

Connecting Radiative Neutrino Mass, Neutron-Antineutron Oscillation, Proton Decay, and Leptogenesis through Dark Matter

What a title!!!

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Abstract

The scotogenic mechanism for radiative neutrino mass is generalized to include neutron-antineutron oscillation as well as proton decay. Dark matter is stabilized by extending the notion of lepton parity to matter parity. Leptogenesis is also a possible byproduct. This framework unifies the description of all these important, but seemingly unrelated, topics in physics beyond the standard model of particle interactions.

Introduction :

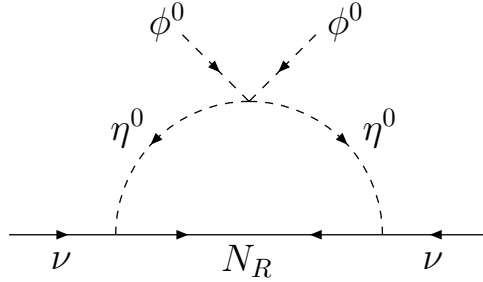
The standard model (SM) of quarks and leptons is based on the well-tested $SU(3)_C \times SU(2)_L \times U(1)_Y$ gauge symmetry. It admits two well-known accidental symmetries, baryon number B and lepton number L , which are known to be conserved as far as present experimental limits are concerned. Of course, if neutrino masses are confirmed as Majorana from neutrinoless double beta decay in the near future, then L should be downgraded to just $(-1)^L$, i.e. lepton parity P_L . This is actually an important concept, because dark matter may be stabilized by the proper extension of P_L to physics beyond the SM [1]. It would also tell us that P_L may be the true symmetry of a complete theory, whereas the conservation of L only holds in the absence of neutrino masses.

Let us now consider B . Is there a possible clue that it is not the true symmetry of a complete theory? The analog to Majorana neutrino mass is then neutron-antineutron ($n - \bar{n}$) oscillation. If proven to exist, B would be downgraded to $(-1)^{3B}$, i.e. baryon parity P_B . What about proton decay? If it exists, then the final product must contain a lepton, e.g. $p \rightarrow \pi^0 e^+$ or $p \rightarrow \pi^+ \nu(\bar{\nu})$. This would violate both lepton parity and baryon parity. It may however be accommodated by combining lepton parity with baryon parity to form matter parity, i.e. $P_M = (-1)^{3B+L}$.

In this paper, we assume that the true symmetry of a complete theory beyond the SM is P_M . However, P_L and P_B are respected by all dimension-four and dimension-three terms of the Lagrangian, broken only to P_M by a unique dimension-two term. With the present available experimental accuracy, the separate conservation of B and L holds. To confirm our hypothesis, it would take future extraordinary discoveries, i.e. neutrinoless double beta decay (for P_L), neutron-antineutron oscillation (for P_B), and proton decay (for P_M). Nevertheless, there is already a theoretical framework for connecting all of these phenomena. It is the scotogenic mechanism (from the Greek *scotos* meaning darkness), invented 10 years ago [2].

Scotogenic neutrino mass :

The scotogenic mechanism was applied to obtaining one-loop Majorana neutrino masses as shown in Fig. 1. The scalar doublet (η^+, η^0) is odd under P_L to distinguish it from the SM



Scotogenic neutrino masses

Figure 1: One-loop Z_2 scotogenic neutrino mass.

