

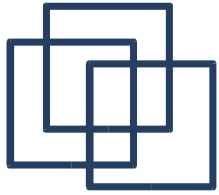
$B^\pm \rightarrow D(*)K^\pm$ Dalitz γ Analysis

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IFIC-Valencia & INFN-Pisa

*for the D0K-dalitz group
BaBar Collaboration Meeting, December 2004*

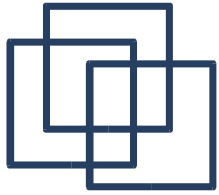
BAD#899 and BAD#1086

PRL draft under way



Outline

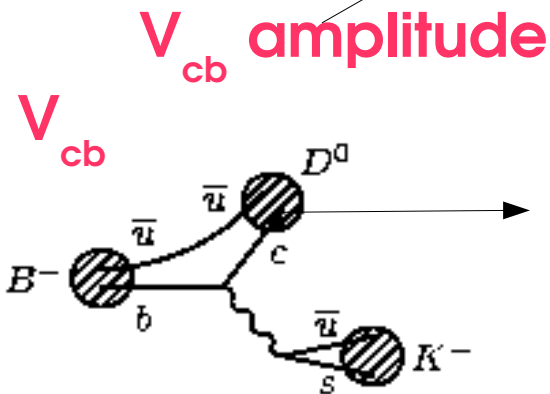
- Method of measurement
- The Dalitz model
- Data sample and event selection
- Background parameterization
- CP fit
- Frequentist interpretation and significance of CP violation
- Summary and plans



Method of measurement

B⁺: $\text{pdf}_+ = | f(s_{12}, s_{13}) + r_b e^{i(\gamma+\delta)} f(s_{13}, s_{12})^2 |$ γ changes sign in the two different B charge samples

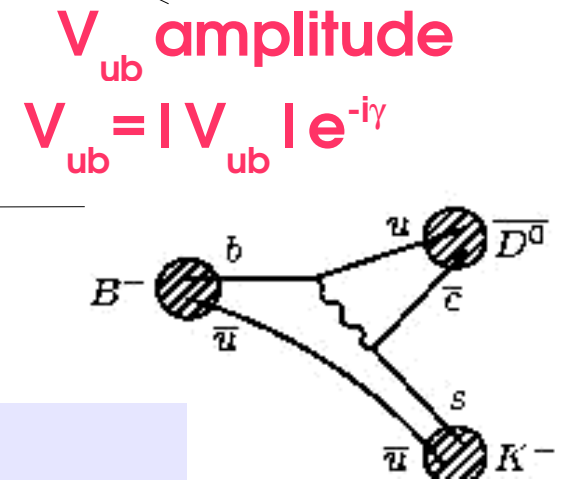
B⁻: $\text{pdf}_- = | f(s_{13}, s_{12}) + r_b e^{i(-\gamma+\delta)} f(s_{12}, s_{13})^2 |$



$$s_{12} = m^2(Ks\pi^-)$$

$$s_{13} = m^2(Ks\pi^+)$$

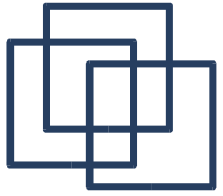
Same final state
 $B^- \rightarrow D(*)K^-, D \rightarrow Ks\pi^+\pi^-$
Interference



The Dalitz model gives $f(s_{12}, s_{13})$

The CP Dalitz analysis extracts $r_B^{(*)}, \gamma, \delta^{(*)}$

Only two-fold ambiguity in γ extraction ($\gamma \rightarrow \gamma + \pi, \delta \rightarrow \delta + \pi$)



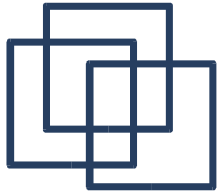
Method of measurement

Advantages:

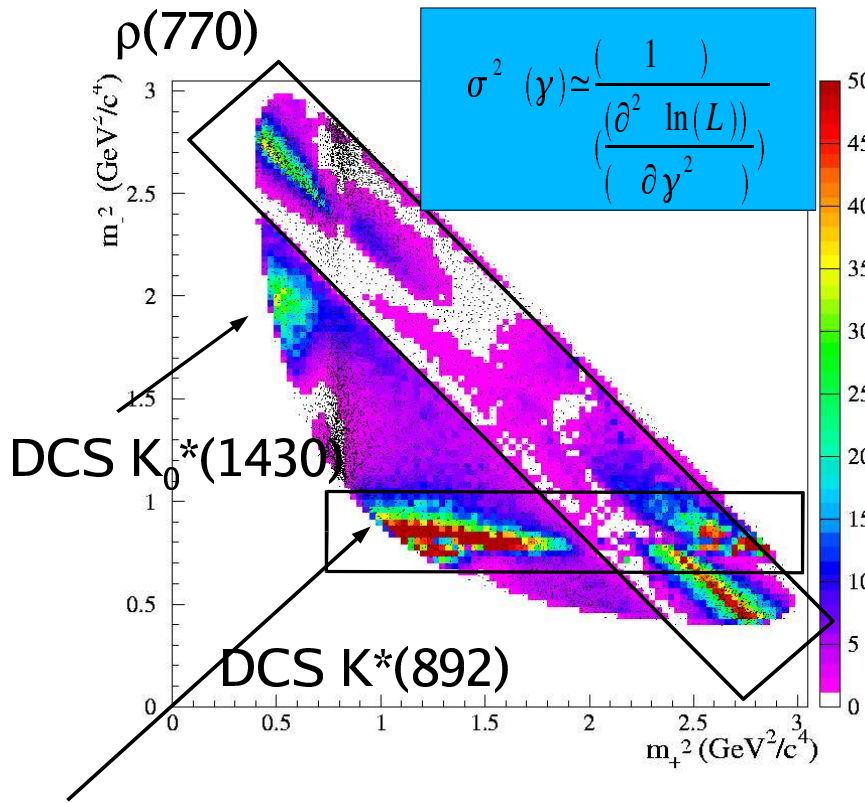
- Interference is proportional to $r_B \sim 0.1$ and to $A(s_{12}, s_{13})A^*(s_{13}, s_{12})$ which is large in several regions of the Dalitz plot, i.e. $K^*(892)$ DCS, $\rho(770)$, $K^{*0}(1430)$ DCS
- Combination of GLW and ADS methods
- Need to reconstruct only one decay channel which has relatively high statistics

Disadvantages:

- Dalitz plot analysis imposes a model dependency which may limit asymptotically the reach of the method
- Model independent approach exists but not convenient with the present statistics **A.Giri et al., Phys. Rev. D68, 054018 (2003)**



Sensitivity to γ



Not all the events in the Dalitz are sensitive to γ .
Need regions where interference term is large

E.g. $K^*(892)$ regions, maximal interference

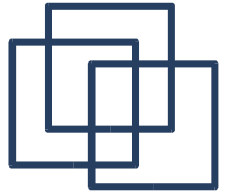
B decay	•	D decay	interfere	B decay	•	D decay
V_{ub}	•	$A_D(CA)$	\Leftrightarrow	V_{cb}	•	$A_D(DCS)$
small	•	large	\Leftrightarrow	large	•	small

$r_B A_D(s_{12}, s_{13})$ = from V_{ub}	$A_D(s_{12}, s_{13})$ CA region	D^0 Decay
$A_D^*(s_{13}, s_{12})$ = from V_{cb}	$A_D^*(s_{13}, s_{12})$ DCS region	D^0 Decay

$$\gamma = 75, \delta = 180, r_B = 0.12$$

$$d\hat{\Gamma}(B^- \rightarrow (K_S \pi^- \pi^+)_D K^-) = \left(A_{12,13}^2 + r_B^2 A_{13,12}^2 + 2r_B \text{Re} \left[A_D(s_{12}, s_{13}) A_D^*(s_{13}, s_{12}) e^{-i(\delta_B - \gamma)} \right] \right) dp$$

Interference term



D* relative effective strong phase

In $B \rightarrow D^* K$ decays:

$$\tilde{D}^* = \frac{D_+^* + D_-^*}{\sqrt{2}} + r_B e^{i(\delta_B - \phi_3)} \frac{D_+^* - D_-^*}{\sqrt{2}}.$$

D_{\pm}^* decaying into CP eigenstates $D^0 \pi^0, D^0 \gamma$

$\eta_{D^*} = \eta_{\pi, \gamma} \eta_D (-1)^{l=1}$ $l=1$ for parity/ang momentum conservation

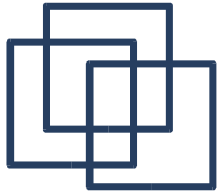
$$\eta_{\gamma} = -1 \cdot \eta_{\pi}$$

$$D_{\pm}^* \rightarrow D^0 \pi^{\pm}, \quad D_{\pm}^* \rightarrow D^0 \gamma^{\mp}$$

Effective strong phase shift of π between $D^0 \pi^0$ and $D^0 \gamma$

Same arguments for ADS analysis.

A. Bondar, T. Gershon, hep-ph/0409281



The Dalitz model

Dalitz model uses 17 components (13 resonances + 1 Non Resonant term)
 Removed DCS $K^*(1680)$, and added $K^*(1410)$, $\rho(1450)$ respect to Belle Model
 All single Breit-Wigners, except for ρ 's (Gounaris-Sakurai)

From $\sim 80K D^* \rightarrow D0\pi$,
 $D0 \rightarrow Ks\pi+\pi-$ events
 provided by
 Antimo Palano

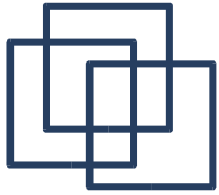
Resonance	Amplitude	phase (degrees)	fit fraction (%)
$K^*(892)$	1.781 ± 0.018	131.0 ± 0.79	58.60
$\rho^0(770)$	1 (fixed)	0(fixed)	22.36
$K^*(892)$ DCS	0.1796 ± 0.0079	-44.1 ± 2.4	0.60
$\omega(782)$	0.0391 ± 0.0016	115.3 ± 2.5	0.56
$f_0(980)$	0.4817 ± 0.011	218.2 ± 2.2	6.09
$f_0(1370)$	2.25 ± 0.28	113.2 ± 4.4	3.20
$f_2(1270)$	0.922 ± 0.040	-21.3 ± 2.8	3.00
$K_0^*(1430)$	2.447 ± 0.073	-8.3 ± 2.0	8.32
$K_0^*(1430)$ DCS	0.368 ± 0.067	-342.2 ± 9.8	0.19
$K_2^*(1430)$	1.054 ± 0.045	-54.3 ± 2.5	2.74
$K_2^*(1430)$ DCS	0.075 ± 0.036	-104 ± 30	0.01
$K^*(1410)$	0.515 ± 0.071	154 ± 10	0.37
$K^*(1680)$	0.89 ± 0.29	-139 ± 19	0.28
$\rho(1450)$	0.515 ± 0.092	38 ± 13	0.24
σ_1	1.358 ± 0.040	-177.9 ± 2.4	9.27
σ_2	0.340 ± 0.024	-207.0 ± 3.8	1.34
Non resonant	3.53 ± 0.44	-232.4 ± 4.7	7.30

Added →

Added →

Nothing changed
 after Summer !

