Computer tools in particle physics

- Lecture 5 : odds and ends -

Avelino Vicente IFIC – CSIC / U. Valencia

Curso de doctorado de la U. València

IFIC May 22-26 2017

IFIC 2017

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Outline of the lecture

- Propaganda
 - FlavorKit
 - DsixTools
- Other popular tools
- Questions, comments, ...



Chuck Norris fact of the day

When Chuck Norris does a pushup, he isn't lifting himself up, he's pushing the Earth down



FlavorKit

W. Porod, F. Staub, A. Vicente

Manual: arXiv:1405.1434 Website: http://sarah.hepforge.org/FlavorKit.html

Step 1: Consider a lagrangian that includes all the operators relevant for the flavor observable

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Example: $BR(\mu \rightarrow e\gamma)$

[In the SM extended with Dirac neutrino masses]

Step 1: Consider a lagrangian that includes all the operators relevant for the flavor observable

$$\mathcal{L}_{\mu e\gamma} = ie \, m_\mu \, \bar{e} \, \sigma^{\mu\nu} q_\nu \left(\frac{K_2^L P_L + K_2^R P_R}{\mu P_L} \right) \mu A_\mu + \text{h.c.}$$

Dipole interaction lagrangian

 K_2^L, K_2^R : Wilson coefficients

Example: $BR(\mu \rightarrow e\gamma)$

[In the SM extended with Dirac neutrino masses]

Step 2: Compute the Wilson coefficients at a given loop order



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Example: BR($\mu \rightarrow e\gamma$)

[In the SM extended with Dirac neutrino masses]

Step 3: Plug the results for the Wilson coefficients into a general expression for the flavor observable

$$BR(\mu \to e\gamma) = \frac{\alpha m_{\mu}^{5}}{4 \Gamma_{\mu}} \left(|K_{2}^{L}|^{2} + |K_{2}^{R}|^{2} \right)$$

Step 1: Consider a lagrangian that includes all the operators relevant for the flavor observable

Some freedom. Requires a good understanding of the observable but technically easy

Step 2: Compute the Wilson coefficients at a given loop order

Complicated and model dependent part of the computation

Step 3: Plug the results for the Wilson coefficients into a general expression for the flavor observable

Model independent. Can make use of results in the literature

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Usual approach



Usual approach

Compute!



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FlavorKit

To compute flavor observables one needs:

- 1) Expressions for all vertices and masses ---- SAR
 2) Expressions for the Wilson coefficients ---- Feyn
 - 3) Expressions for the observables
 - 4) Numerical evaluation



FlavorKit is the combination of these tools

How to use FlavorKit

Basic usage

For those who do not need any operator nor observable beyond what is already implemented in FlavorKit. In this case, FlavorKit reduces to the standard SARAH package.

Observables already in FlavorKit

Lepton flavor	Quark flavor
$\ell_lpha o \ell_eta \gamma$	$B^0_{s,d} \to \ell^+ \ell^-$
$\ell_{lpha} ightarrow 3 \ell_{eta}$	$\bar{B} \to X_s \gamma$
$\mu - e$ conversion in nuclei	$\bar{B} \to X_s \ell^+ \ell^-$
$\tau \to P\ell$	$\bar{B} \to X_{d,s} \nu \bar{\nu}$
$h \to \ell_{\alpha} \ell_{\beta}$	$B \to K \ell^+ \ell^-$
$Z \to \ell_{\alpha} \ell_{\beta}$	$K \to \pi \nu \bar{\nu}$
	$\Delta M_{B_{s,d}}$
	ΔM_K and ε_K
	$P \to \ell \nu$

Ready to be computed in your favourite model!

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How to use FlavorKit

Basic usage

For those who do not need any operator nor observable beyond what is already implemented in FlavorKit. In this case, FlavorKit reduces to the standard SARAH package.