Higgs doublet (ϕ^+, ϕ^0) which is even. The three neutrinos ν_L are odd under P_L , and the three singlet neutral fermions N_R are even. The latter have allowed Majorana masses m_N , forming thus three Majorana fermions $N = N_R + N_R^c$. Note that N_R are not the right-handed neutrinos which would be odd under P_L . **This assignment is equivalent [1] to having odd dark parity for η and N_R , and even dark parity for ν_L and ϕ , using the conserved product $P_L(-1)^{2j}$, where j is the spin angular momentum of the particle.**

Scotogenic neutron-antineutron oscillation :

The scotogenic analog for $n - \bar{n}$ oscillation is actually very simple. Add to the SM two color scalar triplets, one with even P_B and the other with odd P_B as follows:

$$\delta \sim (3, 1, -1/3; +), \quad \xi \sim (3, 1, -1/3; -). \quad (1)$$

The resulting allowed interactions are $d_R N_R \xi^*$, $(\delta^* \xi)^2$, and $u_{L,R} d_{L,R} \delta$. Hence δ is a scalar diquark, and $n - \bar{n}$ oscillation is generated as shown in Fig. 2. Note that N_R is again used because it has even P_B as well as P_L , and the scalar ξ inside the loop has odd dark parity. The new particles of this model are listed in Table 1, together with two other real scalar singlets $\chi_{1,2}$ to be discussed later. **The dark parity P_D is simply defined as $P_M(-1)^{2j}$.**

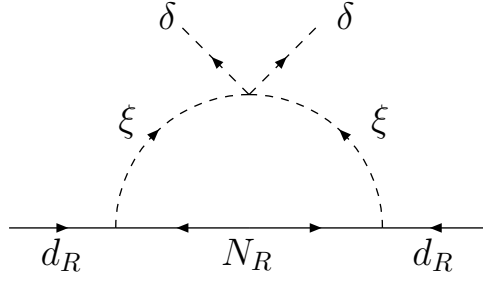


Figure 2: One-loop Z_2 scotogenic $n - \bar{n}$ oscillation.

Scotogenic proton decay :

Let us now bisect Figs. 1 and 2 and try to join the two different halves. The quartic couplings $(\delta^*\xi)(\bar{\phi}^0\eta^0)$ and $(\delta^*\xi)(\phi^0\bar{\eta}^0)$ are forbidden by P_L and by P_B . However they may be induced by the trilinear couplings $\delta^*\xi\chi_1$, $\bar{\phi}^0\eta^0\chi_2$, and $\phi^0\bar{\eta}^0\chi_2$, which respect both P_L and P_B . The

Table 1: Particle content of proposed model.

Particle	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	P_L	P_B	P_M	P_D
$(u, d)_L$	3	2	1/6	+	-	-	+
u_R	3	1	2/3	+	-	-	+
d_R	3	1	-1/3	+	-	-	+
$(\nu, l)_L$	1	2	-1/2	-	+	-	+
l_R	1	1	-1	-	+	-	+
N_R	1	1	0	+	+	+	-
(ϕ^+, ϕ^0)	1	2	1/2	+	+	+	+
(η^+, η^0)	1	2	1/2	-	+	-	-
δ	3	1	-1/3	+	+	+	+
ξ	3	1	-1/3	+	-	-	-
χ_1	1	1	0	+	-	-	-
χ_2	1	1	0	-	+	-	-

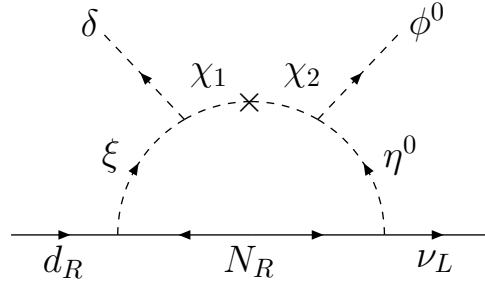
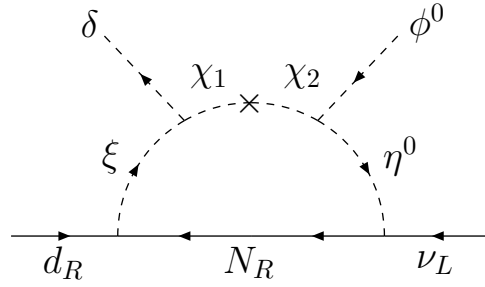
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dimension-two mass-squared term $m_{12}^2\chi_1\chi_2$ is then inserted to break P_L and P_B softly to $P_M = P_LP_B$. The resulting diagrams are shown in Figs. 3 and 4. Both processes conserve


 Figure 3: One-loop Z_2 scotogenic $n \rightarrow \nu$ transition.