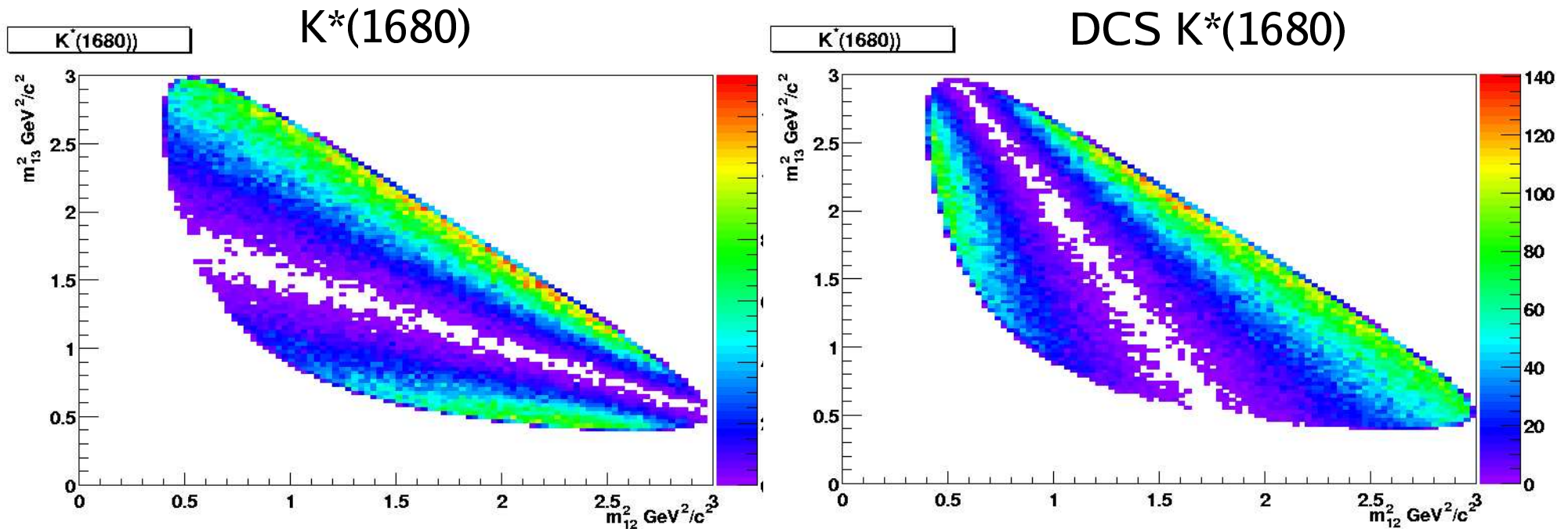
Mass and widths are
 fixed to the
 PDG 2004 values,
 except for σ_1 , σ_2 for
 which we directly fit

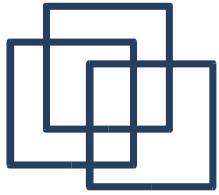


The Dalitz model

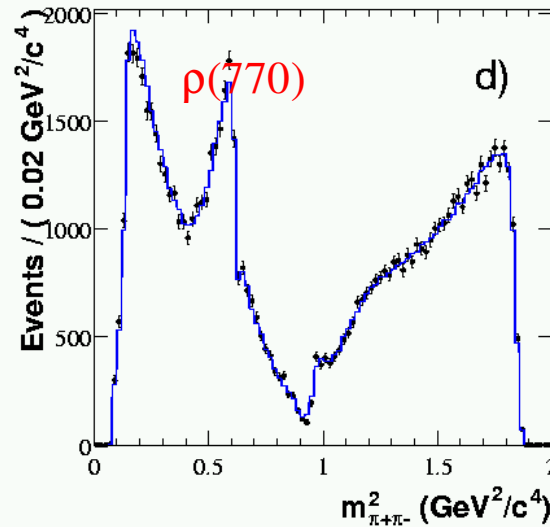
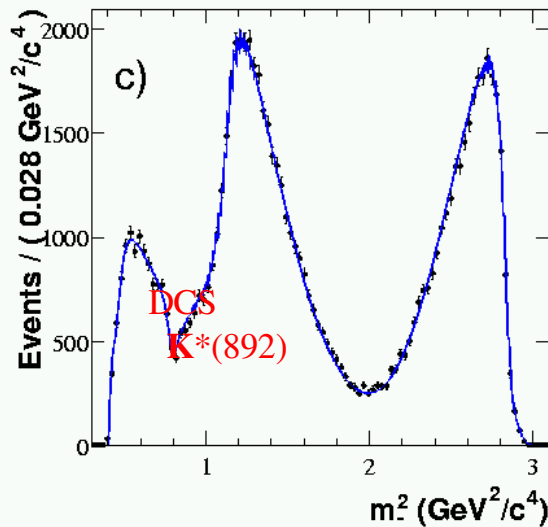
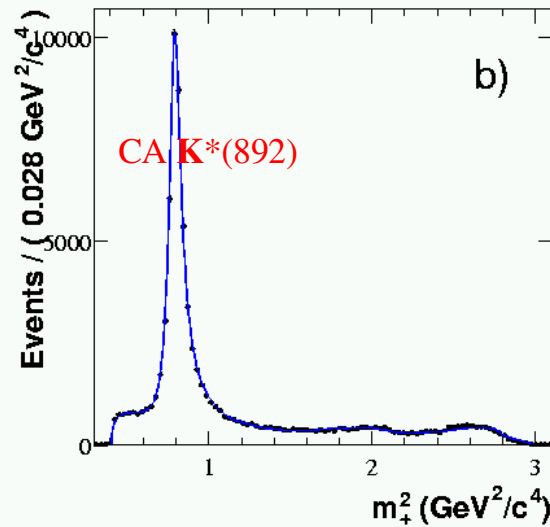
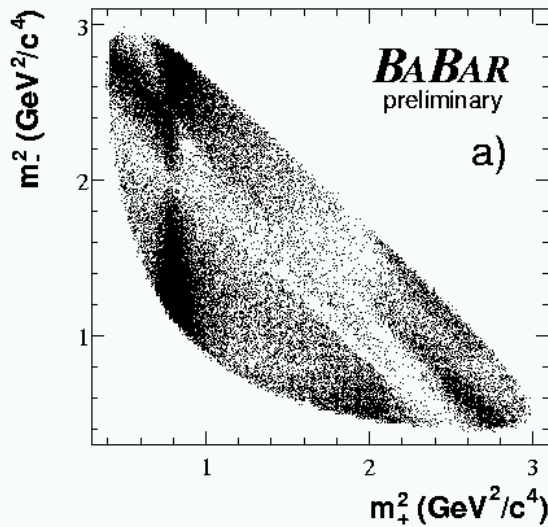
DCS $K^*(1680)$ and DCS $K^*(1410)$ excluded because:

- the number of events expected is very small
- the $K^*(1680)$ and the DCS $K^*(1680)$ overlap in the same Dalitz region: the fit returns \approx the same amplitude for CA and DCS !





The Dalitz model



BaBar Data with Dalitz model fit overlaid

χ^2 fit evaluation of goodness of fit:

BaBar model: 1.27/dof(3054)

CLEO model: 2.2/dof(3054)

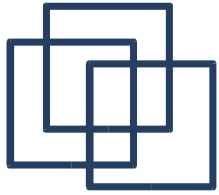
Belle model: 1.88/dof(1130)

Total fit fraction:

BaBar model: 125.0%

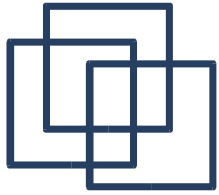
CLEO model: 120%

Belle model: 137%



Data samples

- MC sample :
 - B+ 501 fb-1
 - B0 394 fb-1
 - ccbar 140 fb-1
 - uds 135 fb-1
 - D*0K, D0→Ksππ MC signal 300K events
- DATA sample :
 - **BlackDiamond**
 - DATA ON 215 fb-1
 - DATA OFF 10 fb-1



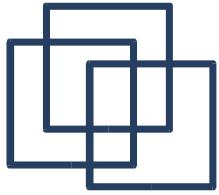
Event selection

	D^0K	$D^{*0}K (D^0\pi^0)$	$D^{*0}K (D^0\gamma)$
$ \cos(\theta_T) $	<0.8	<0.8	<0.8
$ \text{mass}(D^0)\text{-PDG} $	$<12\text{ MeV}$	$<12\text{ MeV}$	$<12\text{ MeV}$
$ \text{mass}(K_S)\text{-PDG} $	$<9\text{ MeV}$	$<9\text{ MeV}$	$<9\text{ MeV}$
Kaon Tight Selector	Yes	Yes	Yes
$ \Delta M\text{-PDG} $	-----	$<2.5\text{ MeV}$	$<10.0\text{ MeV}$
$\cos\alpha_{K_S}$	>0.99	>0.99	>0.99
$ \Delta E $	$<30\text{ MeV}$	$<30\text{ MeV}$	$<30\text{ MeV}$

$|\cos(\alpha_{K_S})|$ suppress fake K_S

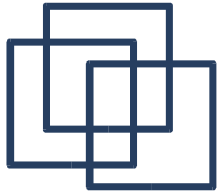
$|\cos(\theta_T)|$ suppress jet-like events

Kaon Tight Selector suppress $D^{(*)}\pi$ events



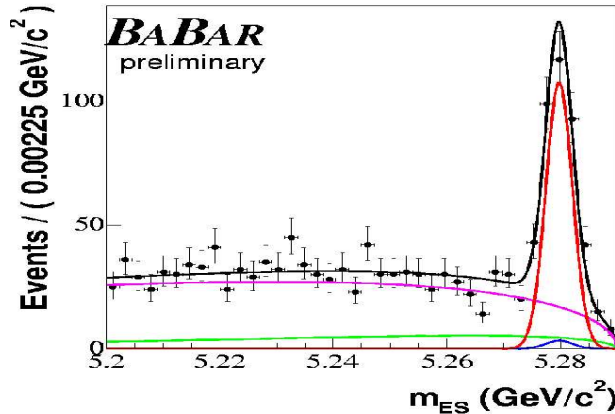
Bkg parametrization

- Continuum events are the largest bkg
 - Fisher PDF for the continuum bkg suppression
$$Fisher = \mathcal{F} [\text{LegendreP0}, \text{LegendreP2}, |\cos(\theta_T)|, \cos(\theta_B^*)]$$
 - allows evaluation of the relative fraction of BB and continuum events from data
- Very small $D\pi$ bkg due to tight ΔE cut
 - Momentum dependent ΔE PDF
- True D^0 fraction evaluated directly on data using the $mES < 5.272$ GeV sidebands and fitting for the D^0 mass (assuming no BB contribution, check on MC)
- Fake D^0 Dalitz shape parameterized as 2D symmetric 2nd order polynomial function and taken from
 - off-resonance data for qqbar combinatorics (continuum)
 - MC for BB



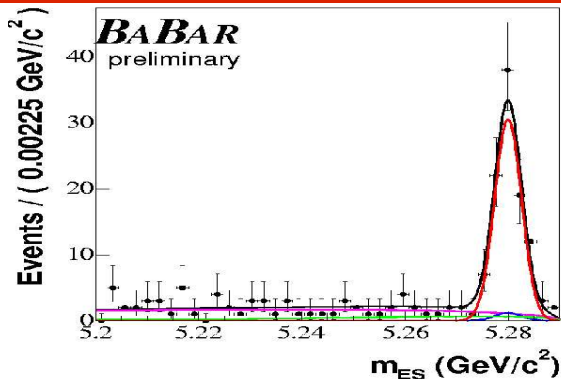
Selection yields: m_{ES}

$B^- \rightarrow DK^- \quad D^0 \rightarrow (K_S \pi \pi)$

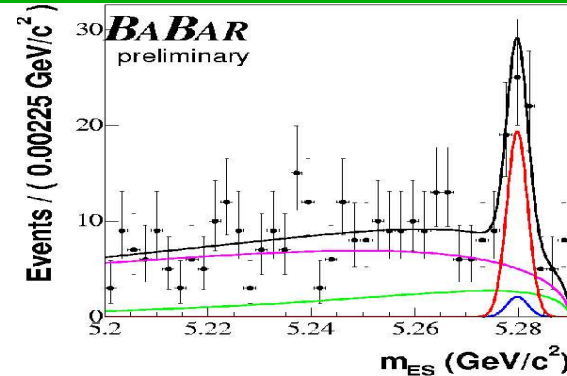


DK	282 ± 20	Sig Evt
D*K (D ⁰ π ⁰)	89 ± 11	Sig Evt
D*K (D ⁰ γ)	44 ± 8	Sig Evt
red	signal	
magenta	qqbar	
green	bbar	
blu	Dπ	

