



UNIVERSITÀ  
DI TORINO



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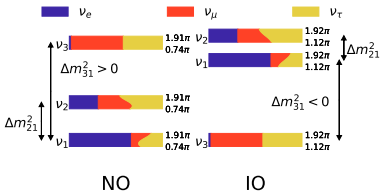
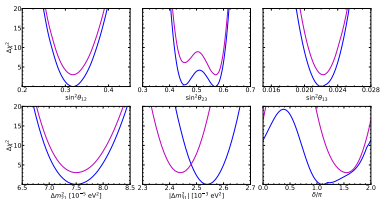
## Testing new physics scenarios with neutrino decoupling and BBN



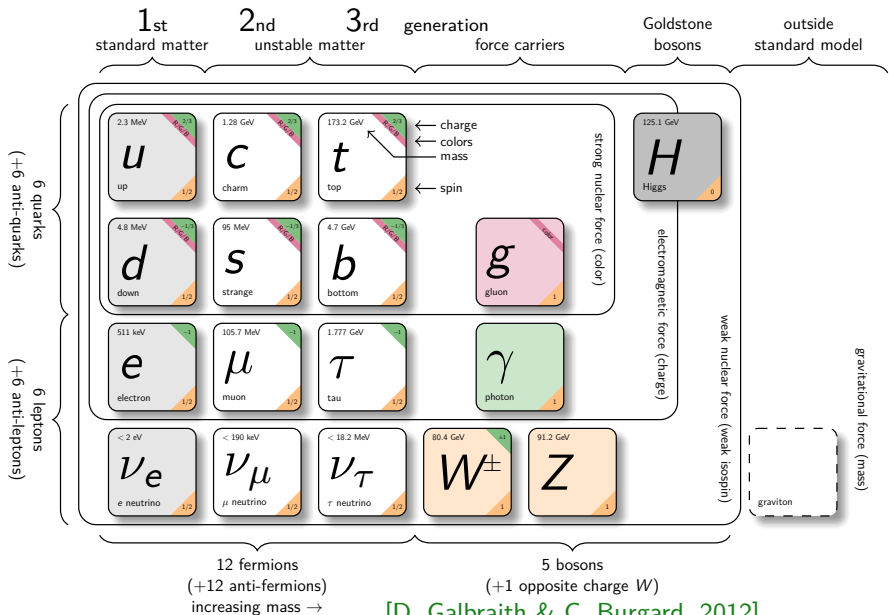
# Neutrinos

A general introduction, based on

JHEP 02 (2021) 071 and update

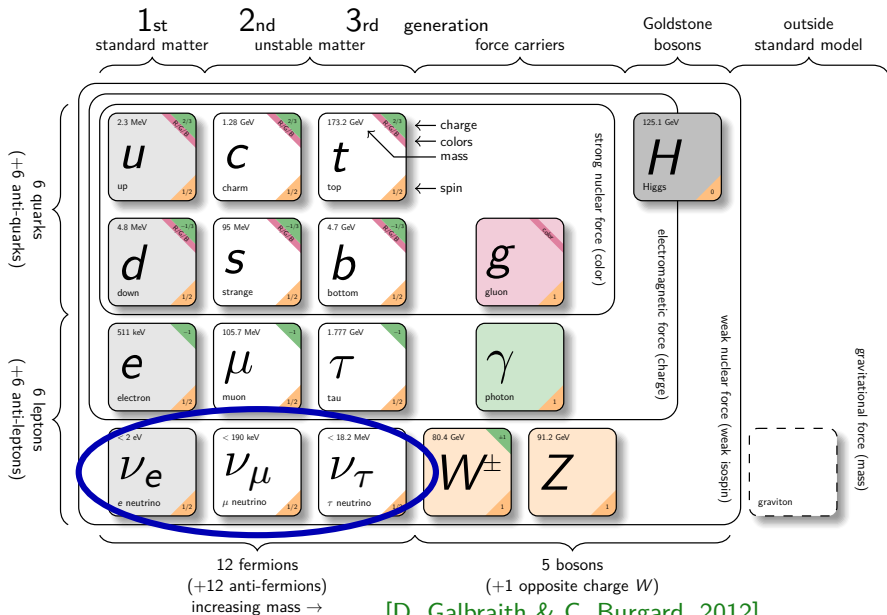


# The Standard Model of Particle Physics



[D. Galbraith & C. Burgard, 2012]

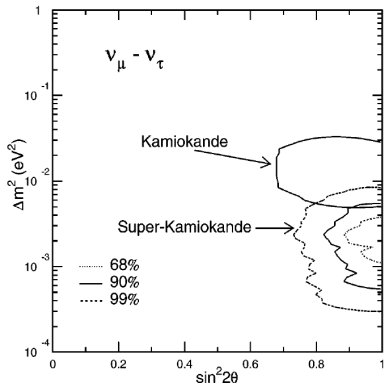
# The Standard Model of Particle Physics



# Neutrino oscillations

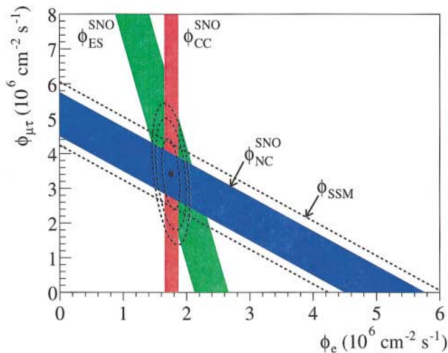
Major discoveries:

[SuperKamiokande, 1998]



first discovery of  $\nu_\mu \rightarrow \nu_\tau$   
oscillations from atmospheric  $\nu$

[SNO, 2001-2002]



first discovery of  $\nu_e \rightarrow \nu_\mu, \nu_\tau$   
oscillations from solar  $\nu$

Nobel prize in 2015

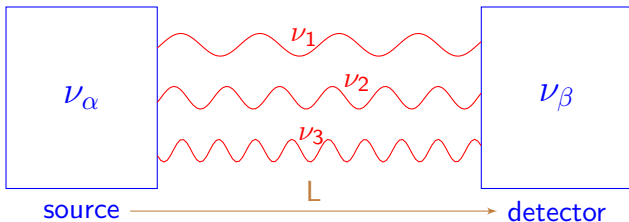
# Two neutrino bases

flavor neutrinos  $\nu_\alpha$

$$|\nu_\alpha\rangle = \sum_k U_{\alpha k} |\nu_k\rangle$$

massive neutrinos  $\nu_k$

$$|\nu(t=0)\rangle = |\nu_\alpha\rangle = U_{\alpha 1} |\nu_1\rangle + U_{\alpha 2} |\nu_2\rangle + U_{\alpha 3} |\nu_3\rangle$$



$$|\nu(t > 0)\rangle = |\nu_\beta\rangle = U_{\alpha 1} e^{-iE_1 t} |\nu_1\rangle + U_{\alpha 2} e^{-iE_2 t} |\nu_2\rangle + U_{\alpha 3} e^{-iE_3 t} |\nu_3\rangle \neq |\nu_\alpha\rangle$$

$$E_k^2 = p^2 + m_k^2 \longleftarrow \text{define} \longrightarrow t = L$$

$$P_{\nu_\alpha \rightarrow \nu_\beta}(L) = |\langle \nu_\beta | \nu(L) \rangle|^2 = \sum_{k,j} U_{\beta k} U_{\alpha k}^* U_{\beta j}^* U_{\alpha j} \exp\left(-i \frac{\Delta m_{kj}^2 L}{2E}\right)$$

$$\Delta m_{ij}^2 = m_i^2 - m_j^2$$

# The mixing matrix

$U$  can be parameterized using 3 angles ( $\theta_{12}$ ,  $\theta_{13}$ ,  $\theta_{23}$ ) and max 3 (1 Dirac  $\delta$ , 2 Majorana [ $\exists$  only for Majorana  $\nu$ ]) phases

$$U = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\substack{\text{mainly atmospheric} \\ \text{and LBL} \\ \text{accelerator} \\ \text{disappearance}}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{\substack{\text{mainly LBL reactors and} \\ \text{LBL accelerator} \\ \text{appearance}}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\substack{\text{mainly solar and} \\ \text{VLBL reactors}}} M$$

Majorana phases irrelevant for oscillation experiments ←

Relevant for example in neutrinoless double-beta decay

$$s_{ij} \equiv \sin \theta_{ij}; \quad c_{ij} \equiv \cos \theta_{ij}$$

LBL = long baseline; VLBL = very long baseline;

# Three Neutrino Oscillations

$$\nu_\alpha = \sum_{k=1}^3 U_{\alpha k} \nu_k \quad (\alpha = e, \mu, \tau)$$

$U_{\alpha k}$  described by 3 mixing angles  $\theta_{12}$ ,  $\theta_{13}$ ,  $\theta_{23}$  and one CP phase  $\delta$

Current knowledge of the 3 active  $\nu$  mixing: [JHEP 02 (2021) update]

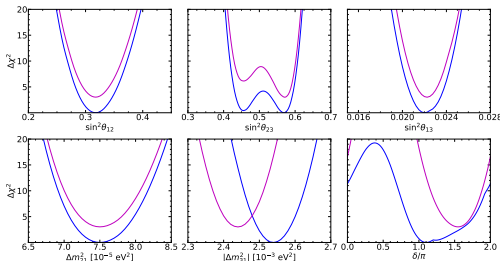
NO/NH: Normal Ordering/Hierarchy,  $m_1 < m_2 < m_3$

IO/IH: Inverted O/H,  $m_3 < m_1 < m_2$

$$\begin{aligned} \Delta m_{21}^2 &= (7.50^{+0.22}_{-0.20}) \cdot 10^{-5} \text{ eV}^2 \\ |\Delta m_{31}^2| &= (2.54 \pm 0.03) \cdot 10^{-3} \text{ eV}^2 \text{ (NO)} \\ &= (2.44 \pm 0.03) \cdot 10^{-3} \text{ eV}^2 \text{ (IO)} \end{aligned}$$

$$\begin{aligned} 10 \sin^2(\theta_{12}) &= 3.18 \pm 0.16 \\ 10^2 \sin^2(\theta_{13}) &= 2.200^{+0.069}_{-0.062} \text{ (NO)} \\ &= 2.225^{+0.064}_{-0.070} \text{ (IO)} \\ 10 \sin^2(\theta_{23}) &= 4.55 \pm 0.13 \text{ (NO)} \\ &= 5.71^{+0.14}_{-0.17} \text{ (IO)} \end{aligned}$$

$$\begin{aligned} \delta/\pi &= 1.10^{+0.27}_{-0.12} \text{ (NO)} \\ &= 1.54 \pm 0.14 \text{ (IO)} \end{aligned}$$



mass ordering  
still unknown

$\delta$  still unknown

see also: <http://globalfit.astroparticles.es>

# Neutrinos and their masses

## Normal ordering (NO)

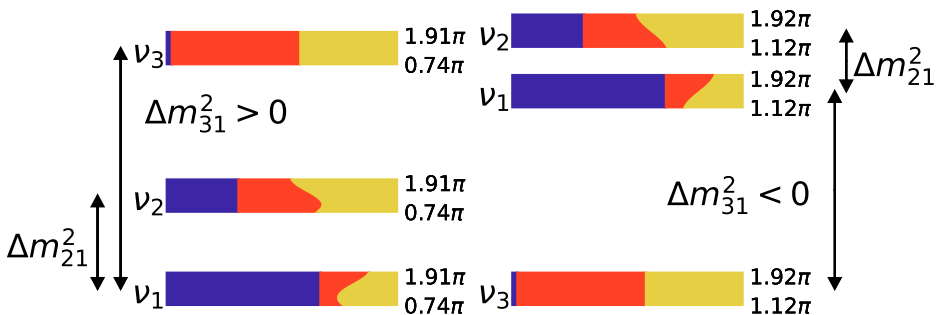
$$m_1 < m_2 < m_3$$

$$\sum m_k \gtrsim 0.06 \text{ eV}$$

## Inverted ordering (IO)

$$m_3 < m_1 < m_2$$

$$\sum m_k \gtrsim 0.1 \text{ eV}$$



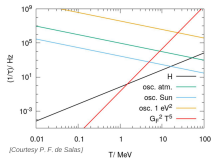
Absolute scale unknown!