 Figure 4: One-loop Z_2 scotogenic $n \rightarrow \bar{\nu}$ transition.

P_M , whereas $n \rightarrow \nu$ conserves $B + L$ in Fig. 3, and $n \rightarrow \bar{\nu}$ conserves $B - L$ in Fig. 4. It will be shown later that the integral associated with Fig. 4 is negligible compared to that of Fig. 3. Hence proton decay proceeds mainly via $p \rightarrow \pi^+ \nu$, thereby conserving $B + L$ [3, 4], instead of the usual $B - L$. However, since ν cannot be distinguished from $\bar{\nu}$ in practice, this prediction cannot be tested. In this scenario, we assume ξ to be heavier than N , so ξ decays to $N + d$. We also assume that the lightest N is heavier than η , so that its decay to $\eta^+ l^-$ and $\eta^- l^+$ may generate a lepton asymmetry [5], which gets converted to a baryon asymmetry through the sphalerons [6] before the electroweak phase transition is over. The dark-matter candidate is thus either the real or imaginary component of η^0 [7]. For some recent studies on this possibility, see for example Refs. [8, 9, 10].

Evolution of B and L symmetries :

In our scenario the heaviest particle is ξ . For convenience we also assume $\chi_{1,2}$ to be at this

mass scale. They may however be much lighter and not affect our following discussion. As the Universe cools below m_ξ , the effective theory (minus ξ and possibly $\chi_{1,2}$) gains the symmetry B in all its dimension-four terms, whereas the dimension-five term $(\delta^* d_R)^2$ breaks B to P_B . The $(\delta^* d_R)(\phi^0 \nu - \phi^+ l^-)$ and $(\delta^* d_R)(\bar{\phi}^0 \bar{\nu} - \phi^- l^+)$ terms break P_L and P_B to P_M . The next heaviest particles are $N_{1,2,3}$. As the Universe further cools below their masses, the effective theory gains also the symmetry L in all its dimension-four terms, whereas the dimension-five term $(\phi^0 \nu - \phi^+ l^-)^2$ breaks L to P_L . Meanwhile, the decay $N \rightarrow l^\pm \eta^\mp$ has created a lepton asymmetry and is being converted by sphalerons to the observed baryon asymmetry of the Universe. Finally at the electroweak scale, the particle content of our proposal is that of the SM plus the dark scalar doublet (η^+, η^0) , and perhaps also the scalar diquark δ . If m_δ is much heavier, then the $n - \bar{n}$ oscillation effective operators $(u_R d_R) d_R d_R (u_R d_R)$, $(u_L d_L) d_R d_R (u_L d_L)$, $(u_R d_R) d_R d_R (u_L d_L)$ are dimension-nine, and the proton decay effective operators $(u_R d_R) d_R (\bar{\phi}^0 \bar{\nu} - \phi^- l^+)$, $(u_L d_L) d_R (\bar{\phi}^0 \bar{\nu} - \phi^- l^+)$ are dimension-seven [11, 12, 13]. Note that $n \rightarrow \pi^+ e^-$ is possible, but it requires the conversion of ϕ^+ to π^+ , so it is very much suppressed compared to $n \rightarrow \pi^0 \nu$ and $p \rightarrow \pi^+ \nu$.