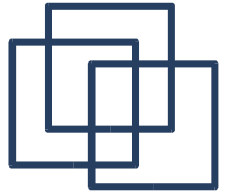
$B^- \rightarrow D^* K^- \quad D^{*0} \rightarrow (D^0 \pi^0)$



$B^- \rightarrow D^* K^- \quad D^{*0} \rightarrow (D^0 \gamma)$



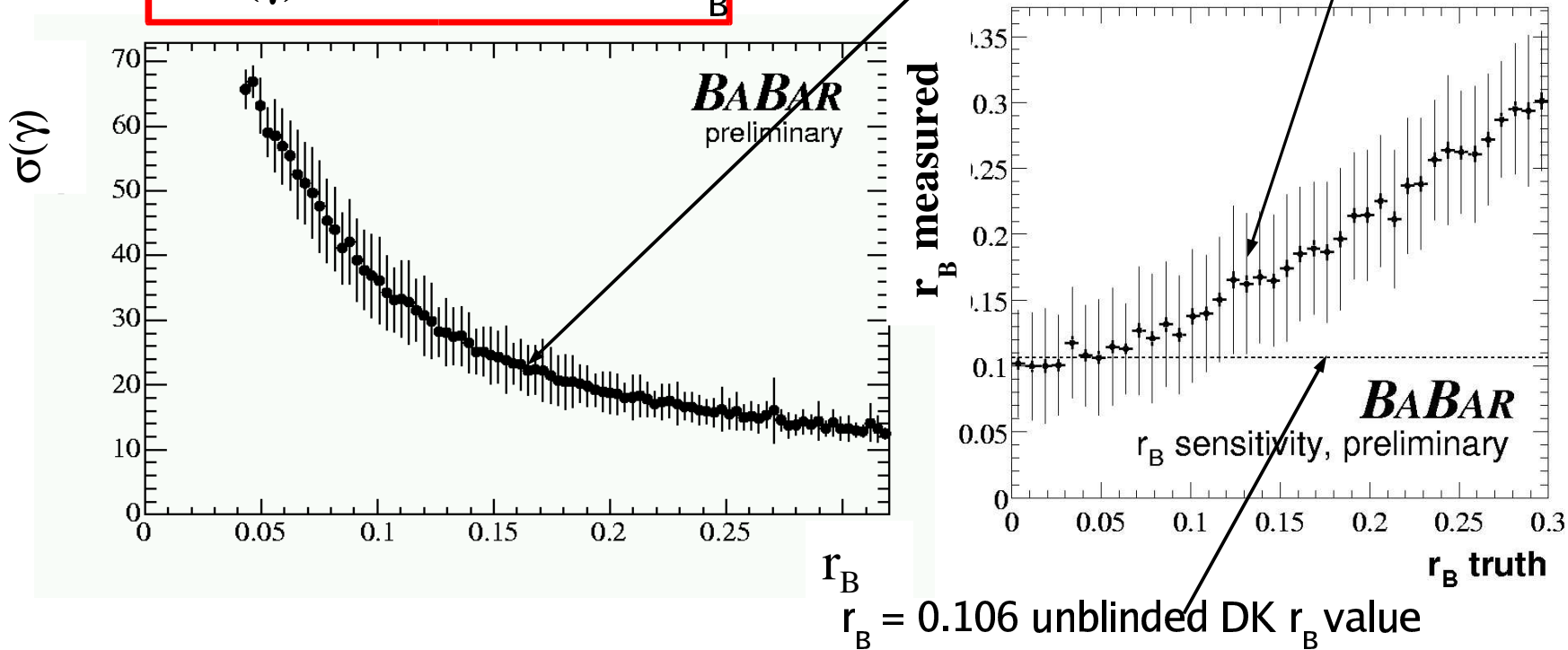
Best Candidate choice applied for DK $\chi^2 = \chi^2(m_{D^0})$ D*K $\chi^2 = \chi^2(\Delta m, (m_{\pi^0}))$



CP fit to r_B, γ, δ : Non-Gaussian effects

Strong dependency of $\sigma(\gamma)$ on the value of r_B

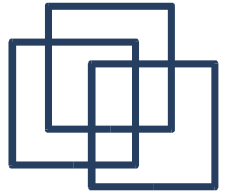
Error is the RMS of the fitted value



With current statistics, no r_B sensitivity for $r_B < 0.10$

Large non-Gaussian effects: low statistics & physical bound ($r_B \geq 0$)

Requires sophisticated statistical treatment to extract constraints on r_B and γ

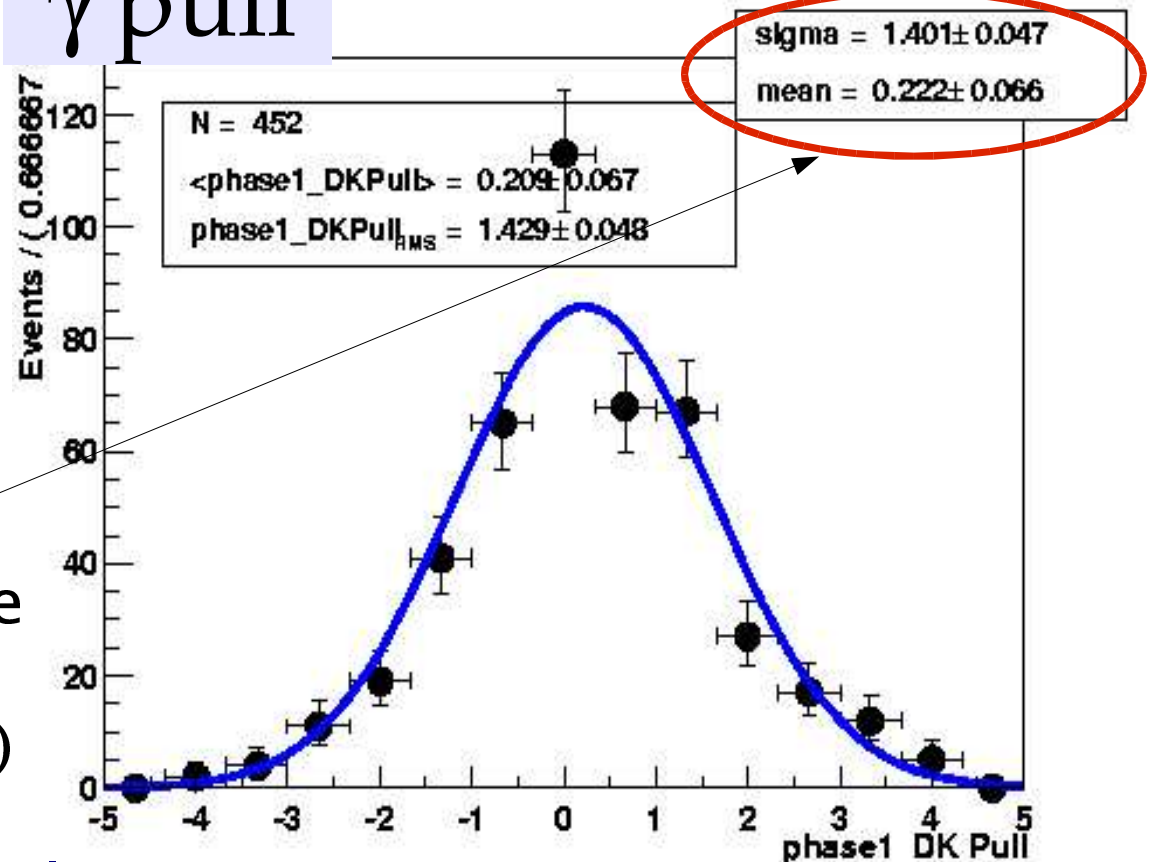


CP fit to r_B, γ, δ : Non-Gaussian effects

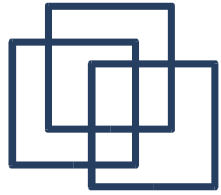
$r_B = 0.106$

γ pull

r_B estimation biased ($r_B \geq 0$)
 γ and δ are unbiased but the
statistical error is
underestimated (pulls ~ 1.4)



Cannot trust fit results (central
values and errors)



CP fit to cartesian coord (CC)

$$x_{\pm} = \text{Re}[r_{B\pm} \exp^{i(\delta\pm\gamma)}] = r_{B\pm} \cos(\delta\pm\gamma) \quad , \quad y_{\pm} = \text{Im}[r_{B\pm} \exp^{i(\delta\pm\gamma)}] = r_{B\pm} \sin(\delta\pm\gamma)$$

Nominal Dalitz fit to BlackDiamond data set

Observable	$D^0 K$	$D^{*0} K$
x_-	$0.0772^{+0.0688}_{-0.0708} [\pm 0.0692]$	$-0.1306^{+0.0940}_{-0.0935} [\pm 0.0934]$
y_-	$0.0635^{+0.0953}_{-0.0888} [\pm 0.0919]$	$-0.1433^{+0.1064}_{-0.1059} [\pm 0.1049]$
x_+	$-0.1287^{+0.0701}_{-0.0704} [\pm 0.0703]$	$0.1397^{+0.0941}_{-0.0943} [\pm 0.0926]$
y_+	$0.0186^{+0.0762}_{-0.0814} [\pm 0.0787]$	$0.0131^{+0.1183}_{-0.1201} [\pm 0.1195]$

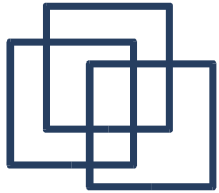
Correlations $D^0 K$

Observable	x_-	y_-	x_+	y_+
x_-	1	2.5×10^{-2}	9.4×10^{-5}	-3.0×10^{-5}
y_-		1	-1.8×10^{-4}	-2.3×10^{-4}
x_+			1	6.0×10^{-2}

