



UNIVERSITÀ  
DI TORINO



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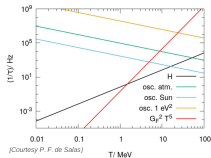
## Neutrino non-standard scenarios in cosmology

XVII CPAN Days, ADEIT Valencia, 20/11/2025

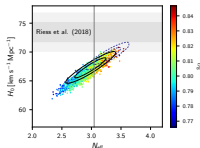
## E

# Neutrinos in the Early Universe

Based on

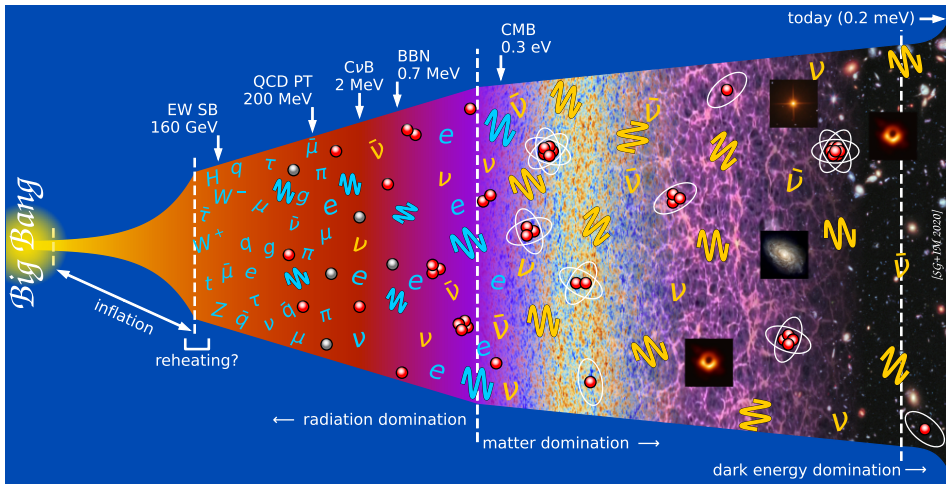


JCAP 04 (2021) 073

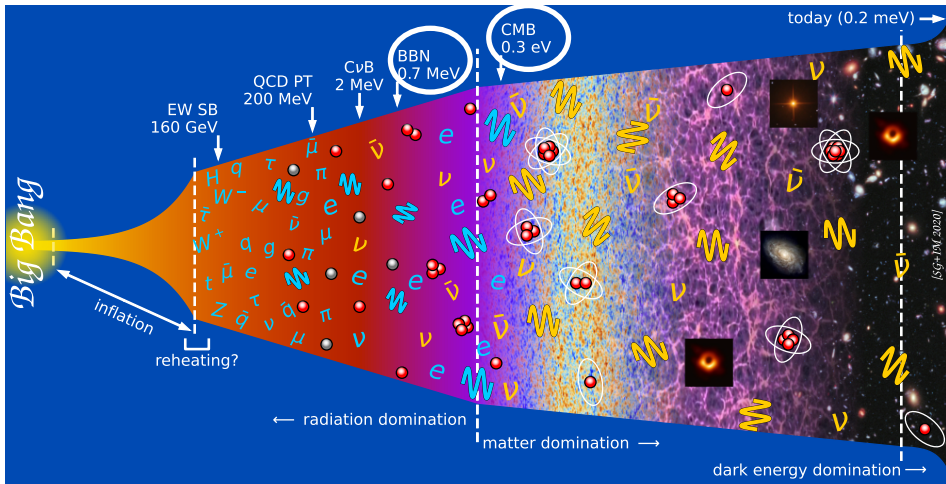


Planck 2018

# History of the universe



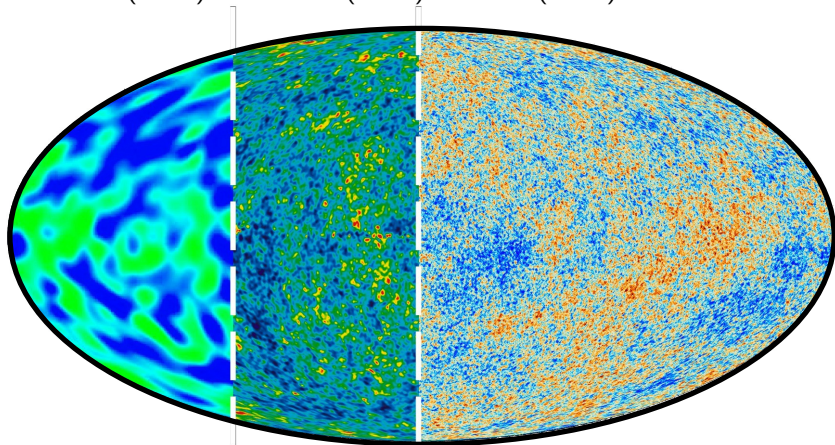
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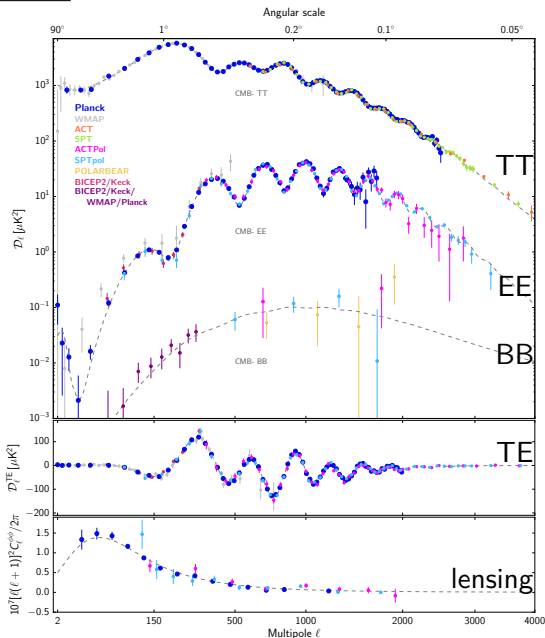
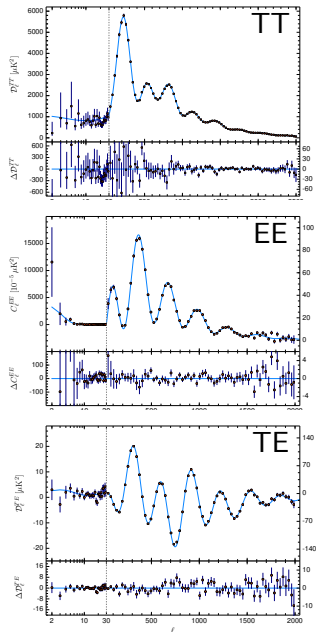


# The oldest picture of the Universe

The Cosmic Microwave Background, generated at  $t \simeq 4 \times 10^5$  years