Can we constrain the mass ordering using bounds on  $\sum m_\nu$ ?

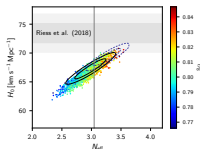


# Neutrinos in the Early Universe

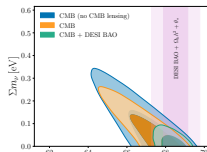
Based on



JCAP 04 (2021) 073

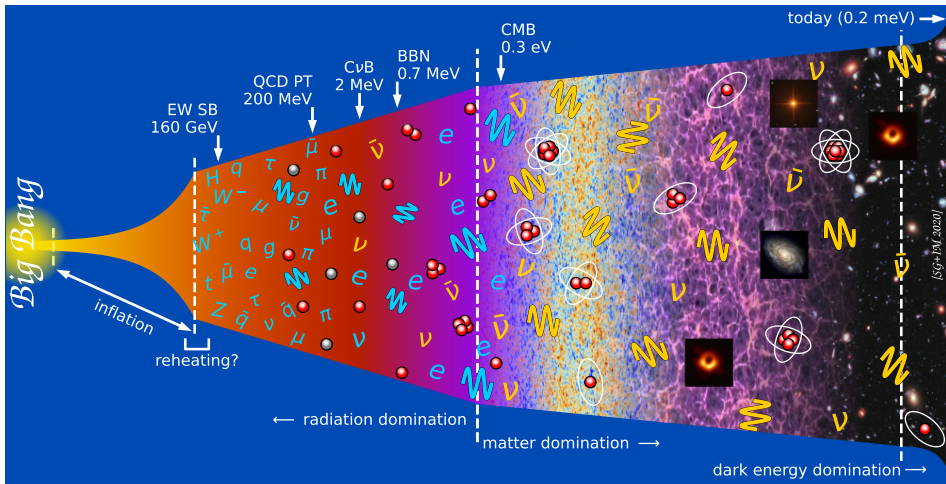


Planck 2018

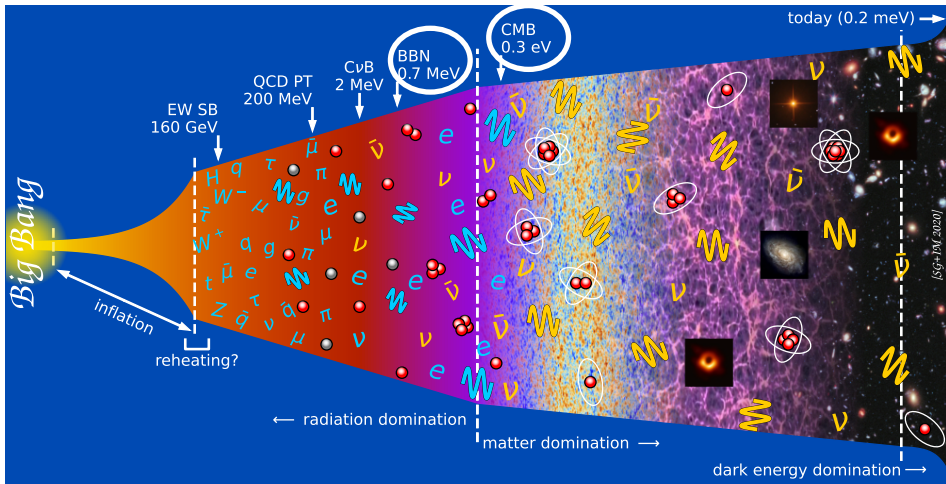


JCAP 02 (2025) 021

# History of the universe



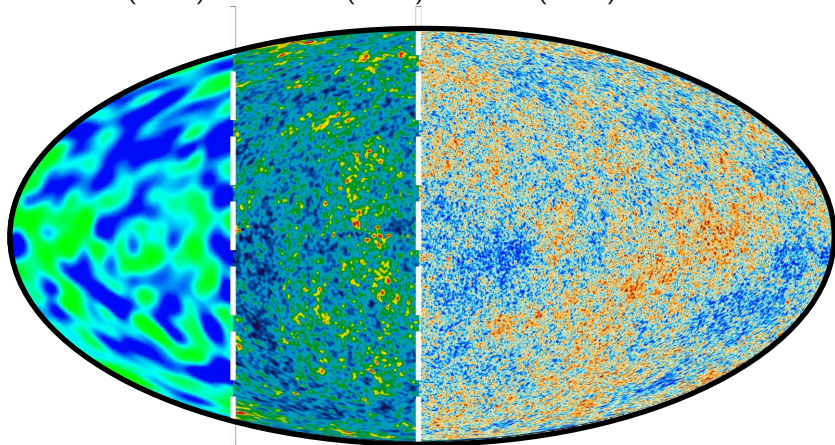
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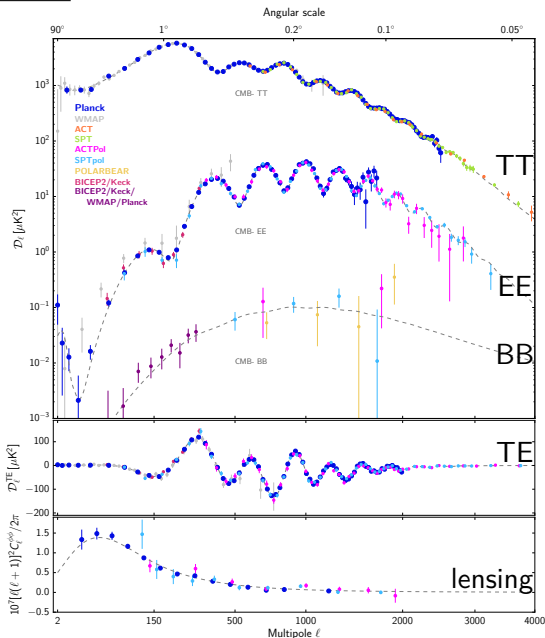
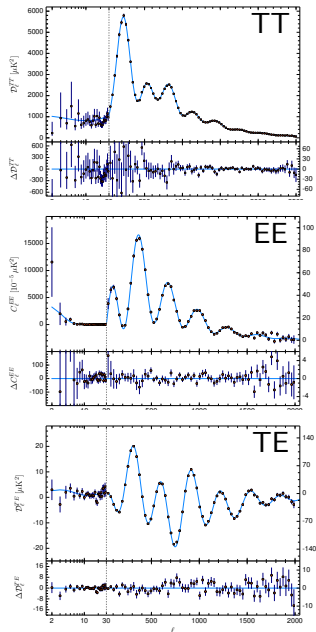


# The oldest picture of the Universe

The Cosmic Microwave Background, generated at  $t \simeq 4 \times 10^5$  years

COBE (1992)    WMAP (2003)    Planck (2013)





# Big Bang Nucleosynthesis (BBN)

BBN: production of light nuclei at  $t \sim 1\text{s}$  to  $t \sim \mathcal{O}(10^2)\text{s}$

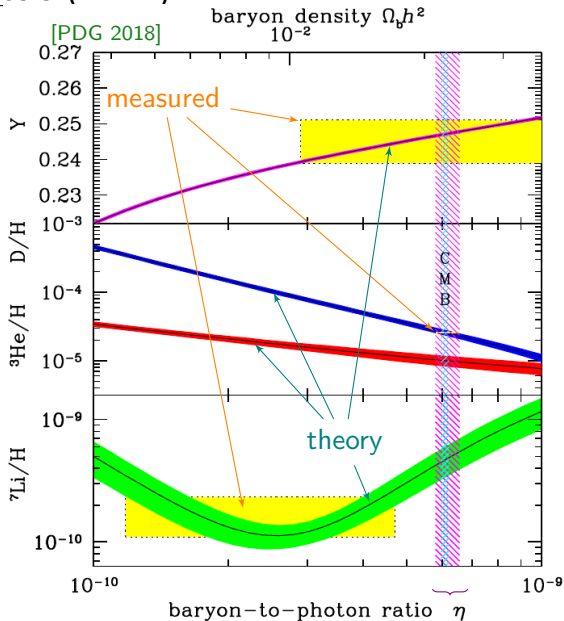
temperature  $T_{fr} \simeq 1\text{ MeV}$   
from nucleon freeze-out

much earlier than CMB!

strong probe for physics  
before the CMB

e.g. neutrinos!

$\nu$  affect  
universe expansion  
and  
reaction rates ( $\nu_e/\bar{\nu}_e$ )  
at BBN time...



