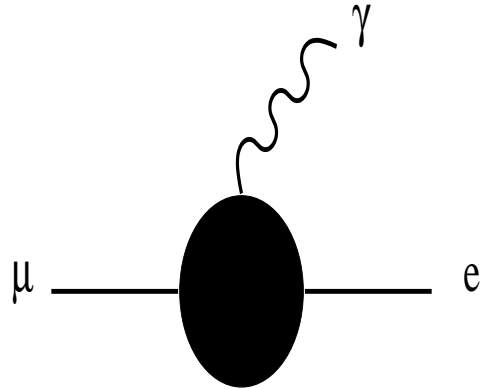




$\mu \rightarrow e\gamma$ *VERSUS* $\mu \rightarrow 3e$

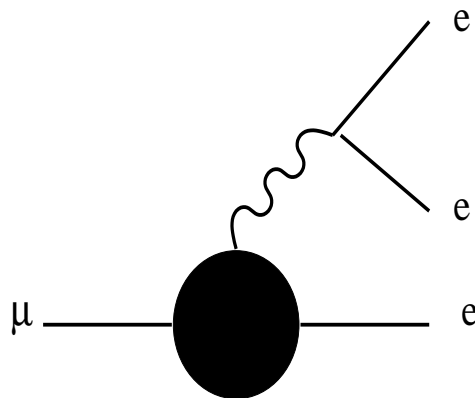
Consider $\mu \rightarrow e\gamma$:

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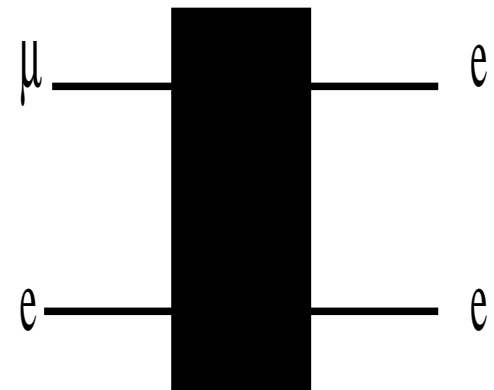


Compare $\mu \rightarrow 3e$:

Same blob
appears in
 $\mu \rightarrow 3e$



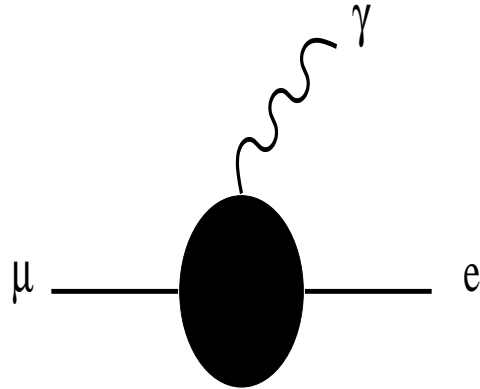
+



$\mu \rightarrow e\gamma$ VERSUS $\mu \rightarrow 3e$

Consider $\mu \rightarrow e\gamma$:

Some physics beyond SM generates blob:

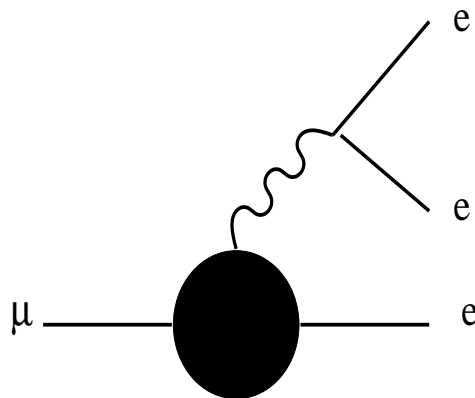


If photon diagram dominates:

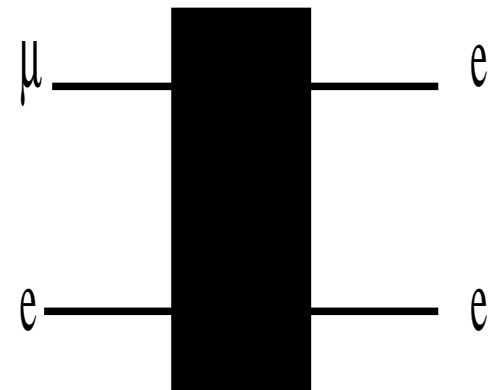
$$Br(l_i \rightarrow l_j l_k l_k) \sim \alpha \times Br(e \rightarrow l_j + \gamma)$$