COBE (1992)    WMAP (2003)    Planck (2013)





# Big Bang Nucleosynthesis (BBN)

BBN: production of light nuclei at  $t \sim 1\text{s}$  to  $t \sim \mathcal{O}(10^2)\text{s}$

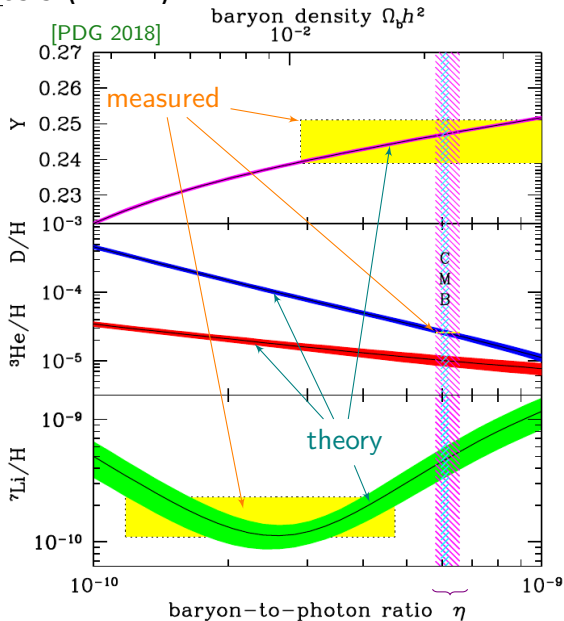
temperature  $T_{fr} \simeq 1\text{ MeV}$   
from nucleon freeze-out

much earlier than CMB!

strong probe for physics  
before the CMB

e.g. neutrinos!

$\nu$  affect  
universe expansion  
and  
reaction rates ( $\nu_e/\bar{\nu}_e$ )  
at BBN time...



BBN concordance

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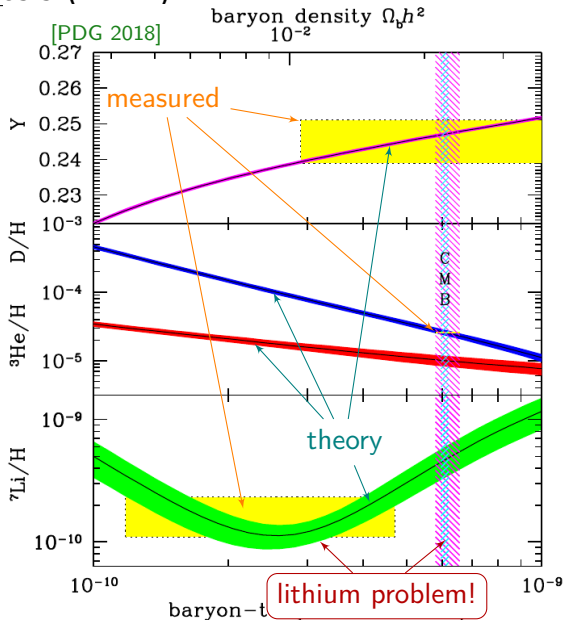
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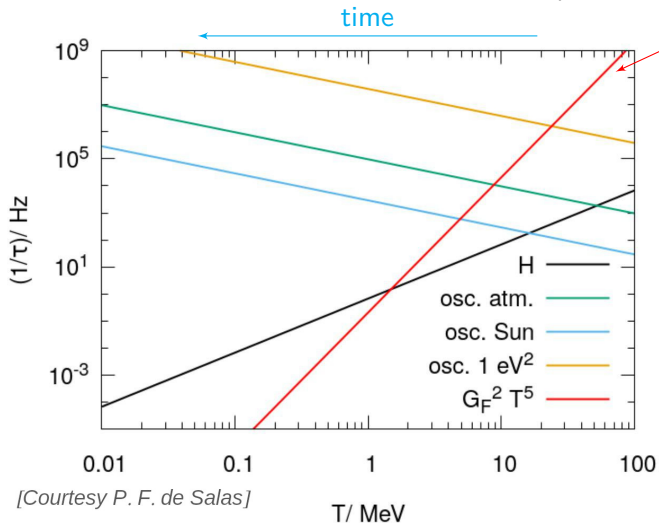