Advanced usage

For those with further requirements:

- New observables
- New operators



2nd Chuck Norris fact of the day

Chuck Norris can run collider simulations with MadGraph on an abacus



A. Celis, J. Fuentes-Martín, A. Vicente, J. Virto

Manual: arXiv:1704.04504 Website: https://dsixtools.github.io/

The SMEFT

$$\mathcal{L} = \mathcal{L}_{SM}^{(4)} + \frac{1}{\Lambda} \sum_{k} C_{k}^{(5)} Q_{k}^{(5)} + \frac{1}{\Lambda^{2}} \sum_{k} C_{k}^{(6)} Q_{k}^{(6)} + \mathcal{O}\left(\frac{1}{\Lambda^{3}}\right)$$

Gauge invariant operators

Focus on dimension-6 operators

Warsaw basis

[Grzadkowski et al, 2010]

2499 real parameters (3045 with B-violation)

Full 1-loop RGEs computed

[Alonso, Chang, Jenkins, Manohar, Shotwell, Trott, 2013-2014]

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Non-trivial coupled system



Computers are known to be good at complex games...

DsixTools

Mathematica package

Modular structure

Each module can be used independently



Stuff DsixTools can do for you

- Complete 1-loop SMEFT RGE running
- Easy analytical treatment
- Direct input on the notebook
- Easy loops with varying WCs and/or energy scales
- Input and Output with SLHA inspired text files
- Transformation to fermion mass basis at the EW scale
- EW matching to many WET operators for B-physics
- QED and QCD running from the EW scale down to the b-quark mass scale

And much more to come!

Other popular tools

FeynRules

A. Alloul, N. D. Christensen, C. Degrande, C. Duhr, B. Fuks

Website: http://feynrules.irmp.ucl.ac.be/

<u>Mathematica</u> package that allows to derive Feynman rules from a Lagrangian

- Similar in purpose to <u>SARAH</u>
- Input required from the user: particle content and Lagrangian
- Many models already implemented
- Interface to other popular codes (matrix element generators)



R. Mertig, F. Orellana, V. Shtabovenko

Website: https://feyncalc.github.io/

<u>Mathematica</u> package for symbolic evaluation of Feynman diagrams and algebraic calculations

- "Abandoned" for many years but recently revived
- Lorentz index contraction, color factor calculation, Dirac matrix manipulation and traces, SU(N) algebra...
- Many tools to deal with loop integrals: PV reduction, tables of integrals...
- Generation of Feynman rules

Sym2Int

R. Fonseca

Website: http://renatofonseca.net/sym2int.php

<u>Mathematica</u> package that lists all valid interactions given the model symmetries and fields

- Uses the theory group of Susyno (http://renatofonseca.net/susyno.php)
- A large variety of symmetry groups and representations
- Not restricted to dim-4 interaction terms
- Can also be used to calculate gauge and Lorentz contractions



The HEPfit collaboration

Website: http://hepfit.roma1.infn.it/index.html

Code for the Combination of Indirect and Direct Constraints on HEP Models

- Global fits to Higgs, precision and flavor observables
- Bayesian statistics
- Predictions to new observables based on fit results
- New BSM models can be added

Concluding remarks

Concluding remarks

Many "routine tasks" can nowadays be performed with the help of (easy to use) computer tools

Keep in mind:

- Do not be afraid to use them
- Always understand what you are doing



Backup slides

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FlavorKit



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New observables

Implementing a new observable

Two files: steering file "observable.m" + Fortran code "observable.f90"

```
NameProcess = "LLpGamma";
NameObservables = {{muEgamma, 701, "BR(mu->e gamma)"},
{tauEgamma, 702, "BR(tau->e gamma)"},
{tauMuGamma, 703, "BR(tau->mu gamma)"}};
NeededOperators = {K2L, K2R}; Steering file
Body = "LLpGamma.f90"; LLpGamma.m
```

Reminder:

$$\mathcal{L}_{\mu e\gamma} = ie \, m_\mu \, \bar{e} \, \sigma^{\mu\nu} q_\nu \left(\frac{K_2^L P_L + K_2^R P_R}{\mu P_L} \right) \mu A_\mu + \text{h.c.}$$

New observables

```
Real(dp) :: width
Integer :: i1, gt1, gt2
                                                            Fortran code
                                                          LLpGamma.f90
Do i1=1,3
 If (i1.eq.1) Then ! mu -> e gamma
     gt1 = 2
     gt2 = 1
Elseif (i1.eq.2) Then
End if
width = 0.25_dp^{mf}(gt1)^{*5}(Abs(K2L(gt1,gt2))^{*2} + Abs(K2R(gt1,gt2))^{*2})^{Alpha}
 If (i1.eq.1) Then
     muEgamma = width/(width+GammaMu)
Elseif (i1.eq.2) Then
End if
End do
```