Correlations $D^{*0} K$

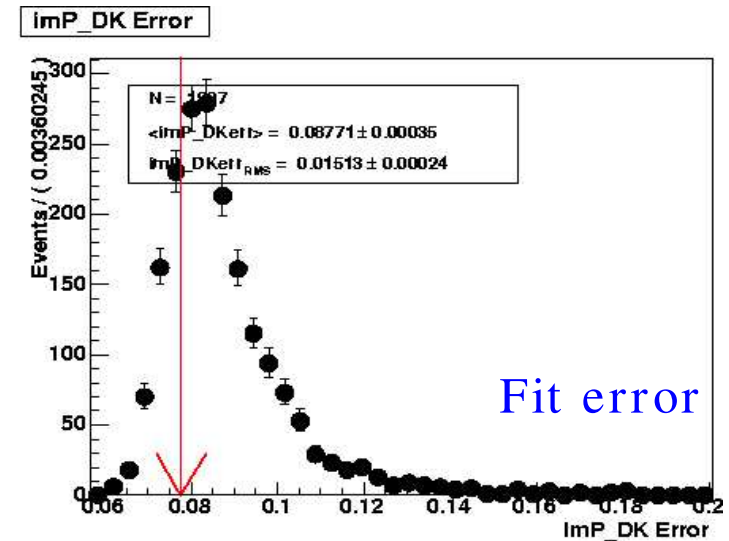
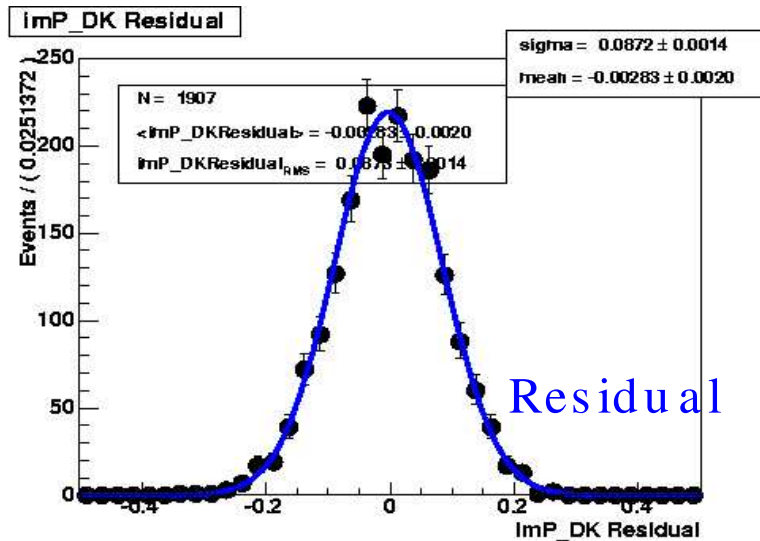
Observable	x_-	y_-	x_+	y_+
x_-	1	-1.7×10^{-1}	-6.3×10^{-3}	3.6×10^{-3}
y_-		1	-5.7×10^{-3}	2.6×10^{-3}
x_+			1	-2.7×10^{-1}

Are these results statistically meaningful?

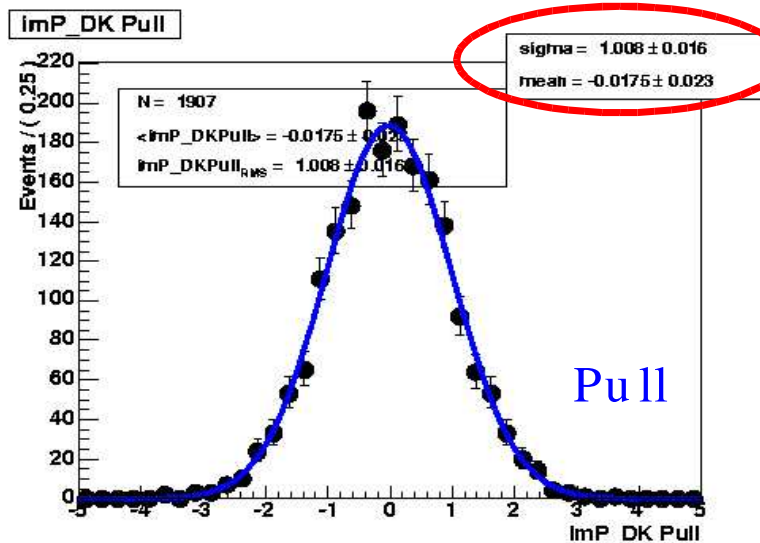


Cartesian coordinates: toy MC

y-



D0K



Excellent Gaussian behavior!

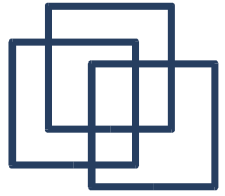
Correlations among coordinates all zero, except pairs

(x-,y-) D0K

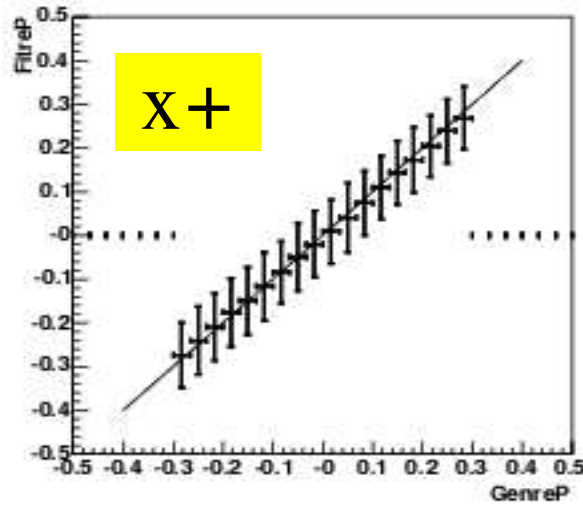
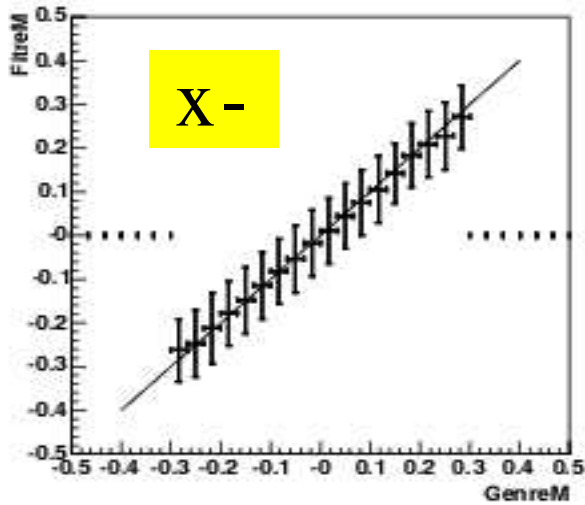
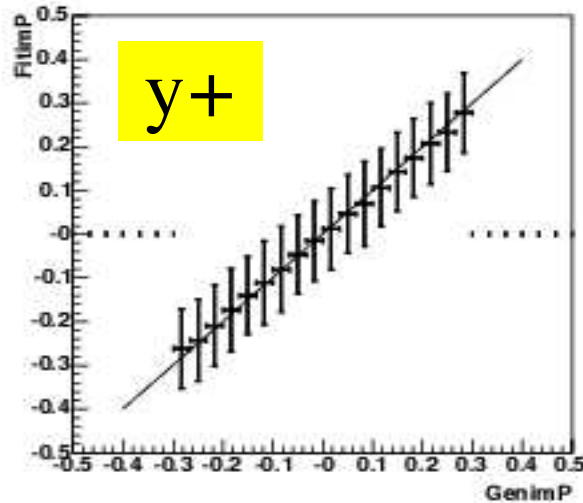
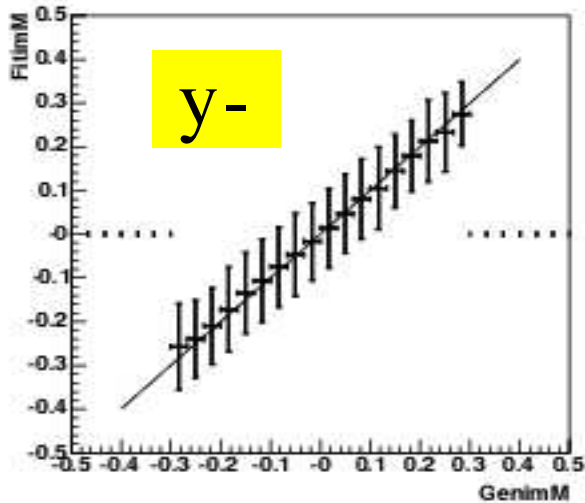
(x+,y+) D0K

(x-,y-) D*0K

(x+,y+) D*0K



Cartesian coordinates: toy MC

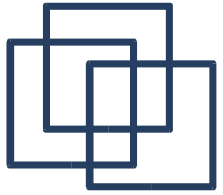


Excellent linearity and rms stability !

Stability of fit error and residual width (σ_{xy}) studied in bins of truth r_B in range [0,0.3]

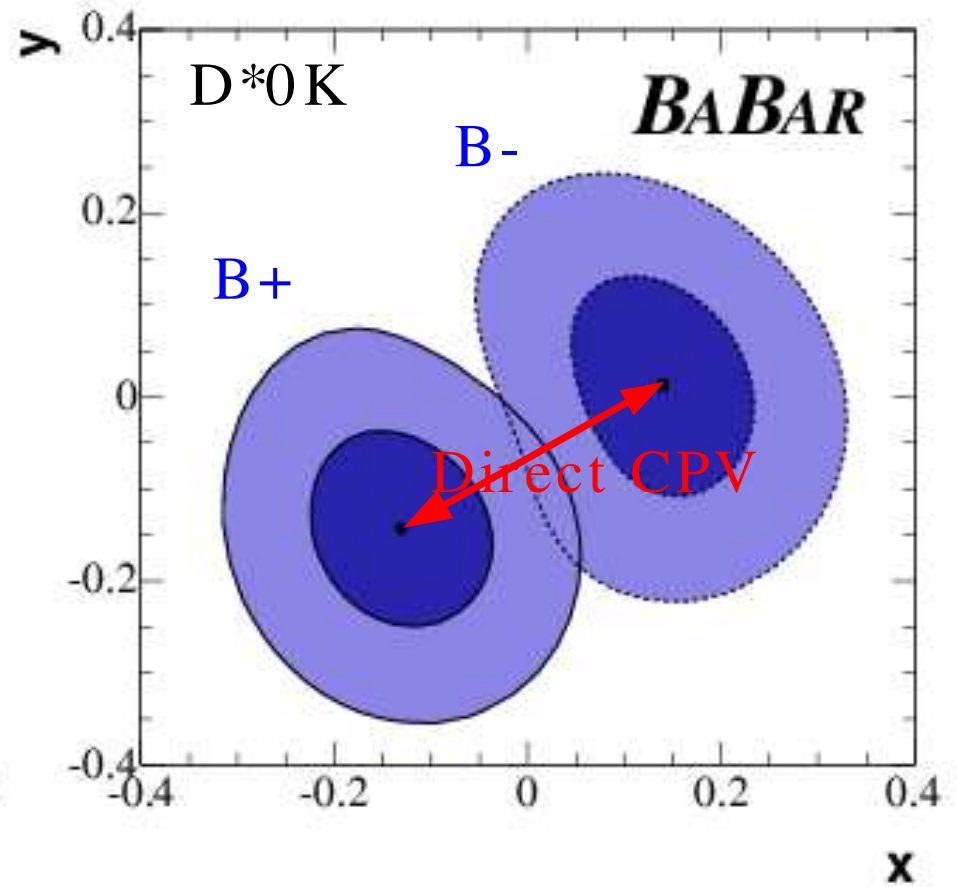
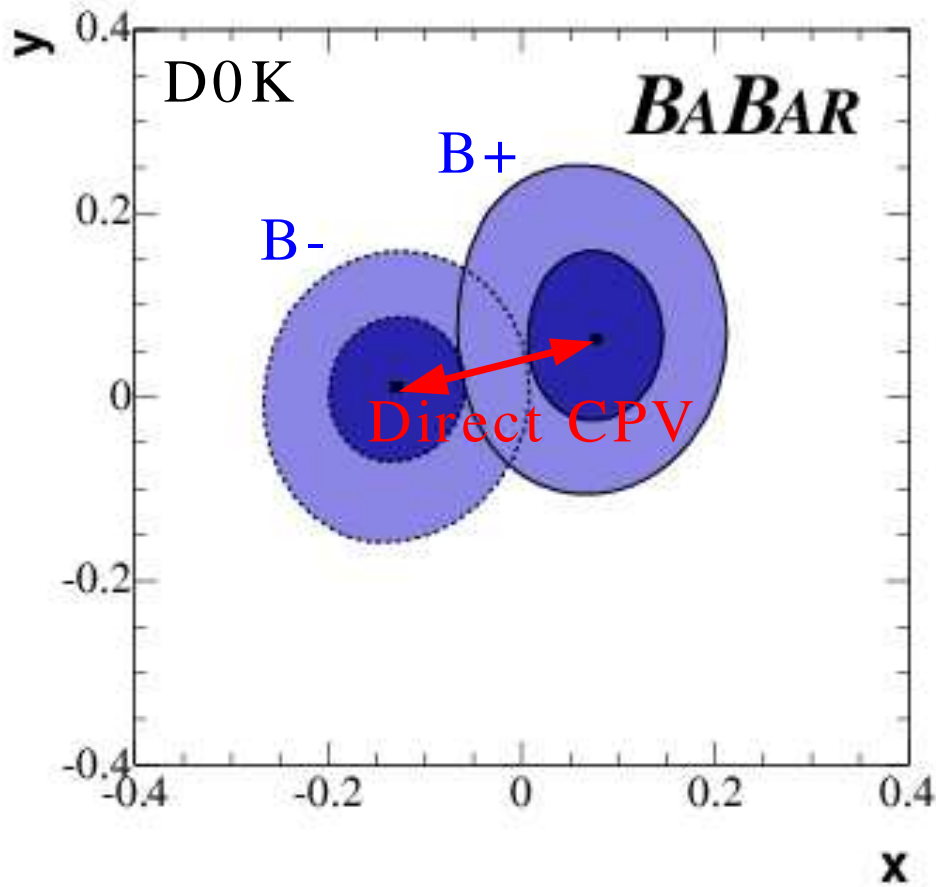
Good <10% (deviations only at large, unrealistic r_B values)