BBN concordance



# Neutrinos in the early Universe

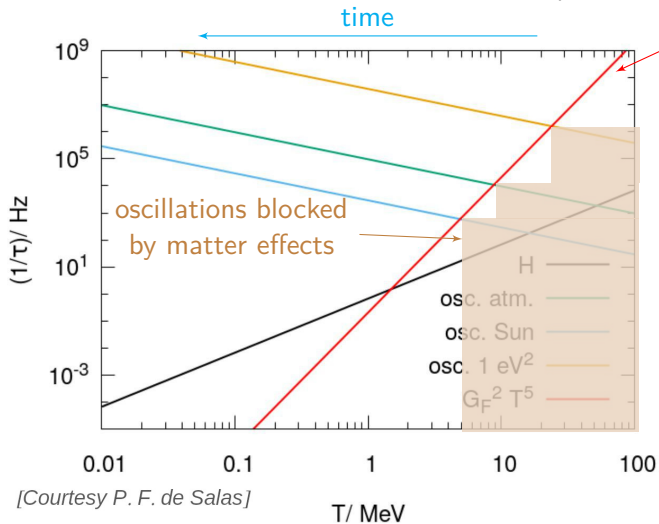
before BBN: neutrinos coupled to plasma ( $\nu_\alpha \bar{\nu}_\alpha \leftrightarrow e^+ e^-$ ,  $\nu e \leftrightarrow \nu e$ )



[Courtesy P. F. de Salas]

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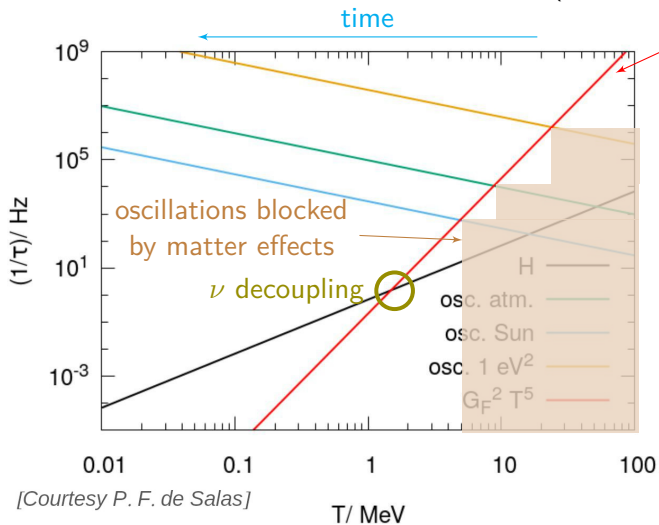
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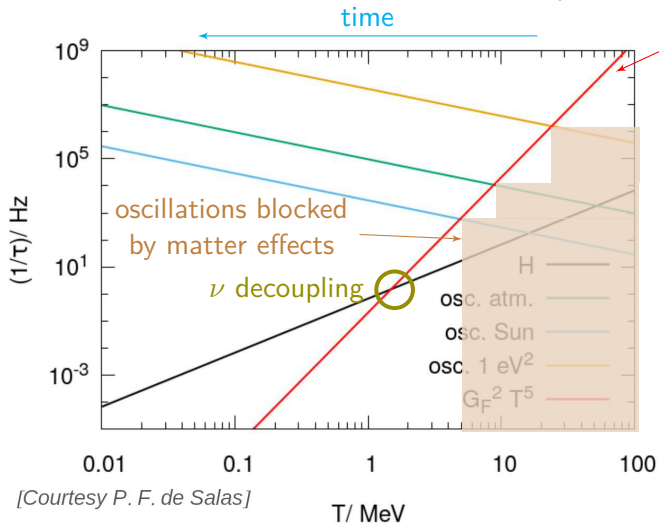
[Courtesy P. F. de Salas]

T/ MeV

$\nu$  decouple mostly before  $e^+ e^- \rightarrow \gamma\gamma$  annihilation!