BBN concordance

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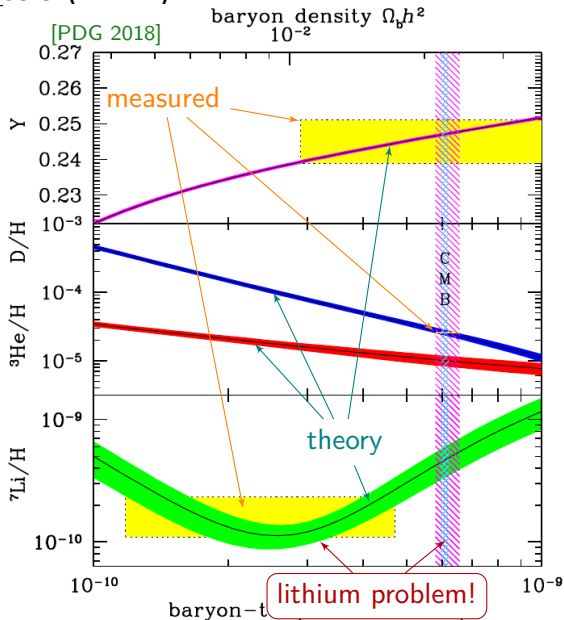
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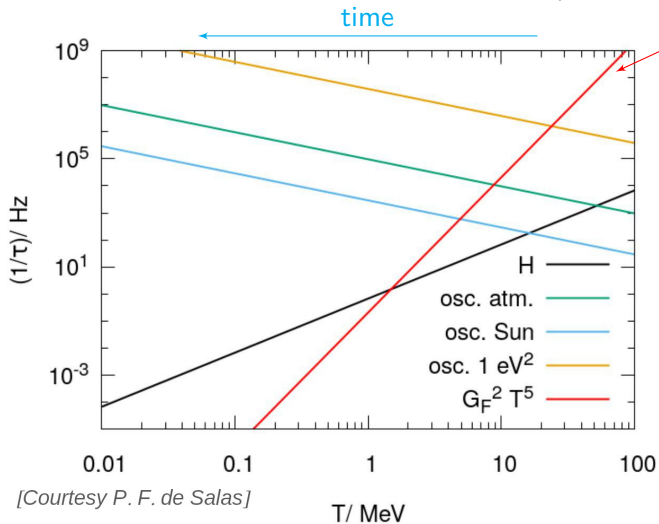
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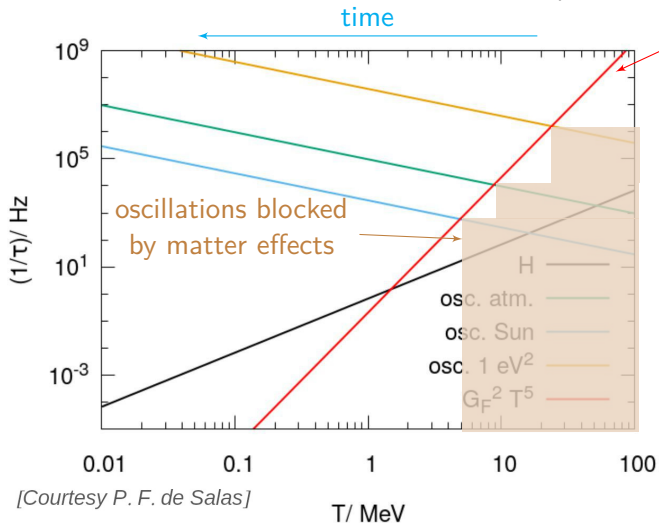
before BBN: neutrinos coupled to plasma ( $\nu_\alpha \bar{\nu}_\alpha \leftrightarrow e^+ e^-$ ,  $\nu e \leftrightarrow \nu e$ )



[Courtesy P. F. de Salas]

# Neutrinos in the early Universe

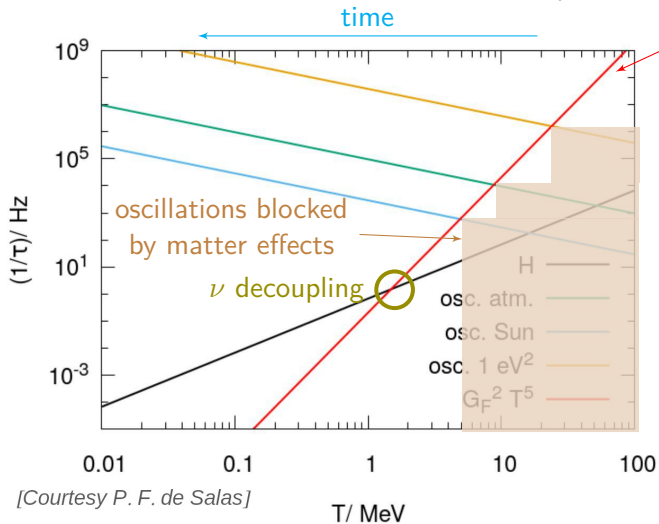
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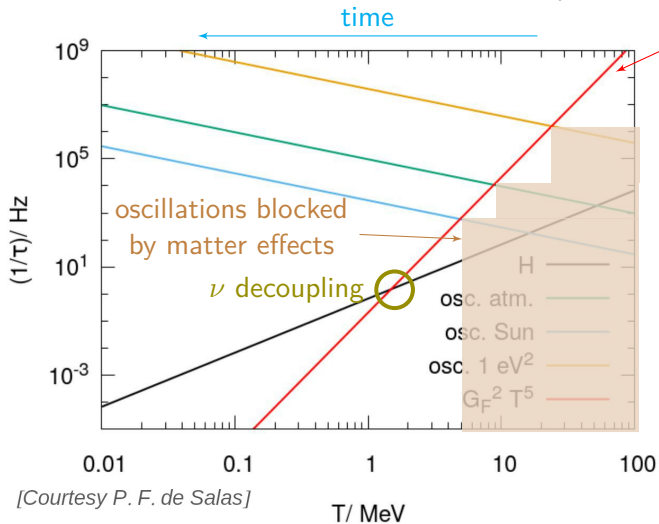


[Courtesy P. F. de Salas]

$\nu$  decouple mostly before  $e^+ e^- \rightarrow \gamma\gamma$  annihilation!

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$$T_\nu \simeq (4/11)^{1/3} T_\gamma$$

after  $e^+ e^- \rightarrow \gamma\gamma$

$f_\nu$ : frozen Fermi-Dirac distribution

Today:

$$T_{\nu,0} = 1.945 \text{ K} \simeq 1.676 \times 10^{-4} \text{ eV}$$

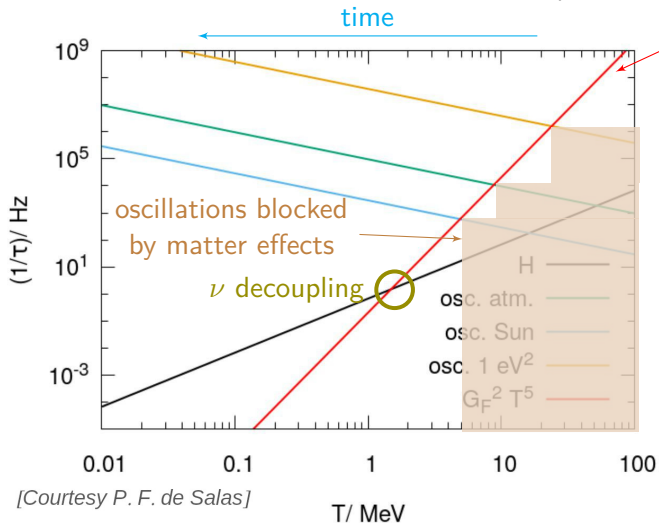
$$\langle E_\nu \rangle \simeq 3.1 T_{\nu,0} \simeq 5 \times 10^{-4} \text{ eV}$$

$$n_0 = n_{\nu,0} = n_{\bar{\nu},0} \simeq 56 \text{ cm}^{-3} \text{ per family}$$

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$\nu$  decouple mostly before  $e^+ e^- \rightarrow \gamma\gamma$  annihilation!  
 actually, the decoupling  $T$  is momentum dependent!

distortions to equilibrium  $f_\nu$ !

# $\nu$ oscillations in the early universe

[Bennett, SG+, JCAP 2021]  
[Sigl, Raffelt, 1993]

comoving coordinates:  $a = 1/T$   $x \equiv m_e a$   $y \equiv p a$   $z \equiv T_\gamma a$   $w \equiv T_\nu a$

density matrix:  $\varrho(x, y) = \begin{pmatrix} \varrho_{ee} \equiv f_{\nu_e} & \varrho_{e\mu} & \varrho_{e\tau} \\ \varrho_{\mu e} & \varrho_{\mu\mu} \equiv f_{\nu_\mu} & \varrho_{\mu\tau} \\ \varrho_{\tau e} & \varrho_{\tau\mu} & \varrho_{\tau\tau} \equiv f_{\nu_\tau} \end{pmatrix}$   
 $\propto \langle a_j^\dagger(p, t) a_i(p, t) \rangle$   
 off-diagonals to take into account coherency in the neutrino system

$$\varrho \text{ evolution from } x \text{ to } y: \quad x H \frac{d\varrho(y, x)}{dx} = -i a [\mathcal{H}_{\text{eff}}, \varrho] + b \mathcal{I}$$

$H$  Hubble factor  $\rightarrow$  expansion (depends on universe content)

effective Hamiltonian  $\mathcal{H}_{\text{eff}} = \frac{M_F}{2y} - \frac{2\sqrt{2}G_F y m_e^6}{x^6} \left( \frac{E_\ell + P_\ell}{m_W^2} + \frac{4}{3} \frac{E_\nu}{m_Z^2} \right)$

vacuum oscillations  $\leftarrow$   $\rightarrow$  matter effects

## $\mathcal{I}$ collision integrals

take into account  $\nu$ -e scattering and pair annihilation,  $\nu$ - $\nu$  interactions

2D integrals over momentum, take most of the computation time

$$\text{solve together with } z \text{ evolution, from } x \frac{d\rho(x)}{dx} = \rho - 3P$$

$\rho, P$  total energy density and pressure, also take into account FTQED corrections

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FORTRAN-EVOLVED PRIMORDIAL NEUTRINO OSCILLATIONS  
(FORTePIANO)

[https://bitbucket.org/ahep\\_cosmo/fortepiano\\_public](https://bitbucket.org/ahep_cosmo/fortepiano_public)

vacuum oscillations

matter effects

$\mathcal{I}$  collision integrals

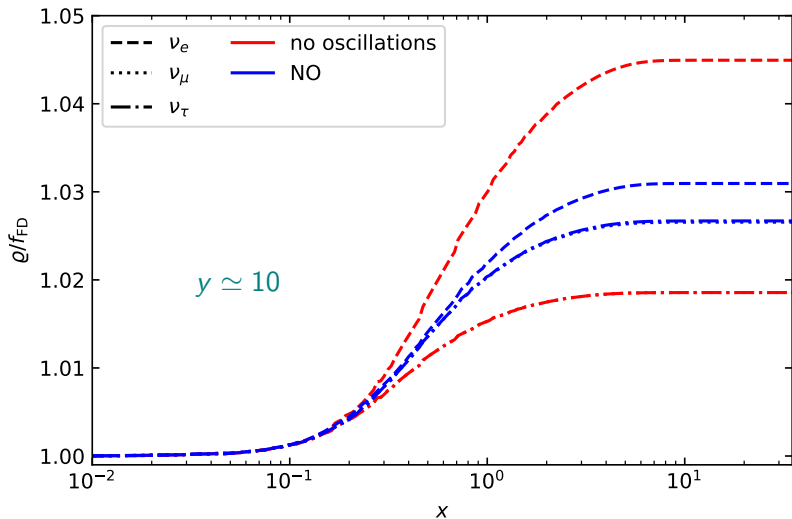
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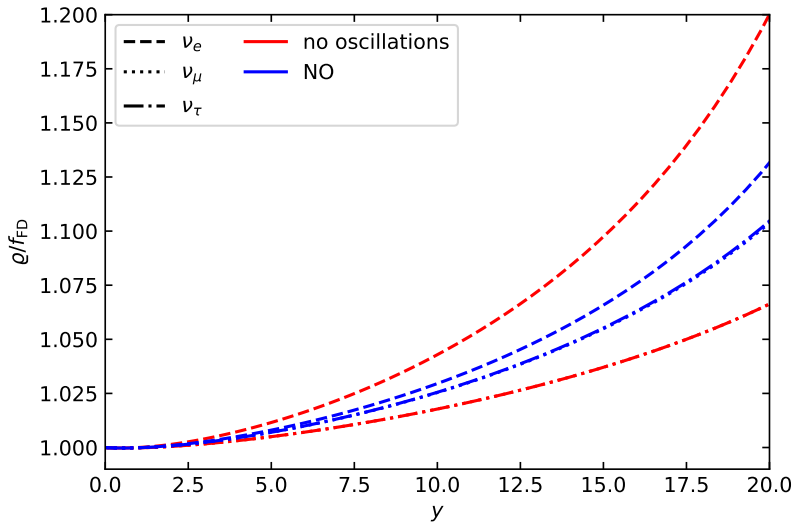
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Distortion of the momentum distribution ( $f_{\text{FD}}$ : Fermi-Dirac at equilibrium)