Compare $\mu \rightarrow 3e$:

Same blob appears in $\mu \rightarrow 3e$



+



Simple example

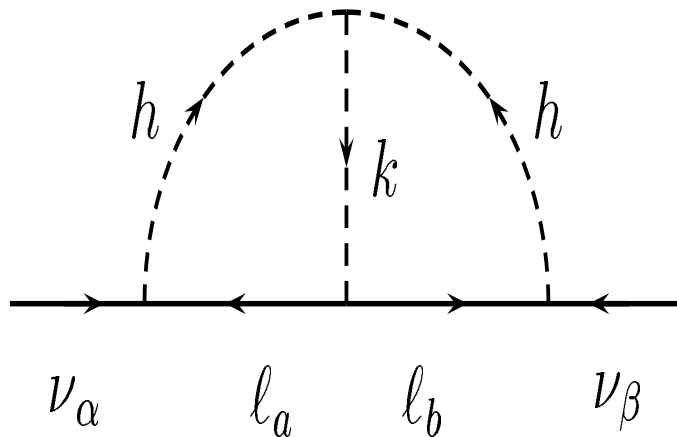
Babu-Zee model for neutrino mass:

$$\mathcal{L} = f(L^T L)h^+ + g(e_R^T e_R)k^{++} - \mu h^+ h^+ k^{--}$$

Cheng & Li, 1980

Zee, 1985

Babu, 1988



Neutrino mass is
2-loop suppressed!

Babu & Macesanu, 2003

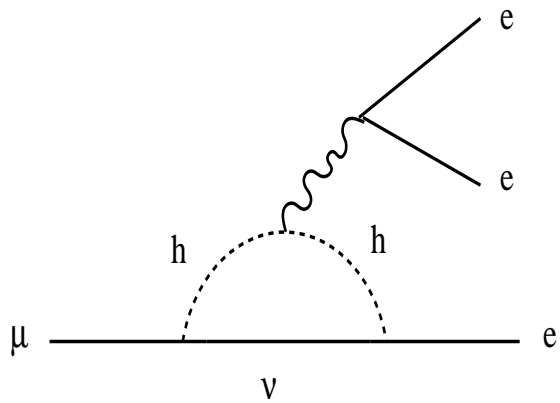
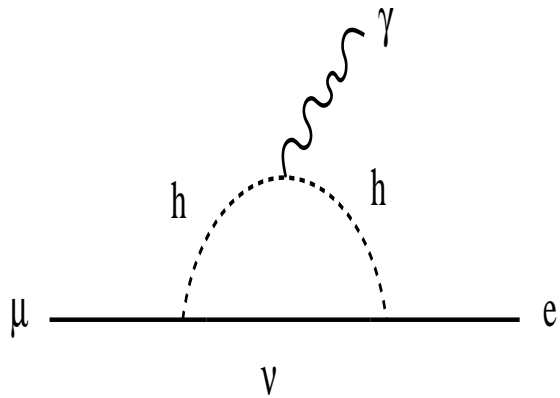
Aristizabal & Hirsch, 2006

$$\mathcal{M}_{\alpha\beta}^\nu = \frac{8\mu}{(16\pi^2)^2 m_h^2} f_{\alpha a} m_a g_{xy} m_b f_{b\beta} \mathcal{I}\left(\frac{m_k^2}{m_h^2}\right),$$