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[Courtesy P. F. de Salas]

$$T_\nu \simeq (4/11)^{1/3} T_\gamma$$

after  $e^+ e^- \rightarrow \gamma\gamma$

$f_\nu$ : frozen Fermi-Dirac distribution

Today:

$$T_{\nu,0} = 1.945 \text{ K} \simeq 1.676 \times 10^{-4} \text{ eV}$$

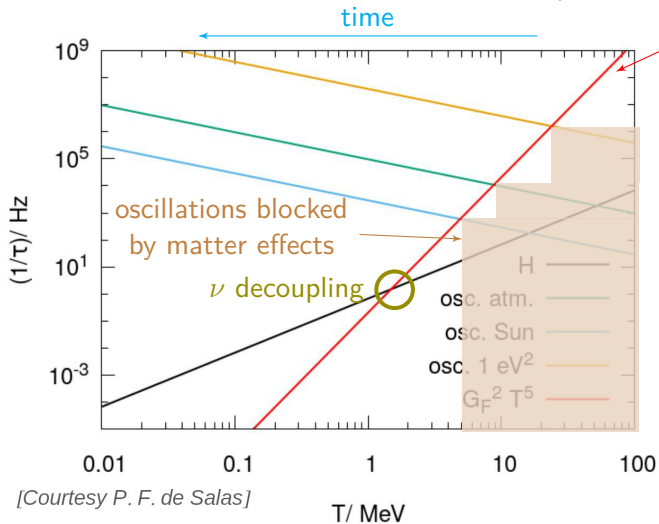
$$\langle E_\nu \rangle \simeq 3.1 T_{\nu,0} \simeq 5 \times 10^{-4} \text{ eV}$$

$$n_0 = n_{\nu,0} = n_{\bar{\nu},0} \simeq 56 \text{ cm}^{-3} \text{ per family}$$

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$\nu$  decouple mostly before  $e^+ e^- \rightarrow \gamma\gamma$  annihilation!  
 actually, the decoupling  $T$  is momentum dependent!

distortions to equilibrium  $f_\nu$ !

# $\nu$ oscillations in the early universe

[Bennett, SG+, JCAP 2021]  
[Sigl, Raffelt, 1993]

comoving coordinates:  $a = 1/T$   $x \equiv m_e a$   $y \equiv p a$   $z \equiv T_\gamma a$   $w \equiv T_\nu a$

density matrix:  $\varrho(x, y) = \begin{pmatrix} \varrho_{ee} \equiv f_{\nu_e} & \varrho_{e\mu} & \varrho_{e\tau} \\ \varrho_{\mu e} & \varrho_{\mu\mu} \equiv f_{\nu_\mu} & \varrho_{\mu\tau} \\ \varrho_{\tau e} & \varrho_{\tau\mu} & \varrho_{\tau\tau} \equiv f_{\nu_\tau} \end{pmatrix}$   
 $\propto \langle a_j^\dagger(p, t) a_i(p, t) \rangle$   
off-diagonals to take into account coherency in the neutrino system

$$\varrho \text{ evolution from } x \text{ to } y: \quad x H \frac{d\varrho(y, x)}{dx} = -i a [\mathcal{H}_{\text{eff}}, \varrho] + b \mathcal{I}$$

$H$  Hubble factor  $\rightarrow$  expansion (depends on universe content)

$$\text{effective Hamiltonian } \mathcal{H}_{\text{eff}} = \frac{M_{\text{F}}}{2y} - \frac{2\sqrt{2}G_{\text{F}}ym_e^6}{x^6} \left( \frac{E_\ell + P_\ell}{m_W^2} + \frac{4}{3} \frac{E_\nu}{m_Z^2} \right)$$

vacuum oscillations  $\longleftarrow$   $\longrightarrow$  matter effects

$\mathcal{I}$  collision integrals

take into account  $\nu$ -e scattering and pair annihilation,  $\nu$ - $\nu$  interactions

2D integrals over momentum, take most of the computation time

$$\text{solve together with } z \text{ evolution, from } x \frac{d\rho(x)}{dx} = \rho - 3P$$

$\rho, P$  total energy density and pressure, also take into account FTQED corrections

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FORTRAN-EVOLVED PRIMORDIAL NEUTRINO OSCILLATIONS  
(FORTePIANO)

[https://bitbucket.org/ahep\\_cosmo/fortepiano\\_public](https://bitbucket.org/ahep_cosmo/fortepiano_public)