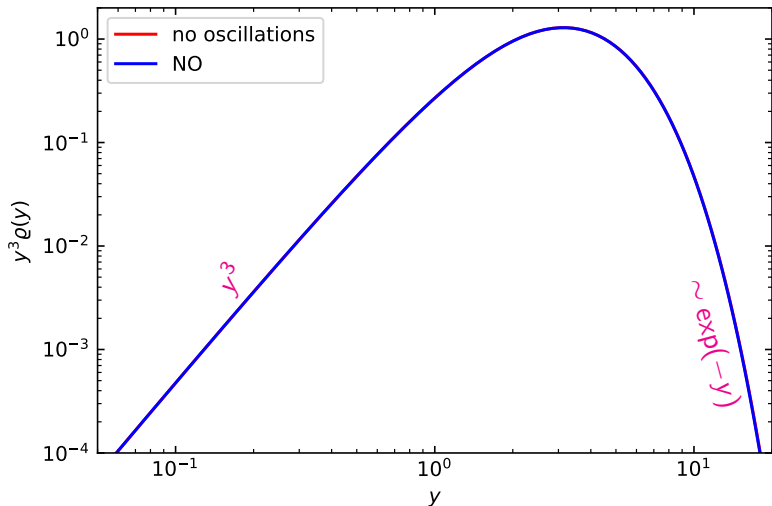
Distortion of the momentum distribution ( $f_{\text{FD}}$ : Fermi-Dirac at equilibrium)



# Neutrino momentum distribution and $N_{\text{eff}}$ [Bennett, SG+, JCAP 2021]

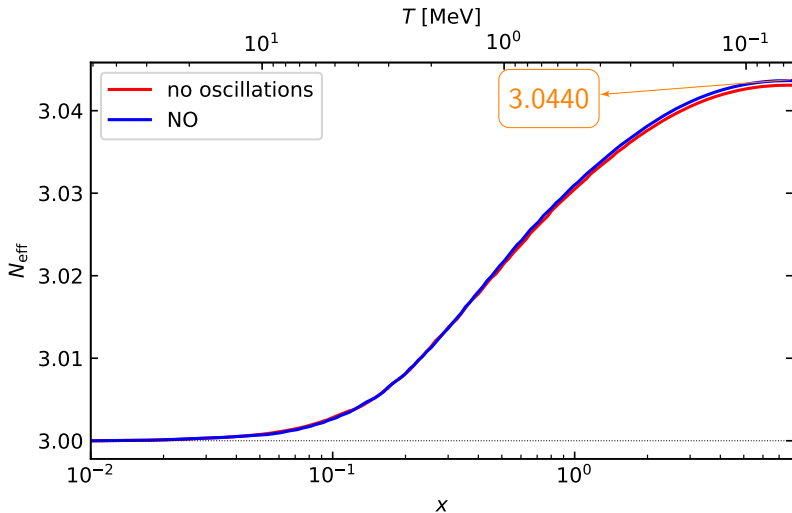
$$N_{\text{eff}}^{\text{final}} = \frac{8}{7} \left(\frac{11}{4}\right)^{4/3} \frac{\rho_\nu}{\rho_\gamma} = \frac{8}{7} \left(\frac{11}{4}\right)^{4/3} \frac{1}{\rho_\gamma} \sum_i g_i \int \frac{d^3 p}{(2\pi)^3} E(p) f_{\nu,i}(p)$$

$(11/4)^{1/3} = (T_\gamma/T_\nu)^{\text{fin}}$ 
 $\hookrightarrow \propto y^3 g_{ii}(y)$



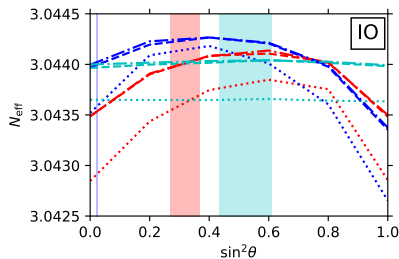
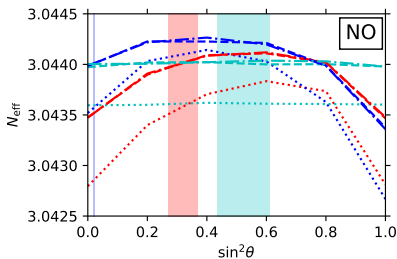
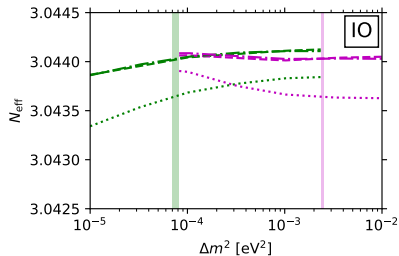
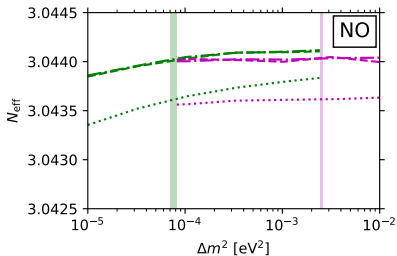
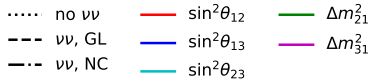
# Neutrino momentum distribution and $N_{\text{eff}}$

$$N_{\text{eff}}^{\text{any time}} = \frac{8}{7} \left( \frac{T_\gamma}{T_\nu} \right)^4 \frac{\rho_\nu}{\rho_\gamma} = \frac{8}{7} \left( \frac{T_\gamma}{T_\nu} \right)^4 \frac{1}{\rho_\gamma} \sum_i g_i \int \frac{d^3 p}{(2\pi)^3} E(p) f_{\nu,i}(p)$$



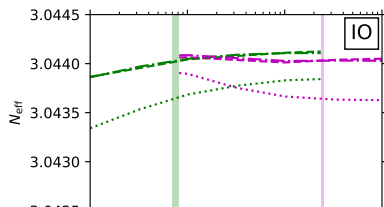
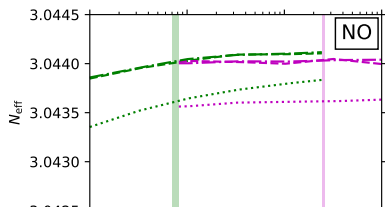
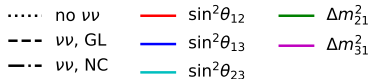
# Effect of neutrino oscillations

[Bennett, SG+, JCAP 2021]

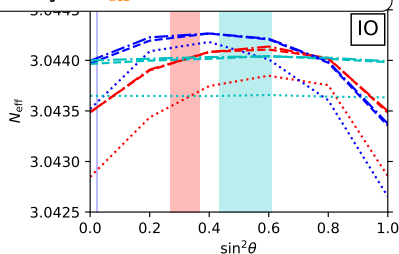
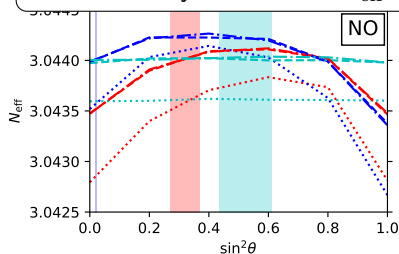


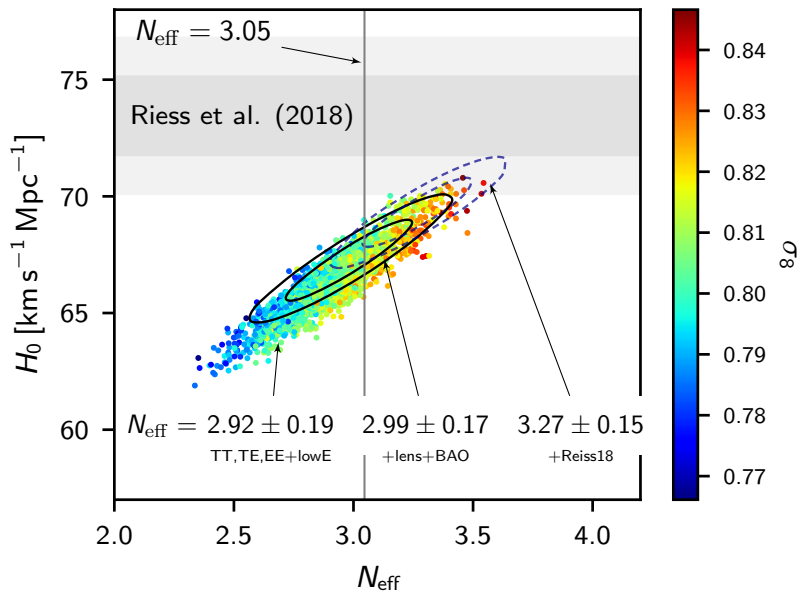
# Effect of neutrino oscillations

[Bennett, SG+, JCAP 2021]



within  $3\sigma$  ranges allowed by global fits [deSalas, SG+, JHEP 2021]  
 only  $\theta_{12}$  affects  $N_{\text{eff}}$ , at most by  $\delta N_{\text{eff}} \approx 10^{-4}$



$N_{\text{eff}}$  and CMB

## What is $N_{\text{eff}}$ ?

radiation density:

$$\rho_r = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma$$

$\rho_\gamma$  photon energy density,  $7/8$  for fermions,  $(4/11)^{4/3}$  due to photon reheating after neutrino decoupling

$$N_{\text{eff}}^\nu = \frac{8}{7} \left( \frac{11}{4} \right)^{4/3} \frac{\rho_\nu}{\rho_\gamma} = \frac{8}{7} \left( \frac{11}{4} \right)^{4/3} \frac{1}{\rho_\gamma} \sum_i g_i \int \frac{d^3 p}{(2\pi)^3} E(p) f_{\nu,i}(p)$$

It is a measurement of the energy density of **relativistic neutrinos!**

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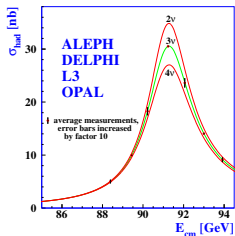
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Nothing to do with [LEP (2006)]

$$N_\nu^{(Z)} = 2.9840 \pm 0.0082$$



# What is $N_{\text{eff}}$ ?

radiation density:

$$\rho_r = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma$$

$\rho_\gamma$  photon energy density,  $7/8$  for fermions,  $(4/11)^{4/3}$  due to photon reheating after neutrino decoupling

$$N_{\text{eff}}^\nu = \frac{8}{7} \left( \frac{11}{4} \right)^{4/3} \frac{\rho_\nu}{\rho_\gamma} = \frac{8}{7} \left( \frac{11}{4} \right)^{4/3} \frac{1}{\rho_\gamma} \sum_i g_i \int \frac{d^3 p}{(2\pi)^3} E(p) f_{\nu,i}(p)$$

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Nothing to do with [LEP (2006)]

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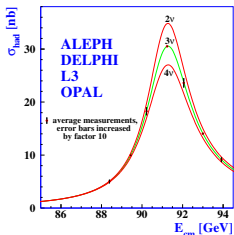
instantaneous decoupling:

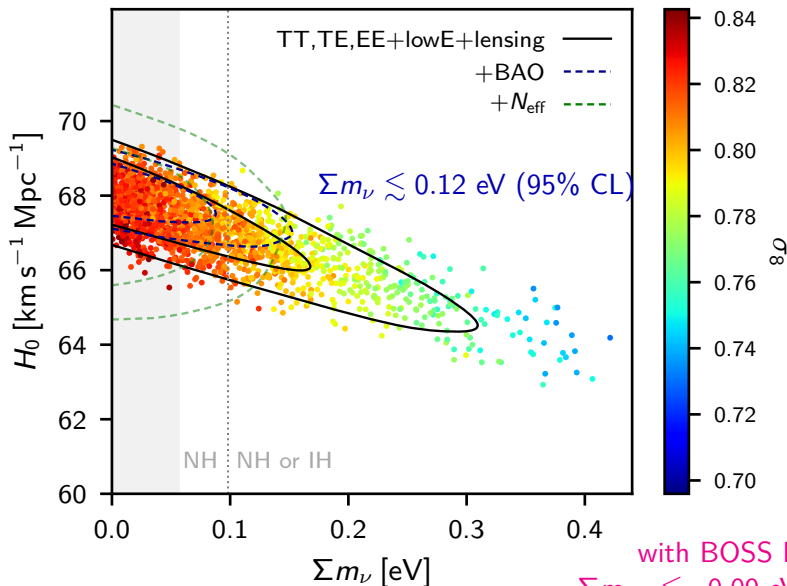
$$N_{\text{eff}}^\nu = 1 \text{ for each } \nu \text{ family}$$

non-instantaneous decoupling:

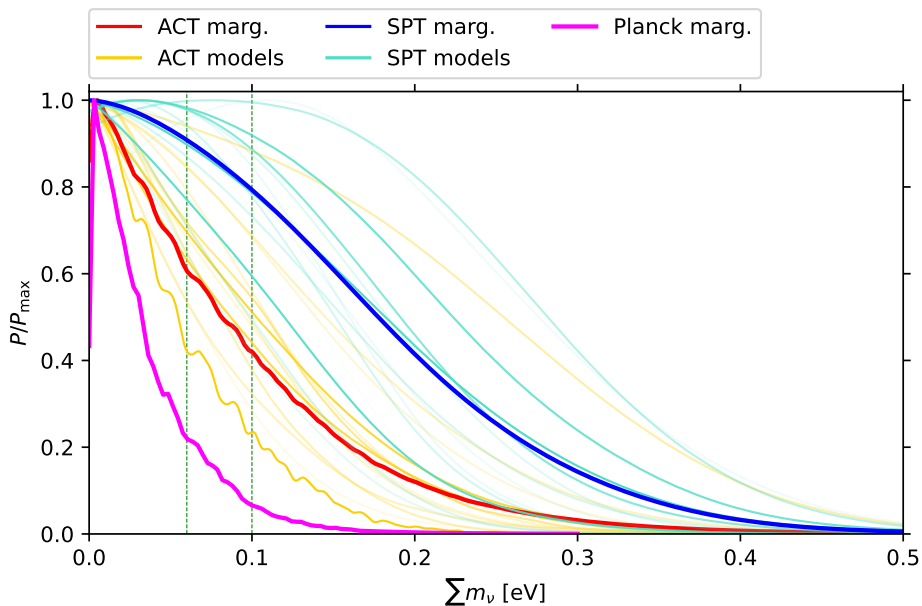
$N_{\text{eff}}^\nu > 3$  because of entropy transfer to photons and neutrinos when electrons become non-relativistic

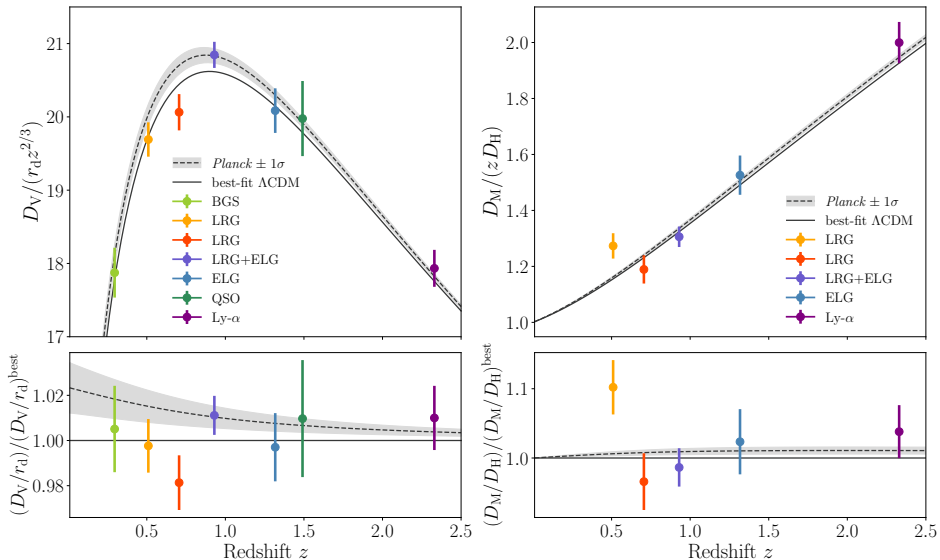
Non-standard physics? see later!

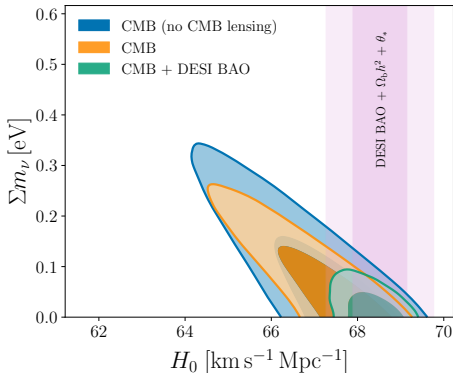
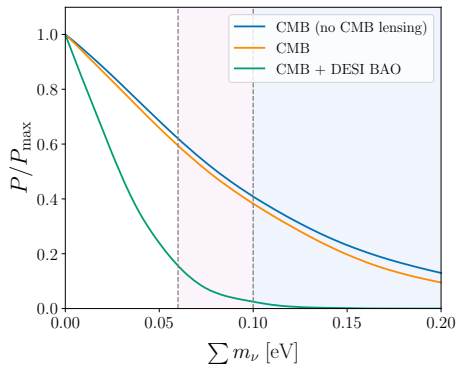


$\Sigma m_\nu$  and CMB

with BOSS DR16 BAO:  
 $\Sigma m_\nu \lesssim 0.09 \text{ eV (95\% CL)}$







$\sum m_\nu < 0.072$  eV (95%, DESI BAO+CMB)

close to disfavoring normal ordering minimum value

$$\sum m_\nu \sim 0.06 \text{ eV}$$

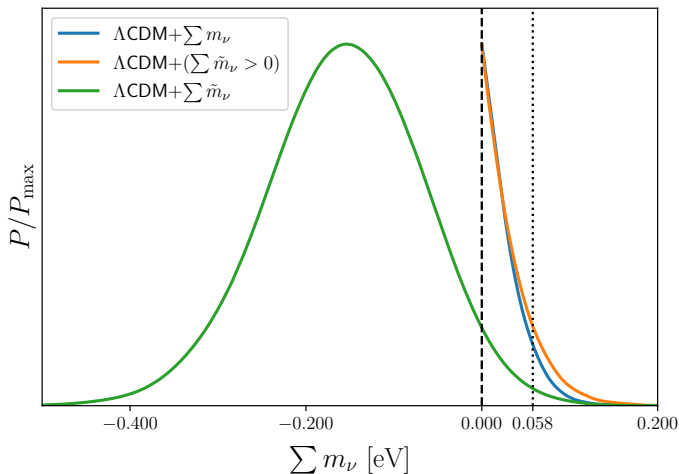
at 95%!

# Negative neutrino masses?

[Craig+, JHEP 09 (2024)]  
[Green+, PRD 111 (2025)]

“Effective  $\nu$  mass  $\Sigma \tilde{m}_\nu$ ” by extrapolating the effect of  $\Sigma m_\nu$  on lensing

“Negative neutrino mass”: increased matter clustering compared to a model with only massless neutrinos

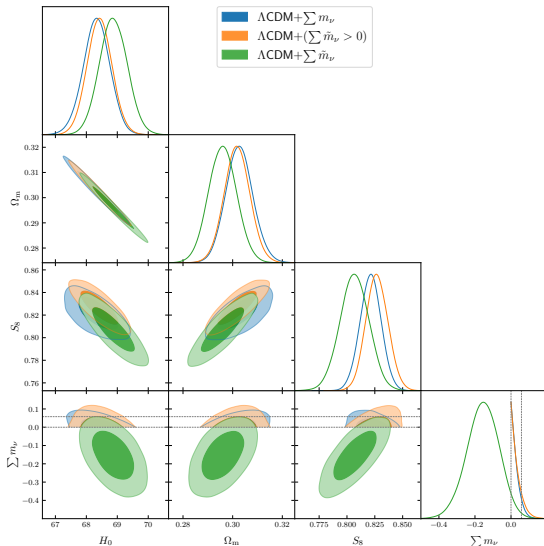


Planck 2018 CMB, ACT+Planck lensing, DESI BAO

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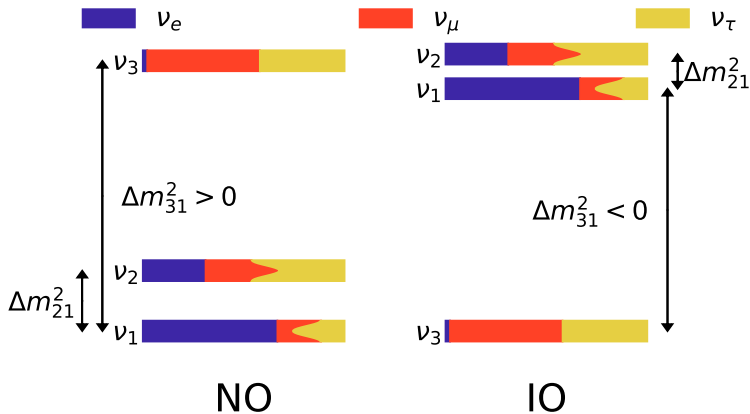
# What is $\Sigma m_\nu$ ?

normal ordering (NO):

$$m_2 \gtrsim 9 \text{ meV}, m_3 \gtrsim 50 \text{ meV}$$

inverted ordering (IO):

$$m_{1,2} \gtrsim 50 \text{ meV}$$



[Valencia global fit]

## What is $\Sigma m_\nu$ ?

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$$m_{1,2} \gtrsim 50 \text{ meV}$$

relic neutrinos have a Fermi-Dirac distribution with  $T_\nu \approx \mathcal{O}(0.1) \text{ meV}$ !

many relic neutrinos are non-relativistic today!

$$\text{energy density } \rho_{\nu, \text{non-rel}} = \sum_i m_i n_i$$

$$\text{fractional energy density } \omega_\nu = \Omega_\nu h^2 = \frac{\sum_i m_i n_i}{\rho_{\text{cr}}} = \frac{\Sigma m_\nu}{94.1 \text{ eV}}$$

Background measurements are sensitive to  $\omega_\nu$ , not  $\Sigma m_\nu$ !