Evaluations of the loop integrals :

The evaluation of the integral involved in the one-loop diagram of Fig. 1 is well-known. The $(\lambda_5/2)(\Phi^\dagger \eta)^2 + H.c.$ interaction splits the complex scalar $\eta^0 = (\eta_R + i\eta_I)/\sqrt{2}$ into two mass eigenstates with different eigenvalues $m_{R,I}$, i.e.

$$m_R^2 - m_I^2 = 2\lambda_5 v^2, \quad (2)$$

with $v = \langle \phi^0 \rangle = 174$ GeV. For a given N with mass m_N , their contribution is given by

$$I_1(m_N, m_R, m_I) = \frac{m_N}{16\pi^2} \left[\frac{m_R^2 \ln(m_N^2/m_R^2)}{m_N^2 - m_R^2} - \frac{m_I^2 \ln(m_N^2/m_I^2)}{m_N^2 - m_I^2} \right]. \quad (3)$$

The analog integral for Fig. 2 is

$$I_2(m_N, m_\xi) = \frac{m_N}{16\pi^2} \left[\frac{1}{m_\xi^2 - m_N^2} - \frac{m_N^2 \ln(m_\xi^2/m_N^2)}{(m_\xi^2 - m_N^2)^2} \right]. \quad (4)$$

For Fig. 3, we assume

$$m_{12}^2, m_{R,I}^2 \ll m_N^2 \ll m_\xi^2 \simeq m_{1,2}^2, \quad (5)$$

then the integral is proportional to $\mu_1\mu_2m_Nm_{12}^2$, where $\mu_{1,2}$ are the trilinear couplings of $\chi_1\delta^*\xi$ and $\chi_2\bar{\phi}^0\eta^0$, and the contribution of $m_{R,I}^2$ is negligible. We obtain

$$\begin{aligned} I_3(m_N, m_\xi) &= \frac{\mu_1\mu_2m_Nm_{12}^2}{16\pi^2} \left[\frac{-2m_\xi^2 + m_N^2}{2m_\xi^4(m_\xi^2 - m_N^2)^2} + \frac{\ln(m_\xi^2/m_N^2)}{(m_\xi^2 - m_N^2)^3} \right] \\ &\simeq \frac{\mu_1\mu_2m_Nm_{12}^2[-1 + \ln(m_\xi^2/m_N^2)]}{16\pi^2m_\xi^6}. \end{aligned} \quad (6)$$

Using the same assumption of Eq. (5), we obtain also

$$I_1 \simeq \frac{1}{16\pi^2} \left[\frac{m_R^2}{m_N} \ln\left(\frac{m_N^2}{m_R^2}\right) - \frac{m_I^2}{m_N} \ln\left(\frac{m_N^2}{m_I^2}\right) \right], \quad I_2 \simeq \frac{m_N}{16\pi^2m_\xi^2}. \quad (7)$$

The integral I_4 for Fig. 4 is helicity suppressed, so that m_N has to be replaced by m_d , hence it is negligible compared to I_3 and will not be considered further. There are also contributions to $I_{1,2}$ from $\chi_{2,1}$, but they are suppressed by $\mu_{2,1}^2/m_{2,1}^2$.

Phenomenological details :

The 3×3 neutrino mass matrix is given by

$$(\mathcal{M}_\nu)_{ij} = \sum_k h_{ik}h_{jk}I_1(m_{N_k}, m_R, m_I), \quad (8)$$

where h are the Yukawa $\bar{N}_R\nu\eta^0$ couplings. The applicability of this formula has been studied extensively. For example, if $h \sim 10^{-3}$, $m_{R,I} \sim 100$ GeV, and $m_N \sim 10^6$ GeV, then neutrino masses are of order 0.1 eV.

The above mechanism has also the built-in possibility [14] of leptogenesis [5] from the decay of $N \rightarrow l^\pm\eta^\mp$. In particular, the required CP asymmetry can obtain a resonantly enhanced contribution from self-energy corrections [15] since the decaying singlet fermions may have a quasi-degenerate mass spectrum, i.e.

$$\varepsilon_{N_i} = \frac{1}{8\pi} \sum_{j \neq i} \frac{\text{Im}\{[(h^\dagger h)_{ij}]^2\}}{(h^\dagger h)_{ii}} \frac{m_{N_j}m_{N_i}}{m_{N_j}^2 - m_{N_i}^2}. \quad (9)$$