vacuum oscillations



matter effects

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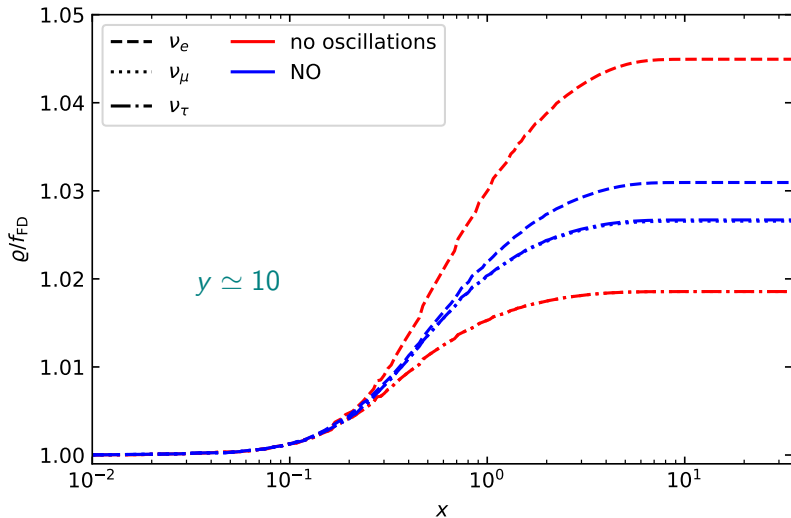
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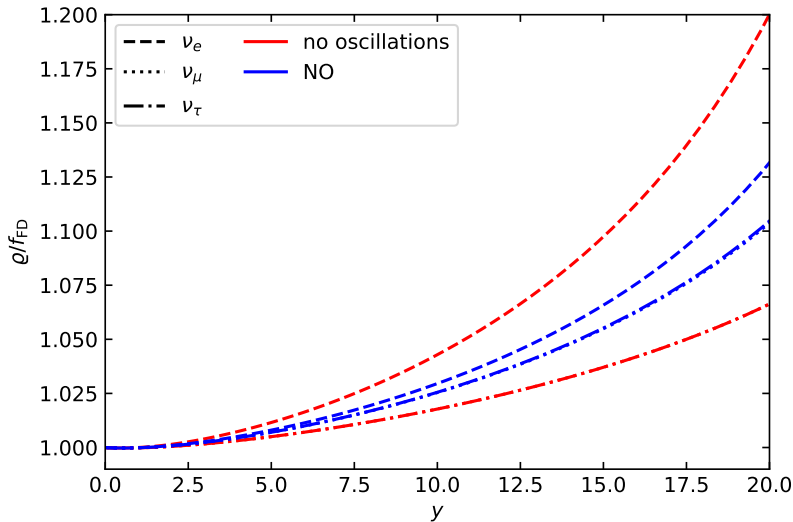
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Distortion of the momentum distribution ( $f_{\text{FD}}$ : Fermi-Dirac at equilibrium)





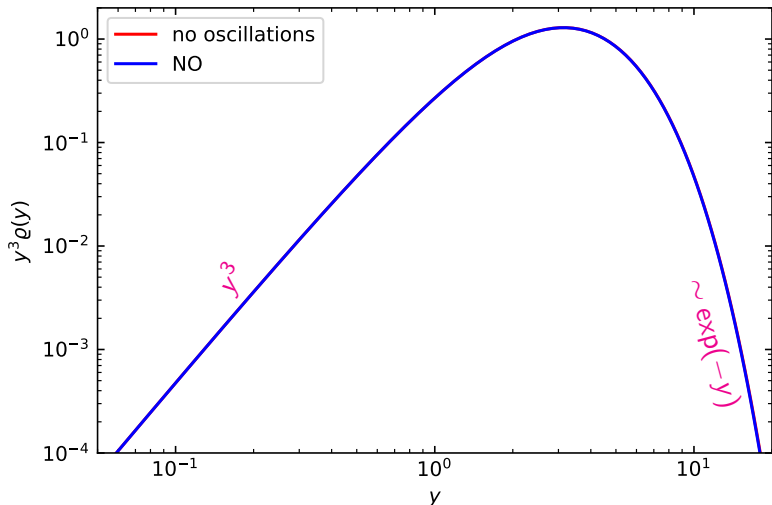
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# Neutrino momentum distribution and $N_{\text{eff}}$

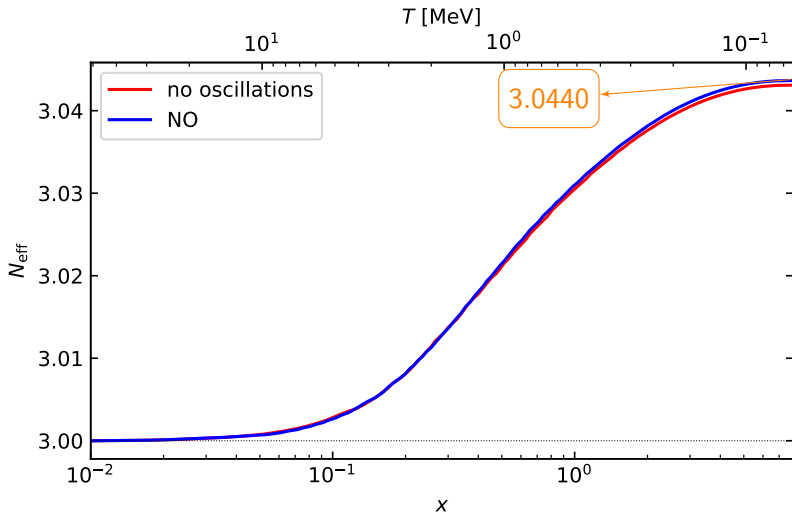
$$N_{\text{eff}}^{\text{final}} = \frac{8}{7} \left(\frac{11}{4}\right)^{4/3} \frac{\rho_\nu}{\rho_\gamma} = \frac{8}{7} \left(\frac{11}{4}\right)^{4/3} \frac{1}{\rho_\gamma} \sum_i g_i \int \frac{d^3 p}{(2\pi)^3} E(p) f_{\nu,i}(p)$$