“Cosmological”  $\Sigma m_\nu$  measures the energy density of non-relativistic  $\nu$ s

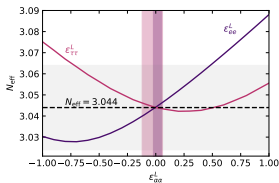
Note: free-streaming scale directly depends on  $m_\nu$ :

$$\lambda_{\text{FS}} \propto v_{\text{th}}/H \propto \langle p \rangle / (m_\nu H) \propto \sim 3T_\nu / (m_\nu H)$$



$$N_{\text{eff}} \simeq 3?$$

Neutrino physics can have small impacts on  $N_{\text{eff}}$ !



e.g.:

Non-Standard Interactions (NSI) [PLB 820 (2021)]

# Non-standard neutrino-electron interactions

Can neutrinos have interactions beyond the SM ones?

e.g.:  $\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{NSIe}}$ , with  $\mathcal{L}_{\text{NSIe}} \propto G_F \sum_{\alpha,\beta} \epsilon_{\alpha\beta}^{L,R} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{e} \gamma_\mu P_{L,R} e)$   
see e.g. [Farzan+, 2018]

coupling strength governed by the  $\epsilon_{\alpha\beta}^{L,R}$  coefficients ( $\alpha = e, \mu, \tau$ )

new interactions **affect all phenomena** involving neutrinos and electrons  
including neutrino decoupling:

collision terms

$$G_{\text{SM}}^L = \text{diag}(g_L, \tilde{g}_L, \tilde{g}_L)$$

$$G_{\text{SM}}^R = \text{diag}(g_R, g_R, g_R)$$

$g_R = \sin^2 \theta_W$ ,  $\tilde{g}_L = g_R + 1/2$ ,  $\tilde{g}_L = g_R - 1/2$

$$G^{L,R} = G_{\text{SM}}^{L,R} + \begin{pmatrix} \epsilon_{ee}^{L,R} & \epsilon_{e\mu}^{L,R} & \epsilon_{e\tau}^{L,R} & \cdots \\ \epsilon_{e\mu}^{L,R} & \epsilon_{\mu\mu}^{L,R} & \epsilon_{\mu\tau}^{L,R} & \cdots \\ \epsilon_{e\tau}^{L,R} & \epsilon_{\mu\tau}^{L,R} & \epsilon_{\tau\tau}^{L,R} & \cdots \\ \vdots & & & \ddots \end{pmatrix}$$

matter effects in oscillations  
(subdominant!)

$$\mathcal{H}_{\text{eff,SM}} \supset k \cdot \text{diag}(\rho_e + P_e, 0, 0)$$

$$\mathcal{H}_{\text{eff}} \supset k(\rho_e + P_e) \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau} & \epsilon_{\mu\tau} & \epsilon_{\tau\tau} \end{pmatrix}$$

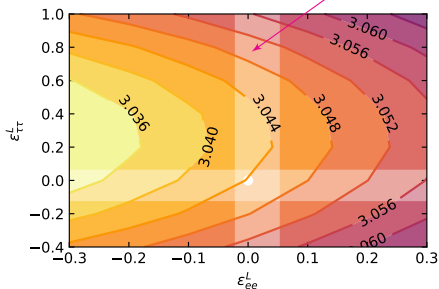
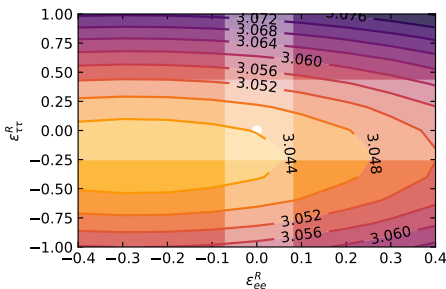
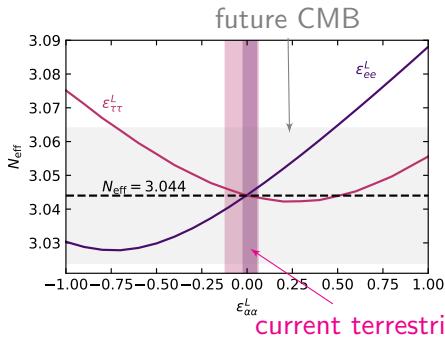
$$\text{with } \epsilon_{\alpha\beta} = \epsilon_{\alpha\beta}^L + \epsilon_{\alpha\beta}^R$$

# NSI effects on $N_{\text{eff}}$

$$G^{L,R} = G_{SM}^{L,R} + \begin{pmatrix} \epsilon_{ee}^{L,R} & \epsilon_{e\mu}^{L,R} & \epsilon_{e\tau}^{L,R} & \dots \\ \epsilon_{e\mu}^{L,R} & \epsilon_{\mu\mu}^{L,R} & \epsilon_{\mu\tau}^{L,R} & \dots \\ \epsilon_{e\tau}^{L,R} & \epsilon_{\mu\tau}^{L,R} & \epsilon_{\tau\tau}^{L,R} & \dots \\ \vdots & & & \ddots \end{pmatrix}$$

e.g.:

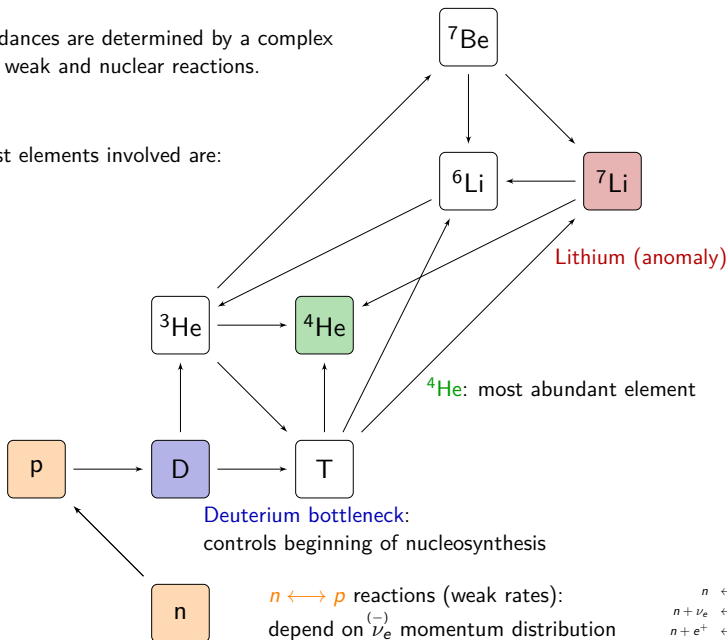
$$\begin{aligned} G_{ee}^L &\rightarrow 0.727 + \epsilon_{ee}^L \\ G_{\tau\tau}^L &\rightarrow -0.273 + \epsilon_{\tau\tau}^L \\ G_{\alpha\alpha}^R &\rightarrow 0.233 + \epsilon_{\alpha\alpha}^R \end{aligned}$$



# Reactions governing BBN

BBN abundances are determined by a complex network of weak and nuclear reactions.

The lightest elements involved are:



# NSI effects on BBN

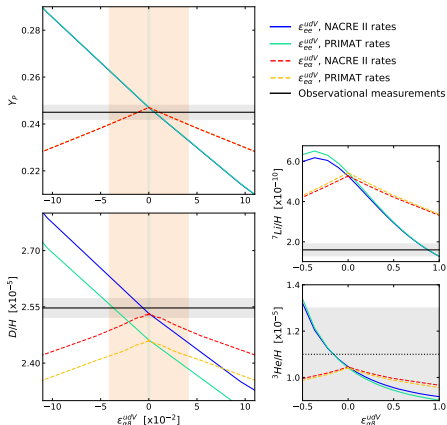
NSI with electrons, such as  $\mathcal{L}_{\text{NSIe}}^{\text{NC}} \propto \sum \epsilon_{\alpha\beta}^{L,R} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{e} \gamma_\mu P_{L,R} e)$ ,  
 have secondary effect on BBN rates because there are no  $\bar{\nu} e$  interactions!

WR depend on  $n \leftrightarrow p$  processes, for which it is more relevant

$$\mathcal{L}_{\text{NSIq}}^{\text{CC}} \propto G_F V_{ud} \sum_{\alpha} \epsilon_{e\alpha}^{udV} (\bar{u} \gamma^\mu P_L d) (\bar{e} \gamma_\mu P_{L,R} \nu_\alpha)!$$

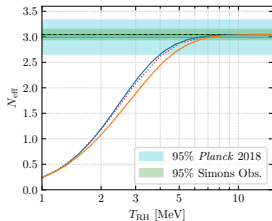
Effect of  $\epsilon_{e\alpha}^{udV}$   
 on BBN abundances  
 can be exploited  
 to derive constraints:

Bounds are comparable and  
 complementary to the ones  
 from terrestrial experiments!





$$N_{\text{eff}} < 3?$$



e.g. low-temperature reheating scenarios

[PRD 92 (2015) 123534], [arxiv:2501.01369]

## Scenarios with low reheating temperature

Reheating: phase ending inflation

during inflation, the inflaton (non-rel. scalar) dominates the energy density

during reheating: inflaton decays into standard model particles

⇒ photons, electrons, ... are populated directly

radiation domination begins after reheating

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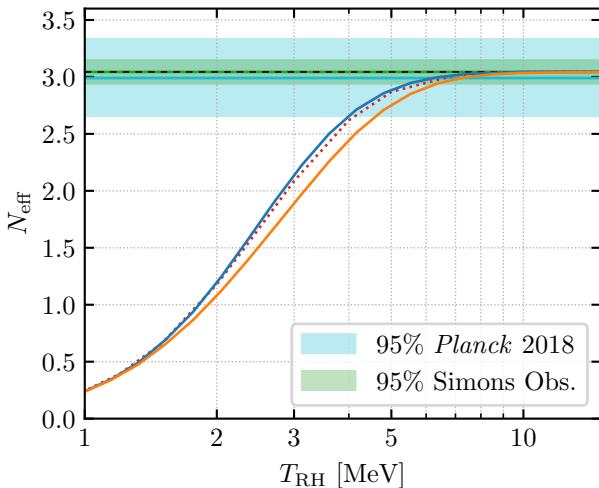
**Low reheating temperature:** when reheating occurs at  $T_{\text{rh}} \lesssim 20$  MeV

notice: if  $T_{\text{rh}} \lesssim 3$  MeV, BBN is broken!