Consider as usual the quantity

$$K_i = \frac{\Gamma_{N_i}}{2H(T)} \Big|_{T=m_{N_i}} \quad \text{with} \quad \Gamma_{N_i} = \frac{1}{8\pi} (h^\dagger h)_{ii} m_{N_i}, \quad H(T) = \left(\frac{8\pi^3 g_*}{90} \right)^{\frac{1}{2}} \frac{T^2}{M_{Pl}}. \quad (10)$$

As an example, let $h \sim 10^{-3}$ and $m_{N_3} \gg m_{N_{1,2}} \sim 10^6$ GeV. We then obtain the CP asymmetries $\varepsilon_{N_{1,2}} = \mathcal{O}(0.01 - 0.1)$ for $m_{N_2} - m_{N_1} = \mathcal{O}(1 - 10$ GeV). Using $g_* \simeq 100$ and $M_{Pl} \simeq 10^{19}$ GeV, we find $K_{1,2} = \mathcal{O}(10^5)$, hence $z_{1,2} \simeq 4.2(\ln K_{1,2})^{0.6} \simeq \mathcal{O}(18)$ [16]. This means that the lighter singlet fermions $N_{1,2}$ can efficiently decay to generate a lepton asymmetry at a temperature around $T_{1,2} \simeq m_{N_{1,2}}/z_{1,2} = \mathcal{O}(10^5$ GeV) where the sphaleron processes are still active. The final baryon asymmetry, which is conveniently described by the ratio of the baryon number density n_B over the entropy density s , is then $n_B/s \simeq \varepsilon_{N_1}/(g_* K_1 z_1) + \varepsilon_{N_2}/(g_* K_2 z_2) = \mathcal{O}(10^{-10})$ as desired [16].

As for the topic of $n - \bar{n}$ oscillation, there has been a recent resurgence of interest [17]. Let the effective Hamiltonian density be given by

$$\mathcal{H}_{eff} = \sum_i c_i \mathcal{O}_i \quad (11)$$

where \mathcal{O}_i are the dimension-nine operators responsible for this transition. Then

$$\langle \bar{n} | \mathcal{H}_{eff} | n \rangle = \sum_i c_i \langle \bar{n} | \mathcal{O}_i | n \rangle \simeq \sum_i c_i \Lambda_{QCD}^6 \simeq \sum_i c_i (180 \text{ MeV})^6. \quad (12)$$

Let the $d_R N_R \xi^*$ coupling be f_ξ , the $u_{L,R} d_{L,R} \delta$ couplings be $f_\delta^{L,R}$, and the $(\delta^* \xi)^2$ coupling be $\lambda/2$, then

$$\sum_i c_i = \frac{(f_\delta^L + f_\delta^R)^2 \lambda f_\xi^2 m_N}{16\pi^2 m_\xi^2 m_\delta^4}. \quad (13)$$

For $\tau_{n-\bar{n}} = 2 \times 10^8$ s, this translates to [17]

$$\sum_i c_i = 10^{-28} \text{ GeV}^{-5}. \quad (14)$$

Inside a nucleus, the $n - \bar{n}$ transition is exponentially suppressed. Hence the present experimental limit [18] $\tau_{n-\bar{n}} > 0.86 \times 10^8$ s yields a deuteron stability lifetime $> 10^{31}$ y. To

match Eq. (13) with Eq. (14), we may for example take again $m_N \sim 10^6$ GeV, then choose $m_\xi \sim 10^7$ GeV, $m_\delta \sim 10^4$ GeV, and $f_\delta^{L,R} \sim \sqrt{\lambda} \sim f_\xi \sim 0.4$.