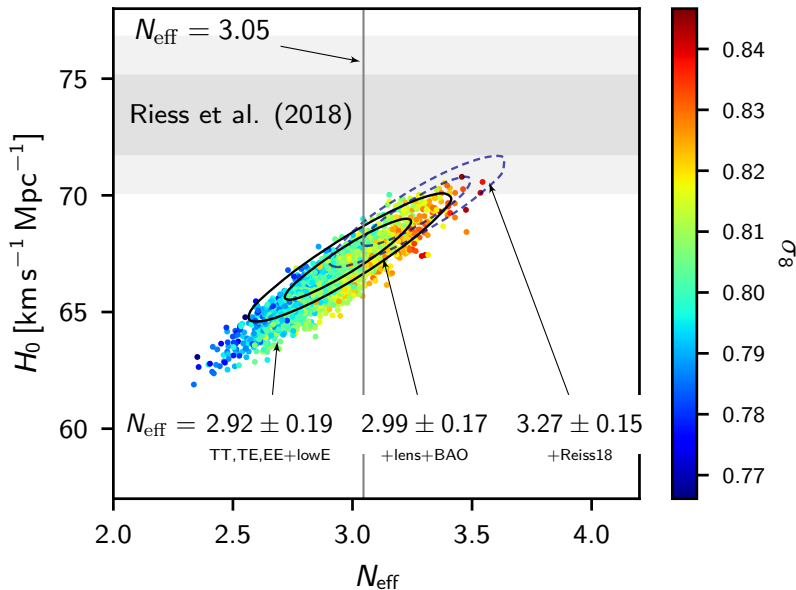
$(11/4)^{1/3} = (T_\gamma/T_\nu)^{\text{fin}}$ 
 $\hookrightarrow \propto y^3 g_{ii}(y)$



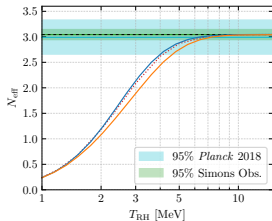
# Neutrino momentum distribution and $N_{\text{eff}}$

$$N_{\text{eff}}^{\text{any time}} = \frac{8}{7} \left( \frac{T_\gamma}{T_\nu} \right)^4 \frac{\rho_\nu}{\rho_\gamma} = \frac{8}{7} \left( \frac{T_\gamma}{T_\nu} \right)^4 \frac{1}{\rho_\gamma} \sum_i g_i \int \frac{d^3 p}{(2\pi)^3} E(p) f_{\nu,i}(p)$$



$N_{\text{eff}}$  and CMB

R  $N_{\text{eff}} < 3?$



e.g. low-temperature reheating scenarios

[PRD 92 (2015) 123534], [PRL 135 (2025) 181003]

## Scenarios with low reheating temperature

Reheating: phase ending inflation

during inflation, the inflaton (non-rel. scalar) dominates the energy density

during reheating: inflaton decays into standard model particles

⇒ photons, electrons, ... are populated directly

radiation domination begins after reheating

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**Low reheating temperature:** when reheating occurs at  $T_{\text{rh}} \lesssim 20$  MeV

notice: if  $T_{\text{rh}} \lesssim 3$  MeV, BBN is broken!

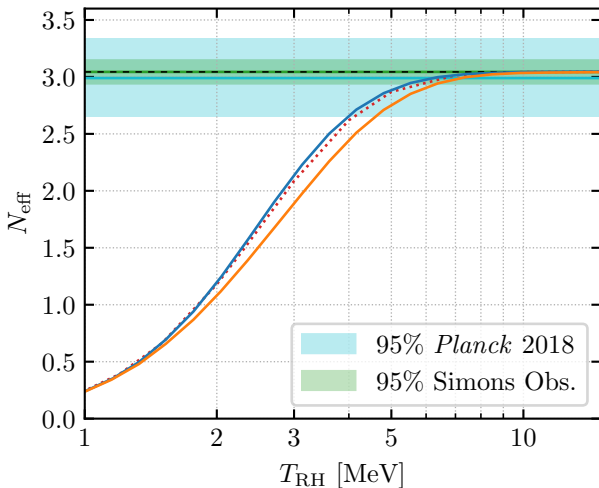
3 neutrino oscillations start to be affected when  $T_{\text{rh}} \lesssim 8$  MeV

what about sterile neutrinos?