Large neutrino mixing angles
require large CLFV

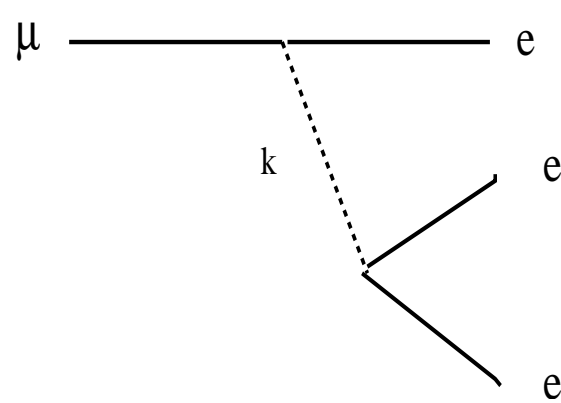
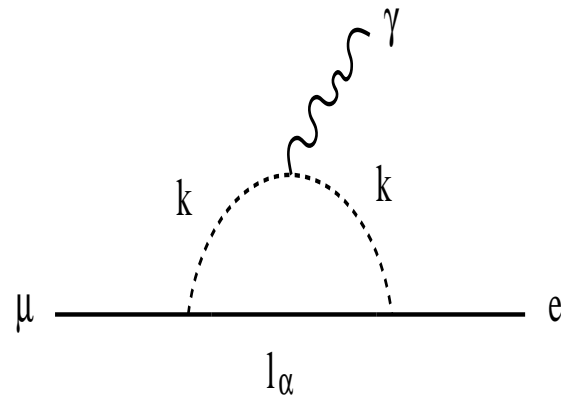
CLFV in Babu-Zee model

If $\frac{g^2}{m_k^2} \ll \frac{f^2}{m_h^2}$:



Photon dominance!

if $\frac{f^2}{m_h^2} \ll \frac{g^2}{m_k^2}$:



$\mu \rightarrow 3e$ tree-level!

Photon dominance?

From [Buras et al., 2010](#): Different particle models predict different ratios for ...

ratio	LHT	MSSM (dipole)	MSSM (Higgs)	SM4
$\frac{\text{Br}(\mu^- \rightarrow e^- e^+ e^-)}{\text{Br}(\mu \rightarrow e \gamma)}$	0.02... 1	$\sim 6 \cdot 10^{-3}$	$\sim 6 \cdot 10^{-3}$	0.06 ... 2.2
$\frac{\text{Br}(\tau^- \rightarrow e^- e^+ e^-)}{\text{Br}(\tau \rightarrow e \gamma)}$	0.04... 0.4	$\sim 1 \cdot 10^{-2}$	$\sim 1 \cdot 10^{-2}$	0.07 ... 2.2
$\frac{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{\text{Br}(\tau \rightarrow \mu \gamma)}$	0.04... 0.4	$\sim 2 \cdot 10^{-3}$	0.06 ... 0.1	0.06 ... 2.2
$\frac{\text{Br}(\tau^- \rightarrow e^- \mu^+ \mu^-)}{\text{Br}(\tau \rightarrow e \gamma)}$	0.04... 0.3	$\sim 2 \cdot 10^{-3}$	0.02 ... 0.04	0.03 ... 1.3
$\frac{\text{Br}(\tau^- \rightarrow \mu^- e^+ e^-)}{\text{Br}(\tau \rightarrow \mu \gamma)}$	0.04... 0.3	$\sim 1 \cdot 10^{-2}$	$\sim 1 \cdot 10^{-2}$	0.04 ... 1.4
$\frac{\text{Br}(\tau^- \rightarrow e^- e^+ e^-)}{\text{Br}(\tau^- \rightarrow e^- \mu^+ \mu^-)}$	0.8... 2	~ 5	0.3... 0.5	1.5 ... 2.3
$\frac{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{\text{Br}(\tau^- \rightarrow \mu^- e^+ e^-)}$	0.7... 1.6	~ 0.2	5... 10	1.4 ... 1.7
$\frac{\text{R}(\mu \text{Ti} \rightarrow e \text{Ti})}{\text{Br}(\mu \rightarrow e \gamma)}$	$10^{-3} \dots 10^2$	$\sim 5 \cdot 10^{-3}$	0.08 ... 0.15	$10^{-12} \dots 26$