For proton decay, the dominant decay $p \rightarrow \pi^+ \nu$ has an effective coupling given by

$$\begin{aligned} G_{eff} &= \frac{\sqrt{(f_\delta^L)^2 + (f_\delta^R)^2} f_\xi h v I_3 \Lambda_{QCD}^3}{f_\pi m_\delta^2} \\ &= \left(\frac{\sqrt{(f_\delta^L)^2 + (f_\delta^R)^2} f_\xi h v \Lambda_{QCD}^3}{f_\pi m_\delta^2} \right) \frac{\mu_1 \mu_2 m_N m_{12}^2 [-1 + \ln(m_\xi^2/m_N^2)]}{16\pi^2 m_\xi^6}. \end{aligned} \quad (15)$$

Let $m_\xi \sim 10^7$ GeV, $m_N \sim 10^6$ GeV, $m_\delta \sim 10^4$ GeV, $\Lambda_{QCD} = 180$ MeV, $f_\delta^{L,R} \sim f_\xi \sim 0.4$, and $h \sim 10^{-3}$ as before. Using $f_\pi = 130$ MeV, and choosing $\mu_{1,2} \sim 10^5$ GeV, $m_{12}^2 \sim 10^7$ GeV² in addition, then $G_{eff} \sim 4.0 \times 10^{-32}$ which yields a proton decay lifetime $\sim 1.4 \times 10^{33}$ y, using

$$\Gamma_p = \frac{G_{eff}^2 (m_p^2 - m_\pi^2)^2}{32\pi m_p^3}. \quad (16)$$

The numerical values of the various parameters are of course for illustration only. They are chosen to demonstrate that realistic solutions exist for neutrino mass, neutron-antineutron oscillation, and proton decay, all in the scotogenic context. Again our framework assumes the validity of matter parity P_M which translates to dark parity $P_D = P_M(-1)^{2j}$, and is derivable from lepton parity P_L and baryon parity P_B , both of which are respected by all dimension-four and dimension-three terms of our renormalizable Lagrangian. A unique dimension-two term breaks both P_L and P_B , but preserves the product $P_M = P_L P_B$. In the illustrative example shown, the heaviest particles are the scalar ξ and perhaps also the scalars $\chi_{1,2}$ at $\sim 10^7$ GeV. They decay to the singlet fermions N with mass $\sim 10^6$ GeV, which also couple to leptons and are responsible for generating a lepton asymmetry of the Universe. Leaving aside these very heavy particles, our proposal also predicts a scalar diquark δ of mass ~ 10 TeV, as compared with the present experimental lower limit [19] of about 6 TeV. Finally, we also have the dark scalar doublet (η^+, η^0) which should be observable at the electroweak scale.

Concluding remarks :

In this scotogenic worldview, new physics phenomena beyond the standard model are all interconnected through dark matter and dictated by the extension of the discrete symmetries lepton parity P_L and baryon parity P_B , both of which are respected by the dimension-four and dimension-three terms of our complete renormalizable Lagrangian. A unique dimension-two term breaks P_L and P_B , but preserves matter parity $P_M = P_L P_B$. Dark parity is then simply $P_M(-1)^{2j}$.

The new particles of this scenario are three dark singlet neutral Majorana fermions N , a dark scalar doublet (η^+, η^0) , a scalar diquark δ , a dark scalar leptoquark ξ , and two dark real scalar singlets $\chi_{1,2}$. Scotogenic radiative neutrino masses are obtained through N and η^0 as shown in Fig. 1. Leptogenesis is facilitated by the decay $N \rightarrow l^\pm \eta^\mp$. Neutron-antineutron oscillation is obtained through N , ξ , and δ as shown in Fig. 2. Slicing the two diagrams and joining them together with $\chi_{1,2}$, proton decay is obtained as shown in Fig. 3. This new notion of physics beyond the standard model connects all four fundamental processes through dark matter. Possible experimental verification includes the discovery of the dark scalar doublet (η^+, η^0) , the crucial heavy scalar diquark δ if kinematically possible, and the prediction that proton decay should be $p \rightarrow \pi^+ \nu$, and not $p \rightarrow \pi^0 e^+$ or $p \rightarrow \pi^+ \bar{\nu}$.

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