# $N_{\text{eff}}$ with low reheating

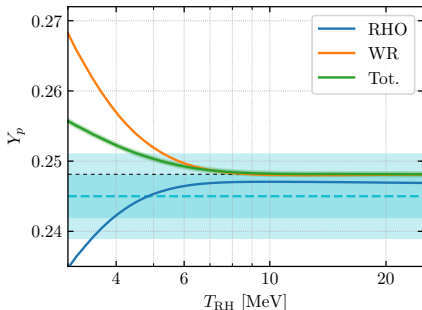
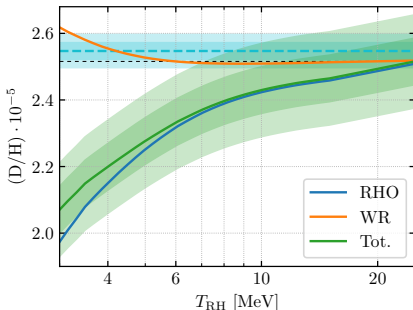
$N_{\text{eff}}$  as a function of  $T_{\text{rh}}$ :



Planck constraint:  $N_{\text{eff}} = 2.92^{+0.36}_{-0.37}$  (95%, TT,TE,EE+lowE)

# BBN and low reheating

Light element abundances depend on  $T_{\text{rh}}$ :



■ **RHO**: total energy density,  
expansion rate



neutrino energy density,  $N_{\text{eff}}$

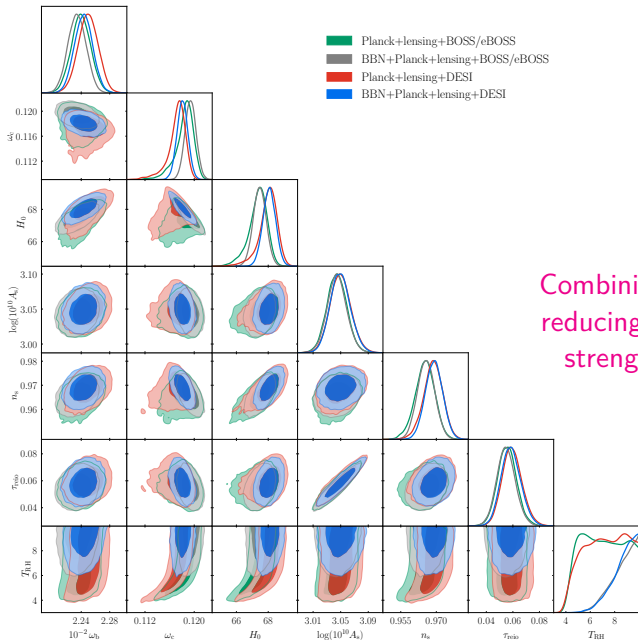
■ **WR**: weak rates  
( $n \leftrightarrow p, \nu_e^{(-)}$  interactions)



$\nu_e^{(-)}$  momentum distribution

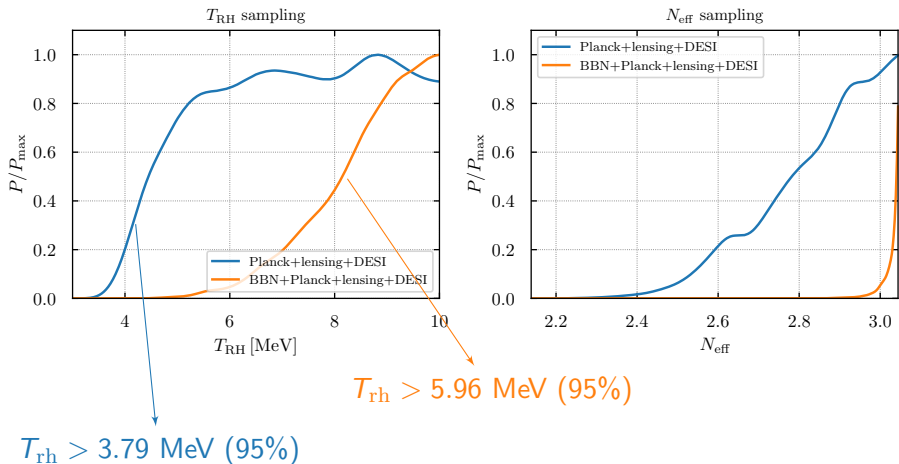
Both effects are important to get Helium right!

# Constraints on low reheating scenarios



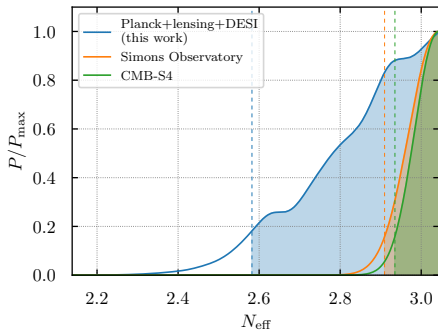
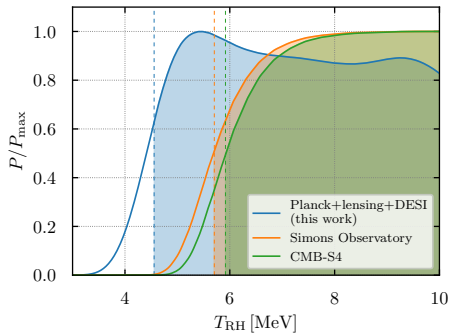
Combining probes helps in reducing degeneracies and strengthening bounds!