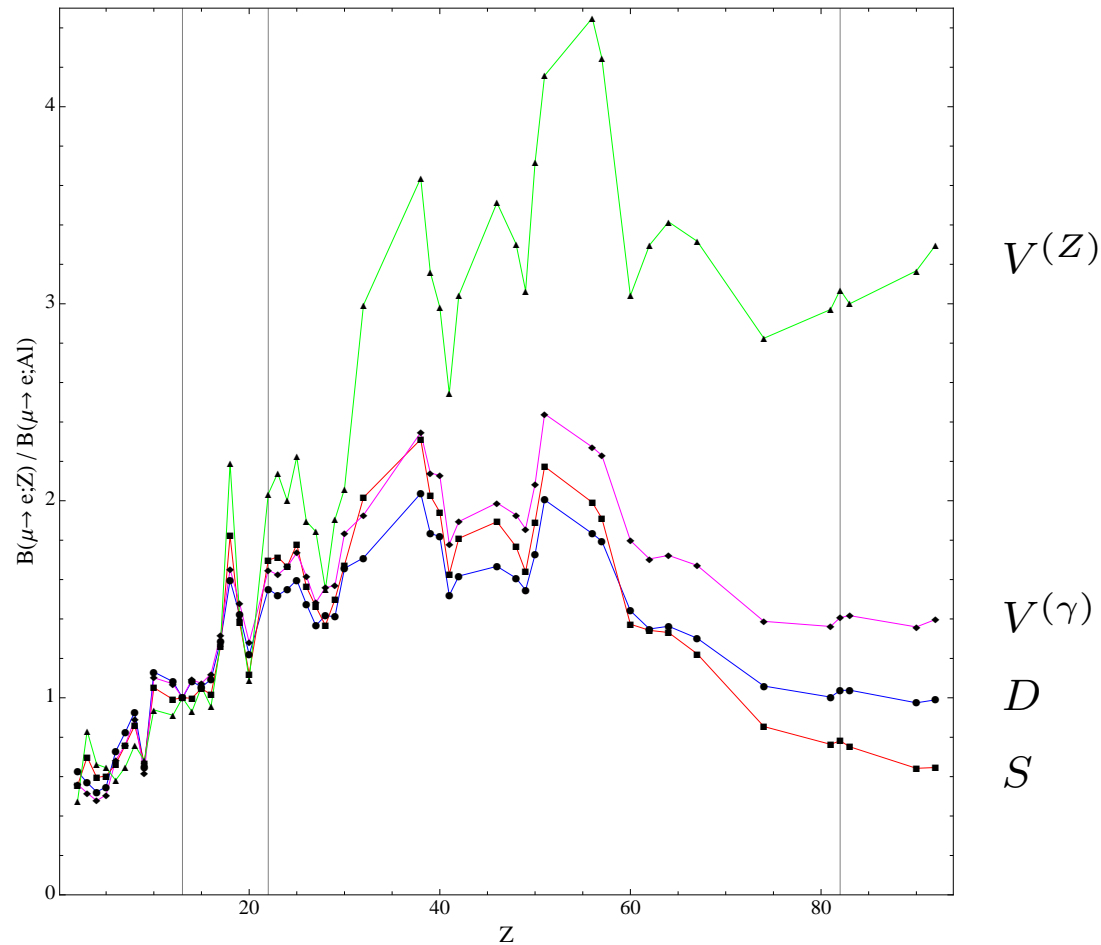
LHT: Little Higgs model with T-parity

MSSM: Minimal supersymmetric model (with R_P)

SM4: Standard model with 4th generation

μ -capture: Different targets

Fig. from Cirigliano et al., 2009



Kitano et al., 2002

μ -capture
on different
nuclei
normalized
to ^{26}Al

\Rightarrow use different nuclear targets to distinguish different operators



Conclusions

- ⇒ lepton flavour is violated - **neutrino oscillations**
- ⇒ all (active) neutrino angles have been measured
- ⇒ Δm_{ij}^2 known with precision
- ⇒ Since 2012 **all active neutrino angles measured**
- ⇒ CP-violation **not yet proven experimentally**

- ⇒ lepton number violation? - **neutrinoless double beta decay**



Conclusions

- ⇒ lepton flavour is violated - **neutrino oscillations**
- ⇒ all (active) neutrino angles have been measured
- ⇒ Δm_{ij}^2 known with precision
- ⇒ Since 2012 **all active neutrino angles measured**
- ⇒ CP-violation **not yet proven experimentally**

- ⇒ lepton number violation? - **neutrinoless double beta decay**

- ⇒ charged lepton flavour not observed

- ⇒ several orders of magnitude improvements expected
Room for discovery!