New operators

Implementing a new operator

One file: PreSARAH input file "operator.m"

Generic expressions for the Wilson coefficients of new operators can be computed with the help of an additional package (PreSARAH):

- User friendly definition of new operators
- Uses FeynArts/FormCalc [by T. Hahn] to obtain the generic expressions
- Writes all necessary files for SARAH

Example:

$$\mathcal{L}_{2d2\ell} = \sum_{\substack{I=S,V,T\\X,Y=L,R}} E_{XY}^{I} \, \bar{d}_{\beta} \Gamma_{I} P_{X} d_{\alpha} \, \bar{\ell}_{\gamma} \, \Gamma_{I} P_{Y} \ell_{\gamma} + \text{h.c.}$$
($\Gamma_{S,V,T} = 1, \gamma_{\mu}, \sigma_{\mu\nu}$)

New operators

```
NameProcess="2d2L";
                                                        PreSARAH input file
ConsideredProcess = "4Fermion";
                                                                2d2L.m
FermionOrderExternal={2,1,4,3};
NeglectMasses={1,2,3,4};
ExternalFields= {DownQuark,bar[DownQuark],ChargedLepton,bar[ChargedLepton]};
CombinationGenerations = \{\{3,1,1,1\}, \{3,1,2,2\}, \{3,1,3,3\}, \{3,2,1,1\}, \{3,2,2,2\}, \{3,2,3,3\}\};
                                                                         Note:
AllOperators={{OddllSLL,Op[7].Op[7]},
               {OddllSRL,Op[6].Op[7]},
                                                                Op[7], Op[6] = P_{L,R}
                                                                      \operatorname{Lor}[1] = \gamma_{\mu}
               {OddllVRR,Op[7,Lor[1]].Op[7,Lor[1]]},
               {OddIITLL,Op[-7,Lor[1],Lor[2]].Op[-7,Lor[1],Lor[2]]},
               ...};
```

Other flavor codes

- MicrOmegas
- NMSSM-Tools
- SPheno
- SuperIso
- SuSeFLAV
- SUSY_FLAVOR

- [Belanger, Boudjema, Pukhov, Semenov]
- [Ellwanger, Hugonie]
 - [Porod, Staub]
 - [Mahmoudi]
- [Chowdhury, Garani, Vempati]
 - [Rosiek, Chankowski, Dedes, Jäger, Tanedo] [Crivellin, Rosiek]

Restrictions: Only specific models + hard to extend

FlavorKit limitations



FlavorKit is a tool intended to be as general as possible. For this reason, there are some limitations compared to codes which perform specific calculations in a specific model:

- Chiral resummation is not included because of its large model dependence
- Higher order corrections cannot be computed (although they can be included in a parametric way)

A simple program: numerics

A DsixTools Program

This notebook loads DsixTools and shows how to use the SMEFTrunner module.

SetDirectory[NotebookDirectory[]];

Start DsixTools

Needs["DsixTools`"]

Read input files

ReadInputFiles["Options.dat", "WCsInput.dat", "SMInput.dat"];

Load SMEFTrunner module

LoadModule["SMEFTrunner"]

Use SMEFTrunner module

LoadBetaFunctions;

RunRGEsSMEFT;

SMEFT WCs input file

Block WC4		
6 1.0	# phiBtilde	
Block IMWCDPHI		
110.1	# dphi(1,1)	
120.2	# dphi(1,2)	
130.3	# dphi(1,3)	
210.1	# dphi(2,1)	
220.2	# dphi(2,2)	
230.3	# dphi(2,3)	
310.4	# dphi(3,1)	
320.5	# dphi(3,2)	
330.6	# dphi(3,3)	
Block WCDD		
23231.0	# dd(2,3,2,3)	
Block WCPHIQ3		
131.0	# phiq3(1,3)	

WCsInput.dat

Simple text file

Inspired by the SLHA

Similar format for the output file

Also possible to give input directly on the notebook

A simple program: numerics

Results after SMEFTrunner

In[7]:= (* The results can also be plotted as a function of the energy scale *)