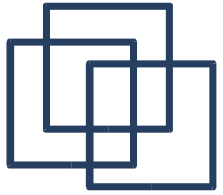
Same behavior for normalized residual



CP fit to CC: likelihood contours

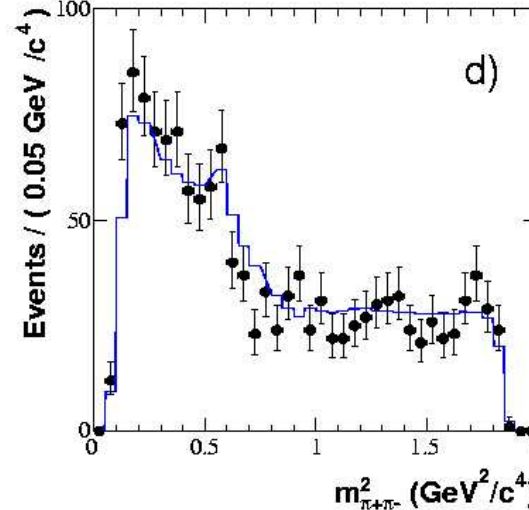
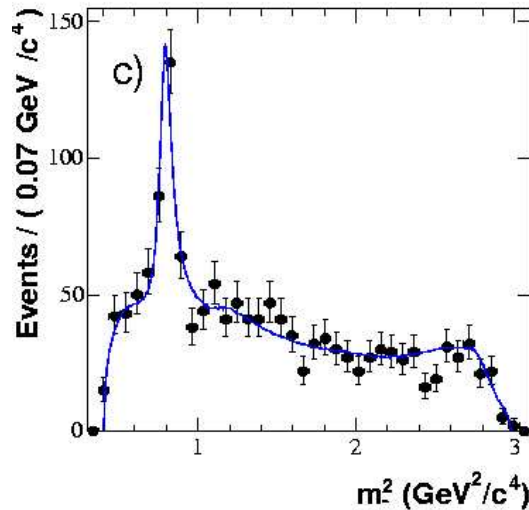
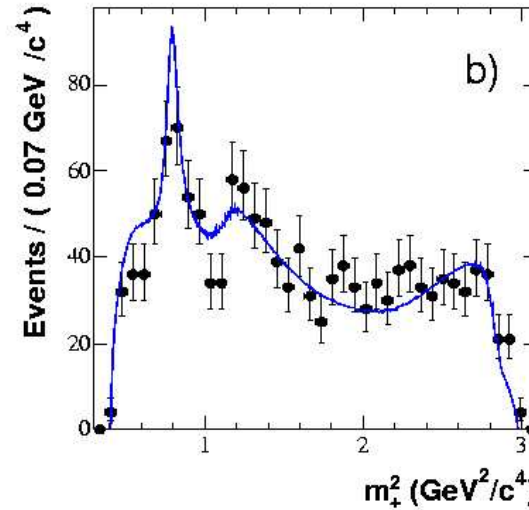
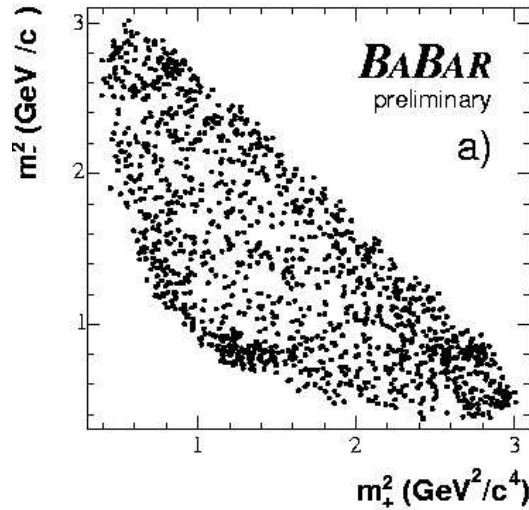
Likelihood contours from $\Delta\ln L = 0.5, 1.921$ (68.3%, 95% CL)



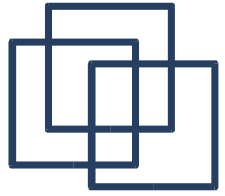


CP fit to CC: Dalitz distributions

D0K

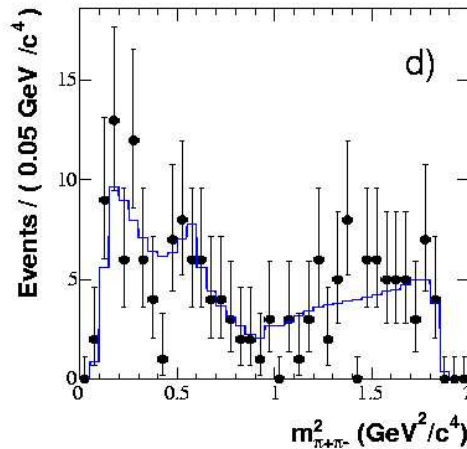
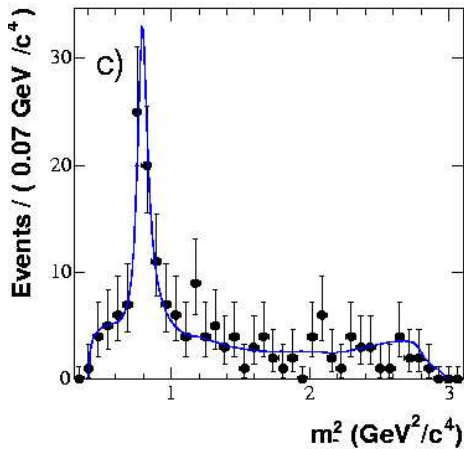
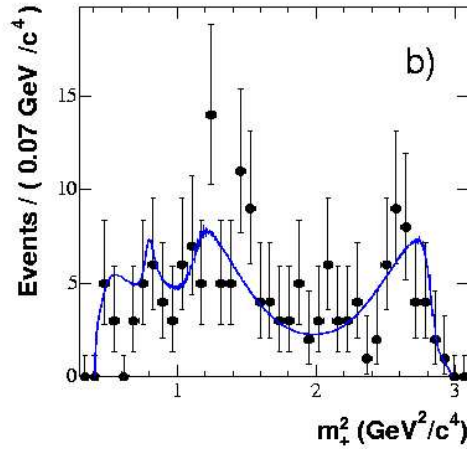
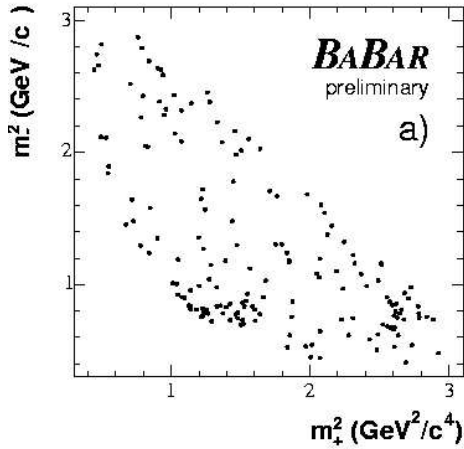


B candidates with $m_{ES} > 5.272 \text{ GeV}/c^2$

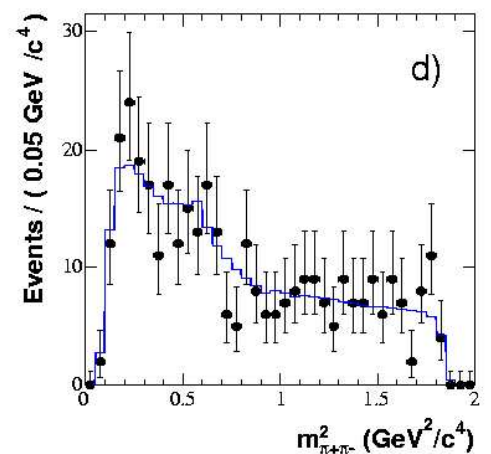
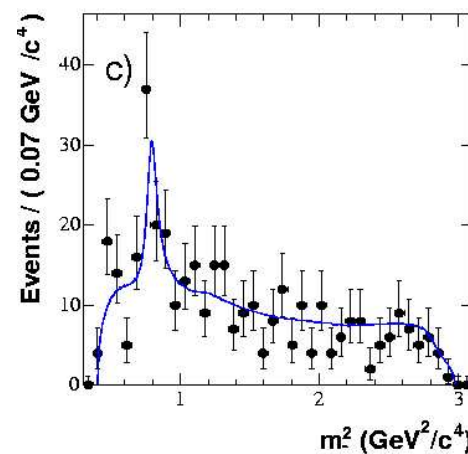
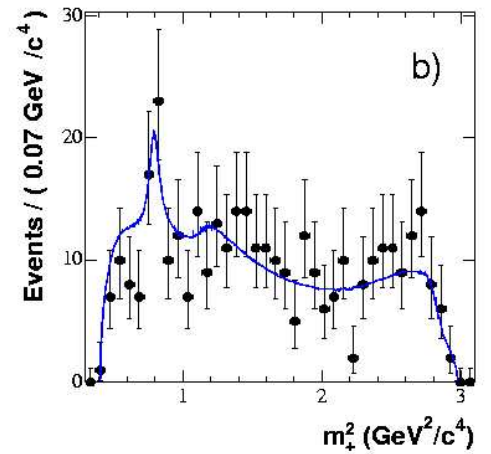
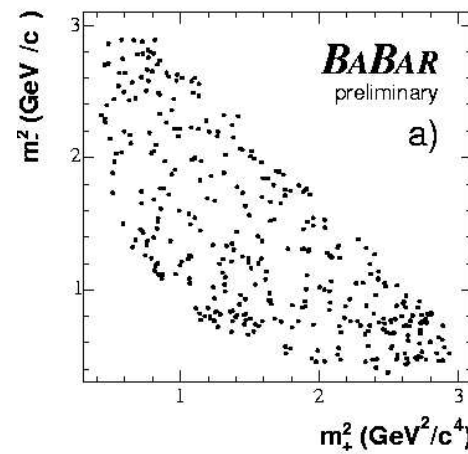