3 neutrino oscillations start to be affected when  $T_{\text{rh}} \lesssim 8$  MeV

# $N_{\text{eff}}$ with low reheating

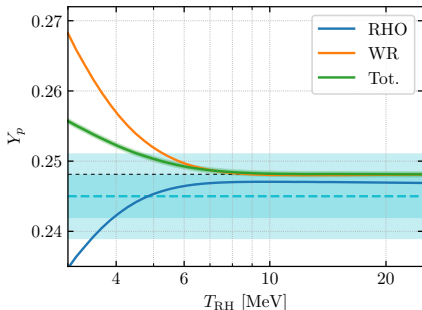
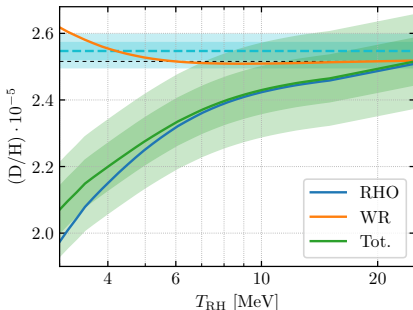
$N_{\text{eff}}$  as a function of  $T_{\text{rh}}$ :



Planck constraint:  $N_{\text{eff}} = 2.92^{+0.36}_{-0.37}$  (95%, TT,TE,EE+lowE)

# BBN and low reheating

Light element abundances depend on  $T_{\text{rh}}$ :



■ **RHO**: total energy density,  
expansion rate



neutrino energy density,  $N_{\text{eff}}$

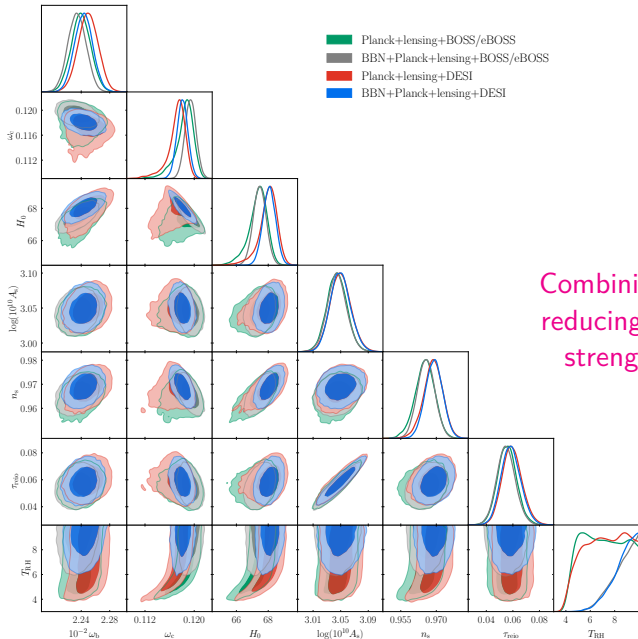
■ **WR**: weak rates  
( $n \leftrightarrow p, \nu_e^{(-)}$  interactions)



$\nu_e^{(-)}$  momentum distribution

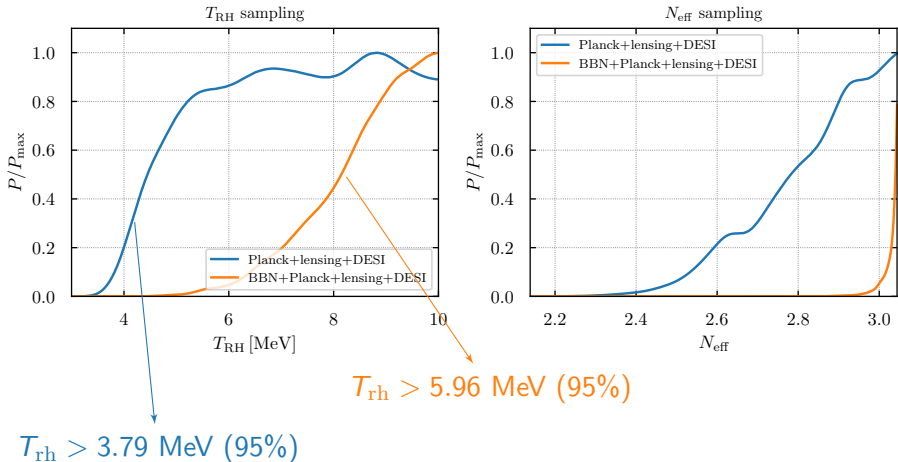
Both effects are important to get Helium right!

# Constraints on low reheating scenarios



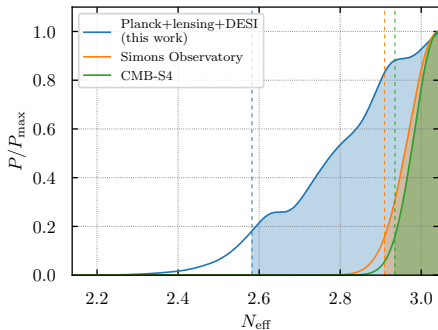
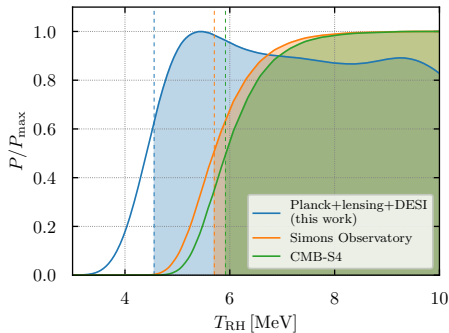
Combining probes helps in reducing degeneracies and strengthening bounds!

# Constraints on low reheating scenarios



BBN occurs at **earlier time than CMB** and is more sensitive to  $N_{eff}$  (RHO) and  $\nu_e^{(-)}$  momentum distribution functions (WR) as a function of  $T_{rh}$ !

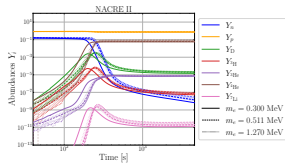
# Constraints on low reheating scenarios



Greater sensitivity will come with future CMB probes  
(more precise in determining  $N_{\text{eff}}$ )

Future CMB alone will reach the precision of  
current BBN+CMB (Planck)+BAO (DESI) observations

**E**  $N_{\text{eff}} > 3?$



e.g. non-standard electron mass [[arxiv:2602.05720](https://arxiv.org/abs/2602.05720)]

# The electron mass $m_e$

From [PDG 2024]:

Citation: S. Navas et al. (Particle Data Group), Phys. Rev. D **110**, 030001 (2024) and 2025 update

## LEPTONS

**e**

$$J = \frac{1}{2}$$

$$\text{Mass } m = (548.579909065 \pm 0.000000016) \times 10^{-6} \text{ u}$$

$$\text{Mass } m = 0.51099895000 \pm 0.00000000015 \text{ MeV}$$

$$|m_{e^+} - m_{e^-}|/m < 8 \times 10^{-9}, \text{ CL} = 90\%$$

$$|q_{e^+} + q_{e^-}|/e < 4 \times 10^{-8}$$

Magnetic moment anomaly

$$(g-2)/2 = (1159.65218062 \pm 0.00000012) \times 10^{-6}$$

$$(g_{e^+} - g_{e^-}) / g_{\text{average}} = (-0.5 \pm 2.1) \times 10^{-12}$$

$$\text{Electric dipole moment } d < 0.041 \times 10^{-28} \text{ e cm, CL} = 90\%$$

$$\text{Mean life } \tau > 6.6 \times 10^{28} \text{ yr, CL} = 90\% \text{ [a]}$$

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today!

$$|m_{e^+} - m_{e^-}|/m < 8 \times 10^{-9}, \text{ CL} = 90\%$$

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was it the same at early times?

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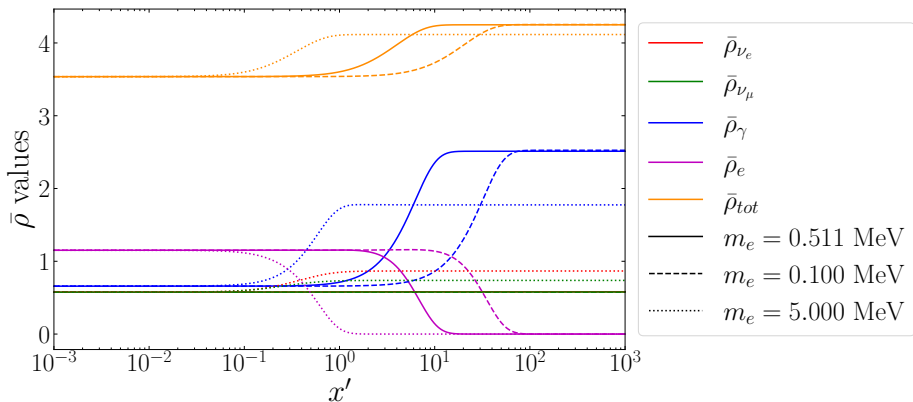
$$\text{Mean life } \tau > 6.6 \times 10^{28} \text{ yr, CL} = 90\% [a]$$

$m_e$  and  $N_{\text{eff}}$ 

In the early Universe, **neutrino decoupling** occurs at  $T \simeq 1 - 2 \text{ MeV}$

**Electron-positron annihilation** occurs slightly later if  $m_e = 0.511 \text{ MeV}$

Decoupled neutrinos **do not receive** energy from  $e^+e^-$  annihilation, which **only goes to photons**

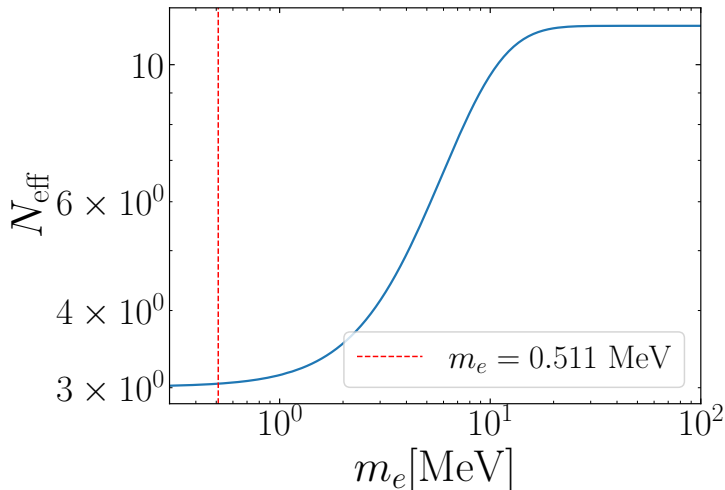


Energy density of **neutrinos** relative to **photons** depends on  $m_e$ !

## $m_e$ and $N_{\text{eff}}$

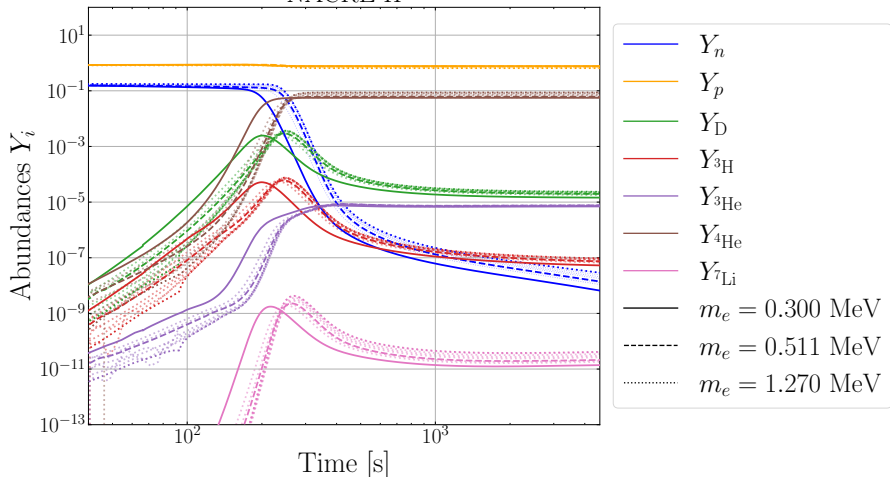
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but  $N_{\text{eff}}$  is the ratio!