In[8]:= (* Gauge couplings *)

- plotGauge1 = Plot[outSMEFTrunner[[1]], {t, tLOW, tHIGH}, Frame → True, Axes → False, PlotRange → {{tLOW, tHIGH}, Automatic}, FrameLabel → {"Log[A/GeV]", "g", None, None}];
- plotGauge2 = Plot[outSMEFTrunner[[2]], {t, tLOW, tHIGH}, Frame → True, Axes → False, PlotRange → {{tLOW, tHIGH}, Automatic}, FrameLabel → {"Log[A/GeV]", "g'", None, None}];
- $plotGauge3 = Plot[outSMEFTrunner[[3]], \{t, tLOW, tHIGH\}, Frame \rightarrow True, Axes \rightarrow False, PlotRange \rightarrow \{\{tLOW, tHIGH\}, Automatic\}, FrameLabel \rightarrow \{"Log[A/GeV]", "g_s", None, None\}];$

plotGauge = {plotGauge1, plotGauge2, plotGauge3}



In[12]:= (* Wilson coefficients *)

- $plotWC1 = Plot[outSMEFTrunner[[48]], \{t, tLOW, tHIGH\}, Frame \rightarrow True, Axes \rightarrow False, PlotRange \rightarrow \{\{tLOW, tHIGH\}, Automatic\}, FrameLabel \rightarrow \{"Log[A/GeV]", "C_{Btilde}", None, None\}];$
- $plotWC2 = Plot[Abs[outSMEFTrunner[[61]]], \{t, tLOW, tHIGH\}, Frame \rightarrow True, Axes \rightarrow False, PlotRange \rightarrow \{\{tLOW, tHIGH\}, Automatic\}, FrameLabel \rightarrow \{"Log[\Lambda/GeV]", "|(C_{d\phi})_{12}|", None, None\}];$
- $plotWC3 = Plot[outSMEFTrunner[[443]], \{t, tLOW, tHIGH\}, Frame \rightarrow True, Axes \rightarrow False, PlotRange \rightarrow \{\{tLOW, tHIGH\}, Automatic\}, and a state of the sta$
 - FrameLabel \rightarrow {"Log[Λ/GeV]", "(C_{dd})₂₃₂₃", None, None}];

plotWC = {plotWC1, plotWC2, plotWC3}



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Another simple program: analytics

A DsixTools Program

This notebook shows how to use the SMEFTrunner module to study SMEFT β functions analytically.

SetDirectory[NotebookDirectory[]];

Start DsixTools

Needs["DsixTools`"]

Set CP conservation

CPV = 0;

Load SMEFTrunner module

LoadModule["SMEFTrunner"]

Compute β functions

GetBeta;

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Another simple program: analytics