CP fit to CC: Dalitz distributions

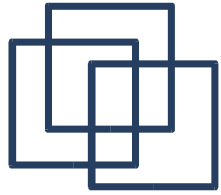
(D0 π^0)K



(D0 γ)K

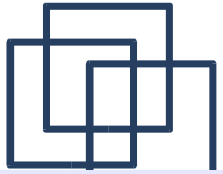


B candidates with $m_{ES} > 5.272 \text{ GeV}/c^2$



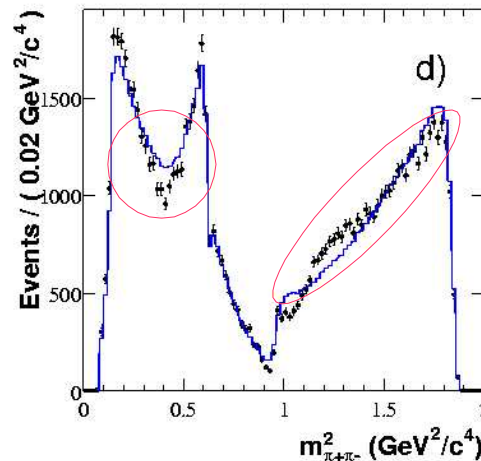
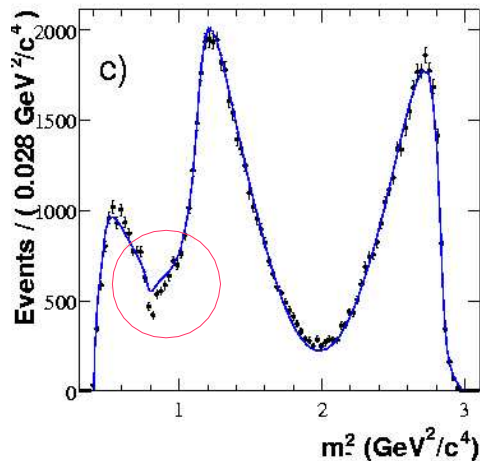
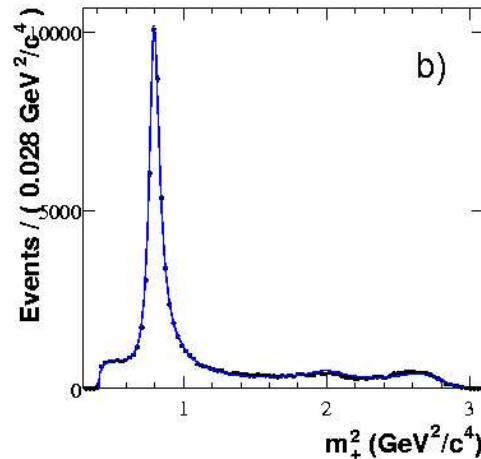
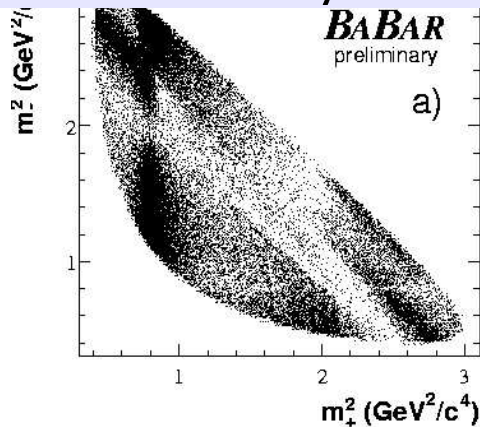
CP fit to CC: systematic errors

Source	x_+	y_+	x_-	y_-	x_+^*	y_+^*	x_-^*	y_-^*
$m_{ES}, \Delta E, \mathcal{F}$ shapes	0.0105	0.0086	0.0088	0.0141	0.0196	0.0218	0.0218	0.0146
Real D^0 fraction	0.0050	0.0047	0.0061	0.0036	0.0035	0.0049	0.0028	0.0032
Right sign D^0 's	0.0157	0.0090	0.0070	0.0211	0.0065	0.0163	0.0108	0.0103
Eff. in the Dalitz plot	0.0078	0.0085	0.0089	0.0119	0.0067	0.0119	0.0040	0.0079
Tracking efficiency	0.0082	0.0080	0.0095	0.0123	0.0058	0.0109	0.0051	0.0046
Cont bkg. Dalitz shape	0.0195	0.0096	0.0160	0.0149	0.0133	0.0084	0.0083	0.0046
BB bkg. Dalitz shape	0.0026	0.0072	0.0069	0.0130	0.0061	0.0098	0.0029	0.0003
Invariant mass resolution	0.0031	0.0023	0.0022	0.0016	0.0031	0.0023	0.0022	0.0016
Dalitz amplitude and phases	0.0012	0.0069	0.0050	0.0033	0.0043	0.0138	0.0079	0.0079
Sub Total	0.0301	0.0226	0.0258	0.0368	0.0275	0.0373	0.0280	0.0223
Dalitz model	0.0068	0.0057	0.0414	0.0109	0.0084	0.0058	0.0346	0.0320
Total	0.0309	0.0232	0.0488	0.0384	0.0288	0.0377	0.0445	0.0390



Dalitz model systematics

BaBar data with CLEO model fit overlaid



Change Blatt-Weisskopf penetration factors (negligible)
Take into account the fit uncertainty of the phases and amplitudes of the resonances
Use different models for the $K_S\pi\pi$ Dalitz decay

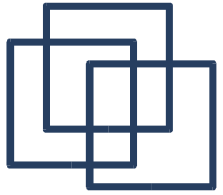
CLEO model is the worse tried model (χ^2 and total fit fraction)

Remove

$K^*(1430)$ DCS,
 $K^*(1430)$ DCS,
 $K^*(1410)$,
 $\rho(1450)$,
 σ_1 ,
 σ_2

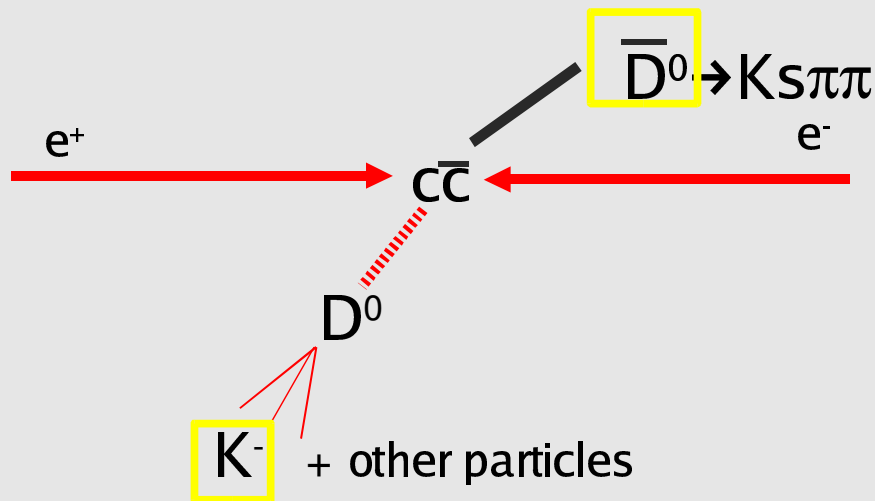
All single Breit-Wigners

Dalitz model uncertainty on γ : 10 degree



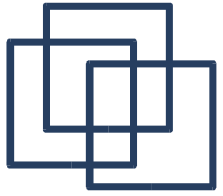
Right sign D^0 systematics

D^0 charge correlation in $c\bar{c}$ events



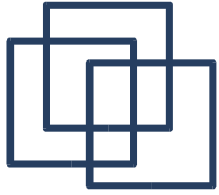
It is more probable to reconstruct a $B^- \rightarrow \bar{D}^0 K^-$

Estimate parameter $R = B^- \rightarrow \bar{D}^0 K^- / (B^- \rightarrow D^0 K^- + B^+ \rightarrow \bar{D}^0 K^-)$ on MC
Vary between the nominal value and 0.5 (quite conservative)



Frequentist interpretation

- Use a frequentist (classical) approach to determine CL regions in $r_B^{(*)}$, γ , $\delta^{(*)}$
- Determines α CL regions so that the probability that the region will contain the true point is α
- Basic problem: find PDF of fitted parameters as a function of the true parameters
 - In principle, fitted-true parameter mapping requires multi-dimensional scan of the experimental (full) likelihood
 - prohibitive amount of CPU and limited precision (steps in the scan)
 - Make optimal choice of fit parameters space and try analytical construction
 - **Cartesian coordinates**



The frequentist PDF

Single channel (D0K or D*0K)

Measured parameters (4D): $\mathbf{z}_+ \equiv (x_+, y_+)$, $\mathbf{z}_- \equiv (x_-, y_-)$

Truth parameters (3D): r_B, γ, δ

$$\frac{d^4 P}{d^2 \mathbf{z}_+ d^2 \mathbf{z}_-}(\mathbf{z}_+, \mathbf{z}_- | \mathbf{p}^t) = G_2(\mathbf{z}_+; r_B^t \cos(\delta^t + \gamma^t), r_B^t \sin(\delta^t + \gamma^t), \sigma_{x_+}, \sigma_{y_+}, \rho_+) \times \\ G_2(\mathbf{z}_-; r_B^t \cos(\delta^t - \gamma^t), r_B^t \sin(\delta^t - \gamma^t), \sigma_{x_-}, \sigma_{y_-}, \rho_-)$$

where

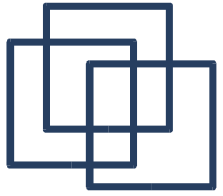
$$G_2(\mathbf{z}; \mu_x, \mu_y, \sigma_x, \sigma_y, \rho) = \frac{1}{2\pi\sigma_x\sigma_y\sqrt{1-\rho^2}} e^{-\frac{1}{2(1-\rho^2)} \left[\frac{(x-\mu_x)^2}{\sigma_x^2} + \frac{(y-\mu_y)^2}{\sigma_y^2} - \frac{2\rho(x-\mu_x)(y-\mu_y)}{\sigma_x\sigma_y} \right]}$$

D0K-D*0K combination

Measured parameters (8D): $\mathbf{z}_+, \mathbf{z}_-, \mathbf{z}_+^*, \mathbf{z}_-^*$

Truth parameters (5D): $r_B, \gamma, \delta, r_B^*, \delta^*$

$$\frac{d^8 P}{d^2 \mathbf{z}_+ d^2 \mathbf{z}_- d^2 \mathbf{z}_+^* d^2 \mathbf{z}_-^*}(\mathbf{z}_+, \mathbf{z}_-, \mathbf{z}_+^*, \mathbf{z}_-^* | \mathbf{p}^t) = \frac{d^4 P_B}{d^2 \mathbf{z}_+ d^2 \mathbf{z}_-}(\mathbf{z}_+, \mathbf{z}_- | r_B^t, \gamma^t, \delta^t) \times \\ \frac{d^4 P_B}{d^2 \mathbf{z}_+^* d^2 \mathbf{z}_-^*}(\mathbf{z}_+^*, \mathbf{z}_-^* | r_B^{*t}, \gamma^t, \delta^{*t})$$