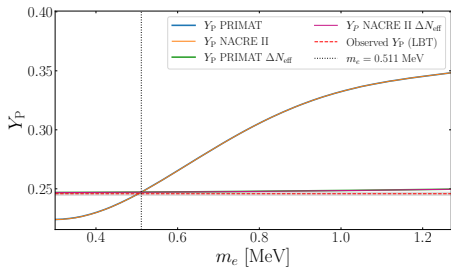
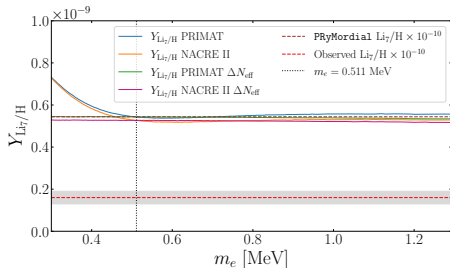
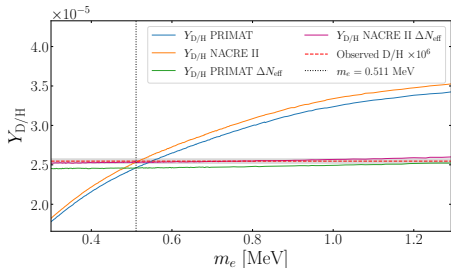
Different  $m_e$  shifts kinematics of neutron  $\beta$ -decay and expansion rate!

NACRE II



NACRE II (shown) and PRIMAT: [alternative nuclear reaction networks](#)

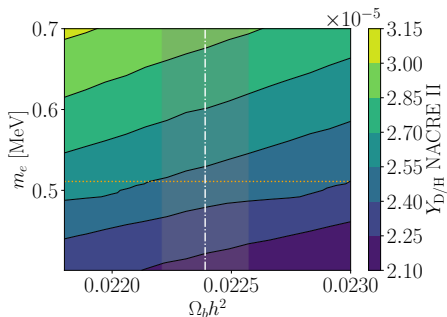
Main abundances as a function of  $m_e$ :



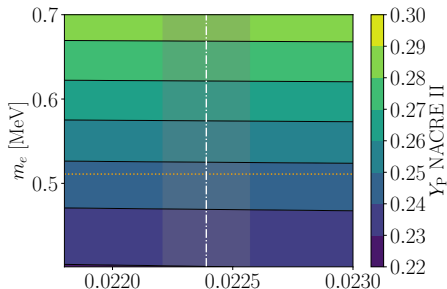
■ **Lithium problem!** unsolved

■ **Expansion** effect ( $\Delta N_{\text{eff}}$ )  
is marginal wrt weak rates

■ **PRIMAT** vs **NACRE II**  
nuclear reaction network give  
differences in Deuterium!

$m_e$  and BBN

Deuterium abundance also depends on baryon density!



Helium abundance does not!

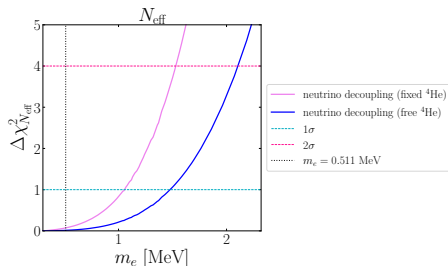
# Which constraints do we get on $m_e$ ?

## CMB:

$$N_{\text{eff}} = 2.99 \pm 0.17 \text{ (fixed } Y_p)$$

$$N_{\text{eff}} = 2.97 \pm 0.29 \text{ (free } Y_p)$$

[Planck Collaboration, 2018]



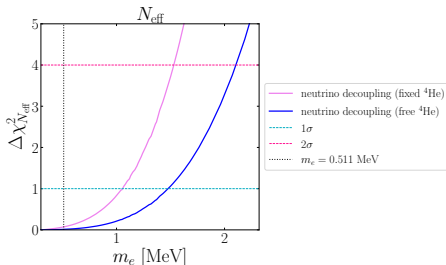
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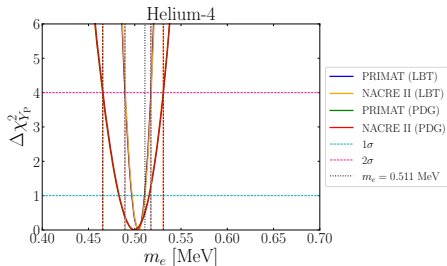
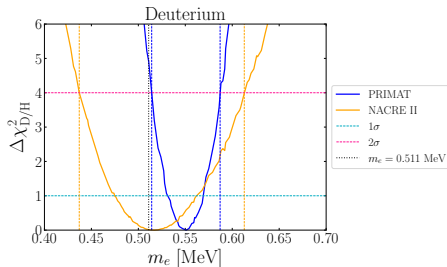
$$N_{\text{eff}} = 2.97 \pm 0.29 \text{ (free } Y_p)$$

[Planck Collaboration, 2018]



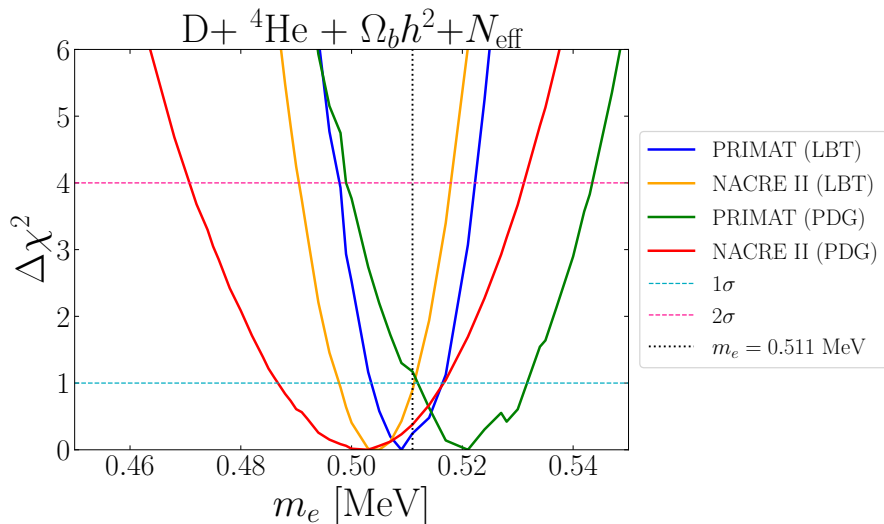
$N_{\text{eff}}$  irrelevant wrt BBN

## Deuterium and Helium:



# Which constraints do we get on $m_e$ ?

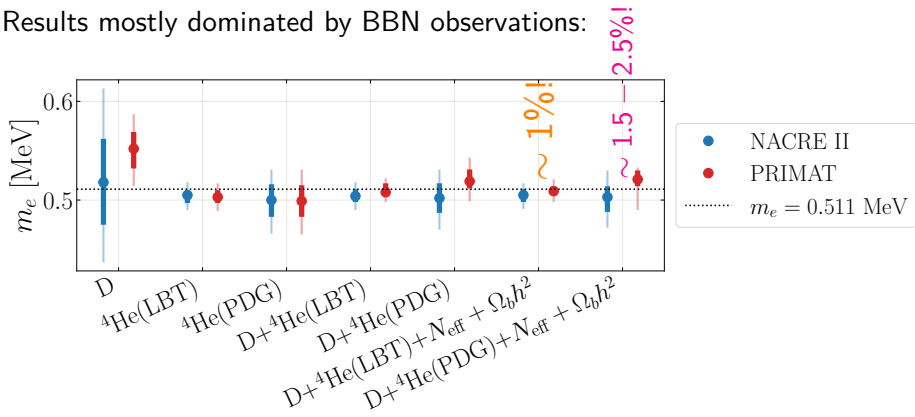
Combination:



$\Omega_b h^2$ : marginalization over baryon density from **CMB**

# Constraints on $m_e$ - summary

Results mostly dominated by BBN observations:



- LBT:  $Y_P = 0.2458 \pm 0.0013$  (most precise) [LBT, arxiv:2601.22238];
- PDG:  $Y_P = 0.245 \pm 0.003$  (conservative) [PDG 2024];

1 – 2.5% precision on  $m_e$  at earliest epoch ever!

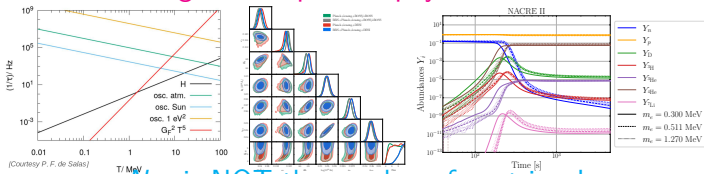


## Conclusions

# What did we learn from $\nu$ decoupling and BBN?

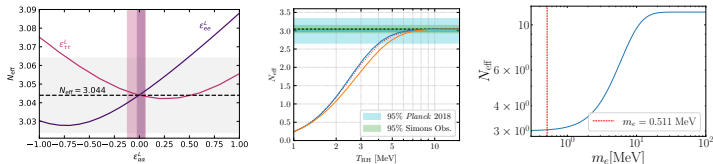
C

All cosmological and particle physics models matter!



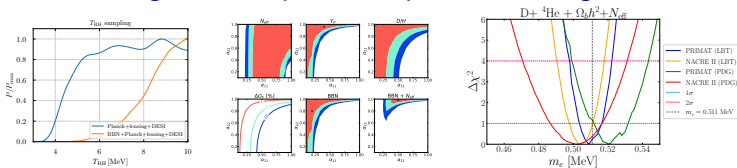
N

$N_{\text{eff}}$  is NOT the number of neutrinos!



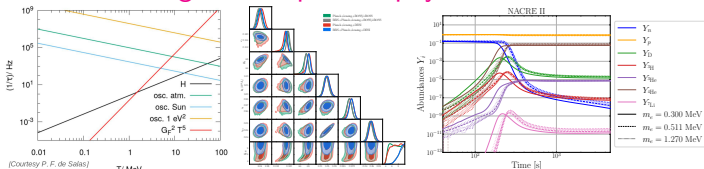
M

Combining different probes helps to break degeneracies!

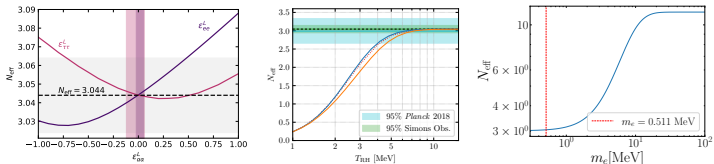


# What did we learn from $\nu$ decoupling and BBN?

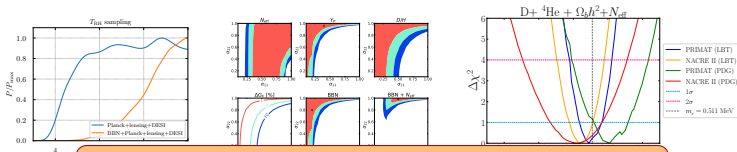
C All cosmological and particle physics models matter!



N  $N_{\text{eff}}$  is NOT the number of neutrinos!



M Combining different probes helps to break degeneracies!



Thanks for your attention!