Results

 $\ln[6]:=$ (* Let us compute β_{1q} ⁽¹⁾ and β_{1q} ⁽³⁾ assuming top dominance and no NP effects in the 1st fermion family *) In[7]:= (* Top dominance approximation *) $top = \{GD[i, j] \Rightarrow 0, GE[i, j] \Rightarrow 0, GU[i, j] \Rightarrow If[i = j = 3, Vtbyt, If[i = 2\&\& j = 3, Vtsyt, 0]]\};$ In[8]:= (* No NP in 1st family *) WCs2F = { ϕ L1, ϕ L3, ϕ Q1, ϕ Q3}; WCs4F = {LQ1, LQ3, LU, QE, QU1, QU8, QD1, QD8, QQ1, QQ3}; $nofirst2F = Table[Part[WCs2F, i][a, b] \rightarrow If[AnyTrue[{a, b}, # == 1 \&], 0, 1] Part[WCs2F, i][a, b], {i, 1, Length[WCs2F]}];$ $nofirst4F = Table[Part[WCs4F, i][a_, b_, c_, d_] \rightarrow If[AnyTrue[\{a, b, c, d\}, \# = 1\&], 0, 1] Part[WCs4F, i][a, b, c, d], for a large start of the st$ {i, 1, Length[WCs4F]}]; nofirst = Join[nofirst2F, nofirst4F]; $\ln[13] = \beta [lq1] [[2, 2, 2, 3]] /. top /. nofirst // Expand$ Out[13]= $\frac{1}{2}$ Vtb Vts yt² LQ1[2, 2, 2, 2] - $\frac{1}{3}$ gp² LQ1[2, 2, 2, 3] + $\frac{1}{2}$ Vtb² yt² LQ1[2, 2, 2, 3] + $\frac{1}{2} \text{Vts}^2 \text{yt}^2 \text{LQ1}[2, 2, 2, 3] + \frac{1}{2} \text{Vtb} \text{Vts} \text{yt}^2 \text{LQ1}[2, 2, 3, 3] + \frac{2}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{LQ1}[2, 2, 2, 3] + \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 2, 3] + 9 \text{g}^2 \text{LQ3}[2, 2, 2, 3] - \frac{1}{3} \text{gp}^2 \text{LQ1}[3, 3, 3] + \frac{1}{3} \text{gp}^2 \text{LQ3}[3, 3] + \frac{1}{3} \text{gp}^2 \text{LQ3}[3] + \frac{1}{3} \text{gp}$ Vtb Vts yt² LU [2, 2, 3, 3] + $\frac{2}{3}$ gp² QD1 [2, 3, 2, 2] + $\frac{2}{3}$ gp² QD1 [2, 3, 3, 3] + $\frac{2}{3}$ gp² QE[2, 3, 2, 2] + $\frac{2}{3} gp^2 QE[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ1[2, 2, 2, 3] - \frac{4}{3} gp^2 QQ1[2, 3, 2, 2] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{3} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 2, 2, 3] - \frac{14}{9} gp^2 QQ1[2, 3, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 3, 3] - \frac{2}{9} gp^2 QQ3[2, 3] - \frac{2}{9}$ $\frac{2}{2} gp^2 QQ3[2, 3, 3, 3] - \frac{4}{2} gp^2 QU1[2, 3, 2, 2] - \frac{4}{2} gp^2 QU1[2, 3, 3, 3] + Vtb Vts yt^2 \varphi L1[2, 2] - \frac{1}{2} gp^2 \varphi Q1[2, 3]$ $\ln[14] = \beta \log 3 = \beta \log 3 [2, 2, 2, 3] /. \text{ top /. nofirst // Expand}$ Out[14]= 3 g² LQ1[2, 2, 2, 3] + $\frac{1}{2}$ Vtb Vts yt² LQ3[2, 2, 2, 2] - $\frac{16}{3}$ g² LQ3[2, 2, 2, 3] - gp² LQ3[2, 2, 2, 3] + $\frac{1}{2}$ Vtb² yt² LQ3[2, 2, 2, 3] + $\frac{1}{2} \text{Vts}^2 \text{yt}^2 \text{LQ3}[2, 2, 2, 3] + \frac{1}{2} \text{Vtb} \text{Vts} \text{yt}^2 \text{LQ3}[2, 2, 3, 3] + \frac{2}{3} \text{g}^2 \text{LQ3}[3, 3, 2, 3] + \frac{2}{3} \text{g}^2 \text{QQ1}[2, 2, 2, 3] + \frac{2}{3} \text{g}^2 \text{QQ1}[2, 3, 3, 3] - \frac{2}{3} \text{g}^2 \text{QQ1}[2, 2, 2, 3] + \frac{2}{3} \text{g}^2 \text{QQ1}[2, 3, 3, 3] - \frac{2}{3} \text{g}^2 \text{QQ1}[2, 2, 2, 3] + \frac{2}{3} \text{g}^2 \text{QQ1}[2, 3, 3, 3] - \frac{2}{3} \text{g}^2 \text{QQ1}[2, 2, 2, 3] + \frac{2}{3} \text{g}^2 \text{QQ1}[2, 3, 3, 3] - \frac{2}{3} \text{g}^2 \text{QQ1}[2, 3, 3] + \frac{2}{3} \text{g}^2 \text{QQ1}[2, 3] + \frac{2}{3} \text{Q1}[2, 3] + \frac{2$ $\frac{2}{2} g^{2} QQ3[2, 2, 2, 3] + 4 g^{2} QQ3[2, 3, 2, 2] + \frac{10}{3} g^{2} QQ3[2, 3, 3, 3] - Vtb Vts yt^{2} \varphi L3[2, 2] + \frac{1}{3} g^{2} \varphi Q3[2, 3]$