Confidence Regions (CR): DOK-D*OK combination

$$\alpha(\mathbf{p}^t) = \int_D \frac{d^8 P}{d^2 \mathbf{z}_+ d^2 \mathbf{z}_- d^2 \mathbf{z}_+^* d^2 \mathbf{z}_-^*}(\mathbf{z}_+, \mathbf{z}_-, \mathbf{z}_+^*, \mathbf{z}_-^* | \mathbf{p}^t) d^2 \mathbf{z}_+ d^2 \mathbf{z}_- d^2 \mathbf{z}_+^* d^2 \mathbf{z}_-^* \quad \text{CL}=1 - \alpha(\mathbf{p}^t)$$

$$\frac{d^8 P}{d^2 \mathbf{z}_+ d^2 \mathbf{z}_- d^2 \mathbf{z}_+^* d^2 \mathbf{z}_-^*}(\mathbf{z}_+, \mathbf{z}_-, \mathbf{z}_+^*, \mathbf{z}_-^* | \mathbf{p}^t) \geq \frac{d^8 P}{d^2 \mathbf{z}_+ d^2 \mathbf{z}_- d^2 \mathbf{z}_+^* d^2 \mathbf{z}_-^*}(\mathbf{z}_+^{\text{data}}, \mathbf{z}_-^{\text{data}}, \mathbf{z}_+^{\text{data}*}, \mathbf{z}_-^{\text{data}*} | \mathbf{p}^t)$$

Integration domain D (CR)
Likelihood ordering

Generate $\approx 200\text{M}$ \mathbf{p}^t points

Calculate $\alpha(\mathbf{p}^t)$: Calculated analytically (hyperspheric coordinates)

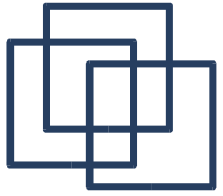
Select points $\alpha(\mathbf{p}^t) \leq \alpha_0$

Chose $\alpha_0 = 0.037, 0.428$

5D joint probability (cumulative χ^2 integral for $\nu=5$)

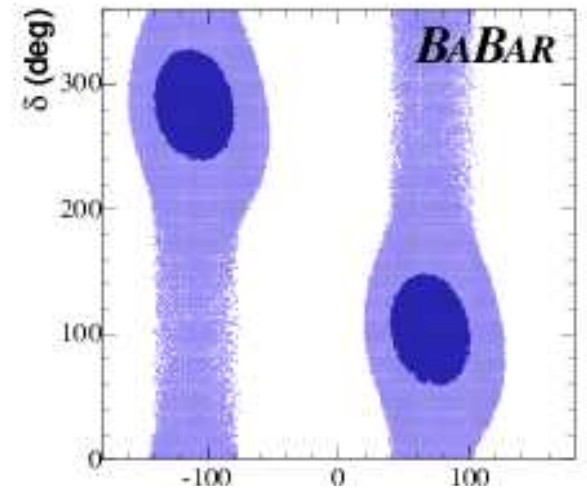
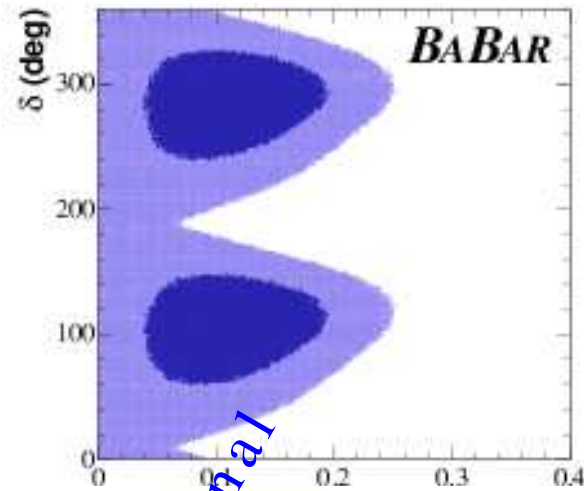
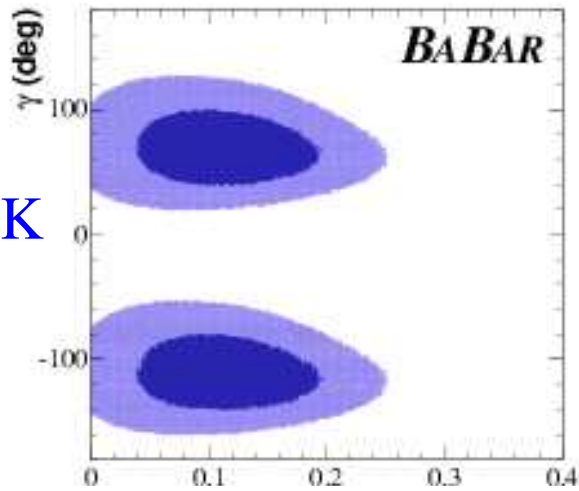
Correspond to 1σ and 1.96σ ellipsoids

Make 1D projections to quote 1σ and 1.96σ regions

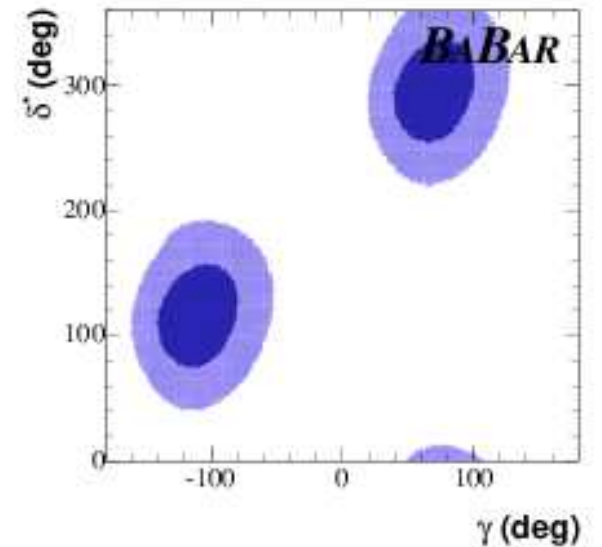
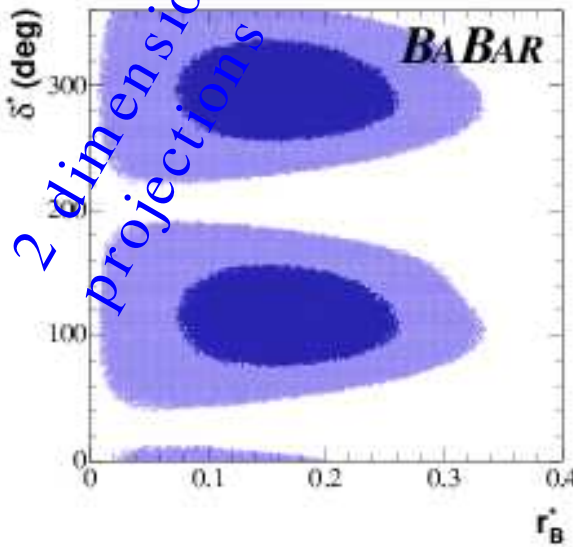
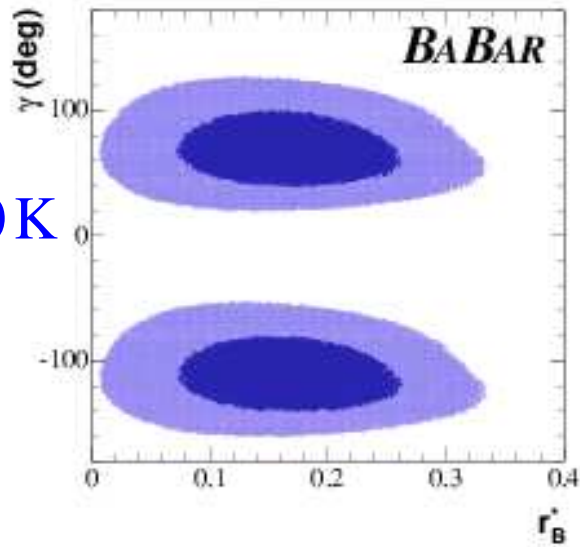


D0K-D*0K combined CR I

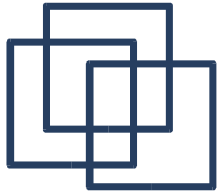
D0K



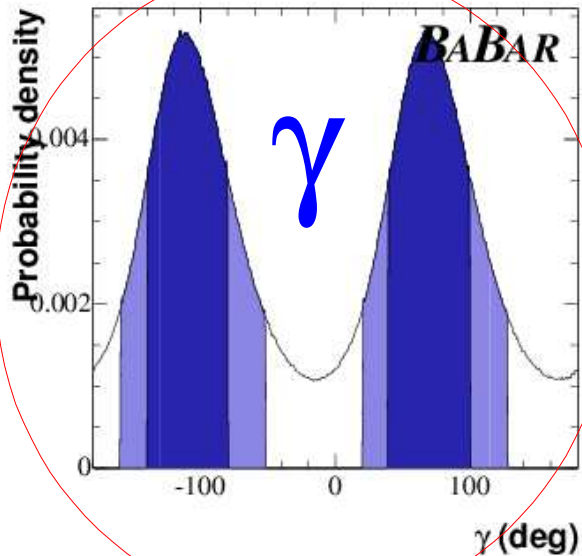
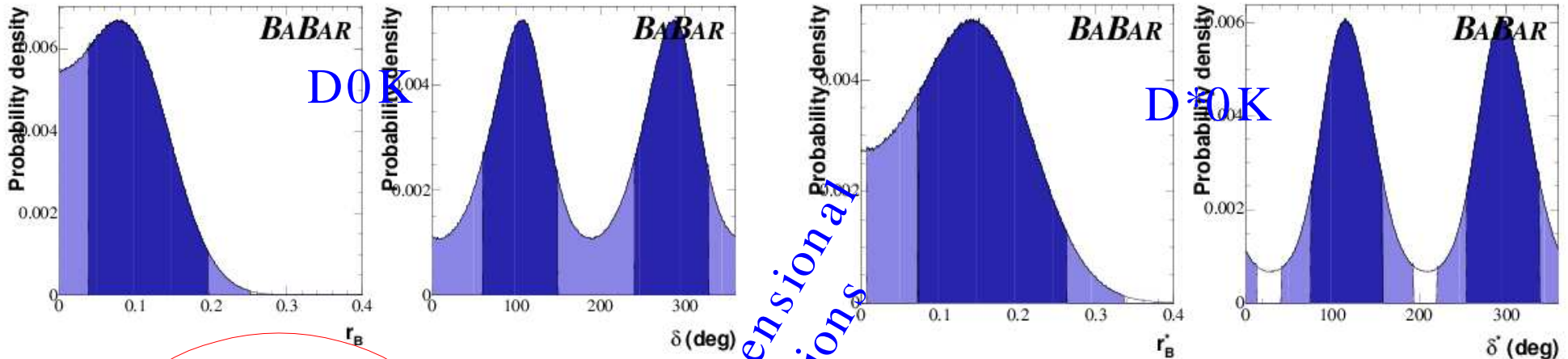
D*0K



2 dimensional
projections



D0K-D*0K combined CR II

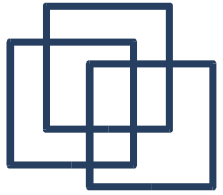


1 dimensional projections

Parameter	1σ	1.96σ	Central value with error (1σ)
γ	[39,101] [220,280]	[20,129] [200,309]	70 ± 31
r_B	[0.039,0.198]	[0,0.253]	0.119 ± 0.079
r_B^*	[0.072],0.264]	[0.007,0.337]	0.168 ± 0.096
δ	[60,150] [240,329]	-	105 ± 45
δ^*	[254,339] [75,158]	[221,374] [41,194]	296 ± 43

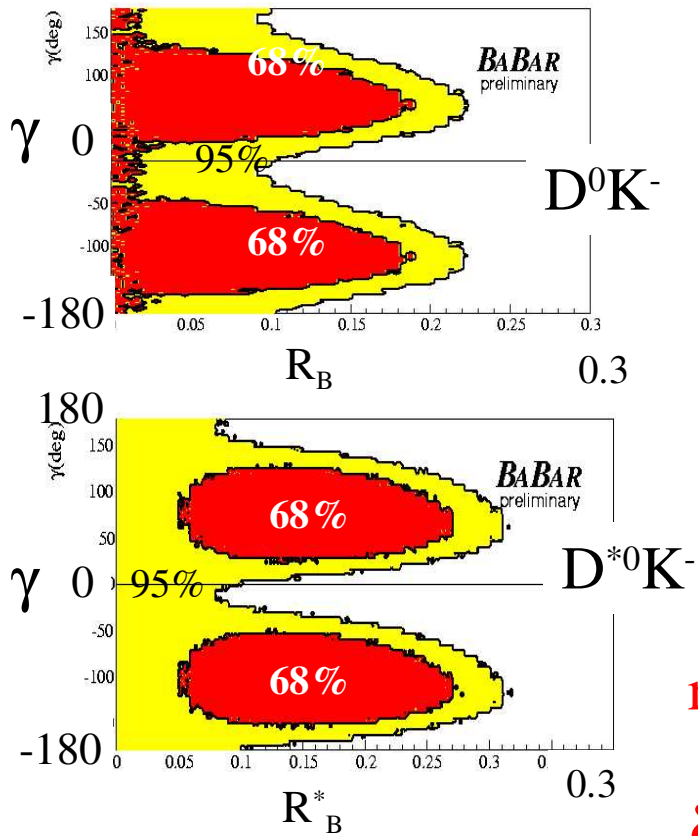
Statistical uncertainties only

Central values are the mean of the confidence intervals



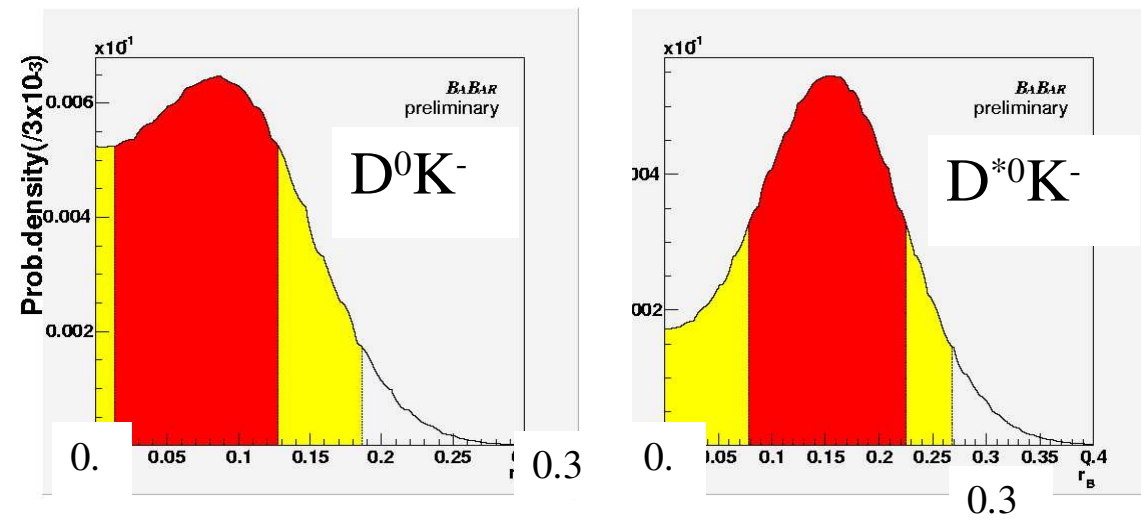
Bayesian approach (check)

180 Updated ICHEP result



Bayesian confidence regions

A posteriori $r_B(r_B^)$ with uniform a priori*



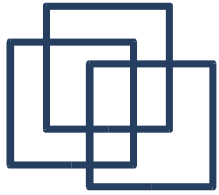
$r_B < 0.19$ (90%CL) $r_B^* = 0.16^{+0.07}_{-0.08} \pm 0.04 \pm 0.02$
stat+syst *stat+syst*

$\delta_B = 114^\circ \pm 41^\circ \pm 8^\circ \pm 10^\circ$ $\delta_B^* = 303^\circ \pm 34^\circ \pm 14^\circ \pm 10^\circ$

$\gamma = 70 \pm 26^\circ \pm 10^\circ \pm 10^\circ$

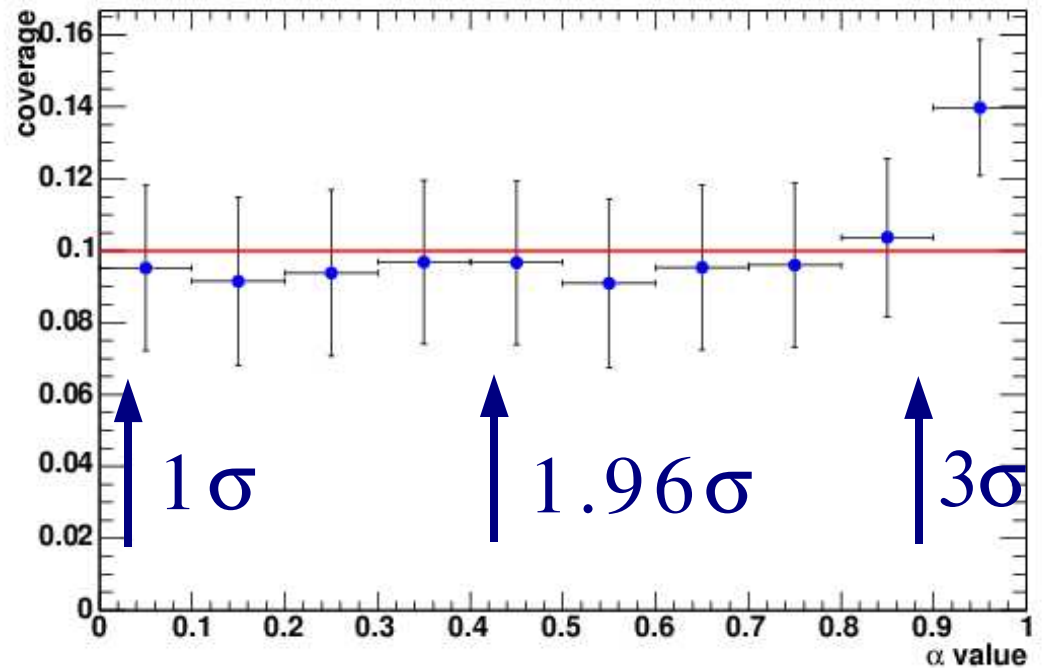
Dalitz model syst

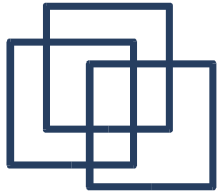
Good agreement with frequentist method !



Frequentist coverage

- Check coverage using experimental (full) likelihood
 - Verify perfect Gaussian behavior, fit error and correlation stability
- Generate 20K toy MC experiments tuned to data using as truth point $\mathbf{pt}=(r_B, r_B^*, \gamma, \delta, \delta^*)$ the fr
- For each experiment:
 - Perform fit in cartesian parameter space
 - Calculate $\alpha(\mathbf{pt})$
 - Count number of experiments for which $\alpha(\mathbf{pt}) \leq \alpha_0$



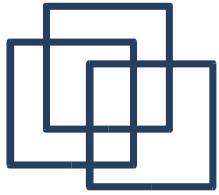


Significance of CP Violation

- Significance of CP Violation determined by evaluating the CL of the most probable CP conserving \mathbf{p}^t point
 - CL most probable CP conserving point = $1 - \alpha_{\min}$
 - Significance of CP violation or CL of CP violation = α_{\min}

$$\mathbf{p}_{CP}^t = \{\mathbf{p}^t | \mathbf{p}^t = (r_B^t = 0, r_B^{*t} = 0, \gamma^t, \delta^t, \delta^{*t}) \text{ or } \mathbf{p}^t = (r_B^t, r_B^{*t}, \gamma^t = 0, \delta^t, \delta^{*t})\}$$

- D0K only (statistical): $\alpha_{\min} = 65.5\% (1.82\sigma)$
- D*0K only (statistical): $\alpha_{\min} = 82.8\% (2.24\sigma)$
- D0K+D*0K (statistical): $\alpha_{\min} = \mathbf{79.1\% (2.68\sigma)}$



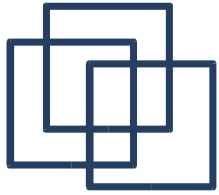
Systematic uncertainties

Systematic uncertainties easily included by replacing the statistical errors in frequentist PDF ($\sigma_{x+}, \sigma_{y+}, \dots$) by the total

Parameter	1σ	1.96σ	Central value with error (1σ)
γ	[37,104] [217,284]	[13,134] [191,314]	70 ± 34
r_B	[0.029,0.206]	[0,0.268]	0.118 ± 0.089
r_B^*	[0.066],0.271]	[0.000,0.348]	0.169 ± 0.103
δ	[54,156] [233,335]	–	105 ± 51
δ^*	[253,342] [72,163]	–	298 ± 45

Significance of CP violation $D^0K+D^{*0}K$
(statistical+systematic)

$$\alpha_{\min} = 72.1\% (2.51\sigma)$$



Summary and plans

- We have measured the CP violating parameters:

$$x_+ = r_{B^+} \cos(\delta+\gamma) = -0.129 \pm 0.070 \pm 0.031$$

$$y_+ = r_{B^+} \sin(\delta+\gamma) = 0.019 \pm 0.079 \pm 0.023$$

$$x_- = r_{B^-} \cos(\delta-\gamma) = 0.077 \pm 0.069 \pm 0.049$$

$$y_- = r_{B^-} \sin(\delta-\gamma) = 0.064 \pm 0.092 \pm 0.038$$

$$x_+^* = r_{B^+}^* \cos(\delta^*+\gamma) = 0.140 \pm 0.093 \pm 0.029$$

$$y_+^* = r_{B^+}^* \sin(\delta^*+\gamma) = 0.013 \pm 0.120 \pm 0.038$$

$$x_-^* = r_{B^-}^* \cos(\delta^*-\gamma) = -0.131 \pm 0.093 \pm 0.045$$

$$y_-^* = r_{B^-}^* \sin(\delta^*-\gamma) = -0.143 \pm 0.105 \pm 0.039$$

- A frequentist analysis of these results yields:

$$\gamma = (70 \pm 34)^\circ$$

- **Significance of direct CP violation 2.5σ**
 - Good agreement with Bayesian analysis with flat prior
 - Planning to have PRL draft ready for CWR by the end of the month
-