# Constraints on low reheating scenarios



BBN occurs at **earlier time than CMB** and is more sensitive to  $N_{eff}$  (RHO) and  $\nu_e^{(-)}$  momentum distribution functions (WR) as a function of  $T_{rh}$ !

# Constraints on low reheating scenarios

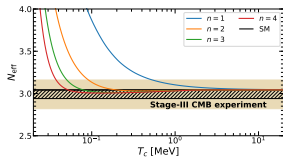


Greater sensitivity will come with future CMB probes  
(more precise in determining  $N_{\text{eff}}$ )

Future CMB alone will reach the precision of  
current BBN+CMB (Planck)+BAO (DESI) observations



$$N_{\text{eff}} > 3?$$



e.g.: additional particles

[JCAP 12 (2023) 20]

## Additional particles in the early universe?

Sterile neutrinos are **coupled via oscillations** to the thermal plasma  
(photons, electrons, neutrinos, (muons), ...)

What if we add a decoupled particle?

let us assume a **non-standard evolution of the energy density**:  $\bar{\rho}_{\text{US}} \propto a^{n+4}$   
 $n = 0 \rightarrow$  radiation;  $n = -1 \rightarrow$  matter;  $n = -2 \rightarrow$  curvature, ...

effect on early universe phenomena is purely gravitational

total energy density:  $\rho = \rho_\gamma + \rho_e + \rho_\nu + \delta\rho_{\text{FTQED}} + \rho_{\text{US}}$

Hubble factor:  $H^2 = 8\pi\rho/(3M_{\text{Pl}}^2)$

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neutrino decoupling: 
$$\frac{d\varrho(y)}{dx} = \frac{1}{xH} \left\{ -i \frac{x^3}{m_e^3} [\mathcal{H}_{\text{eff}}, \varrho] + \frac{m_e^3}{x^3} \mathcal{I}(\varrho) \right\}$$

BBN abundances: 
$$\frac{dX_i}{dx} = \frac{\Gamma_i}{xH}$$

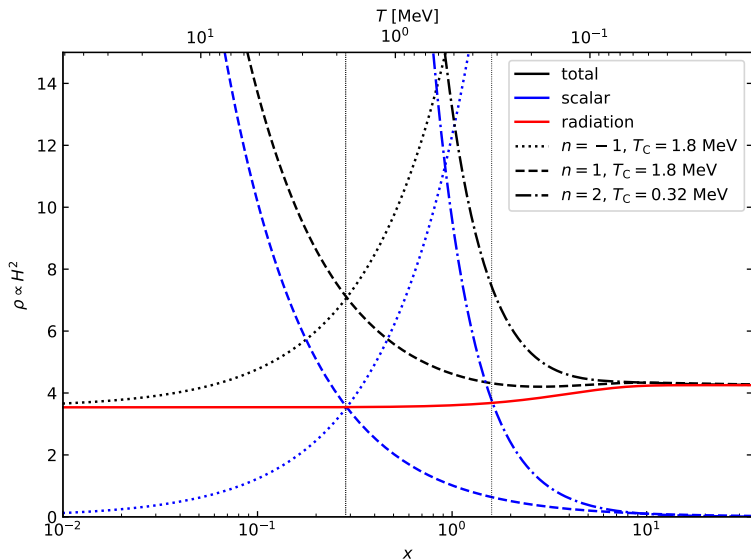
$X_i = n_i/N_B$  abundance relative to total baryons,  $\Gamma_i$  effective reaction rate for nuclide  $i$



# Results from $N_{\text{eff}}$

consider  $\rho_{\text{US}} = \rho_{\text{rad}}$  at  $x_C = m_e/T_C$  for the new particle

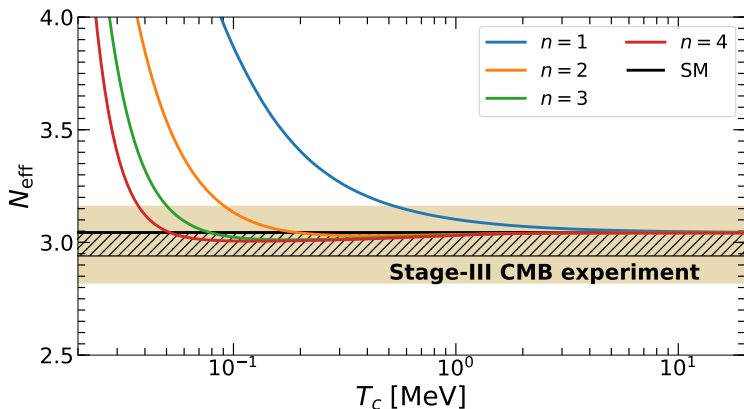
Evolution of the energy density:



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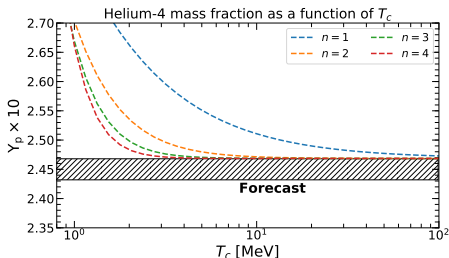
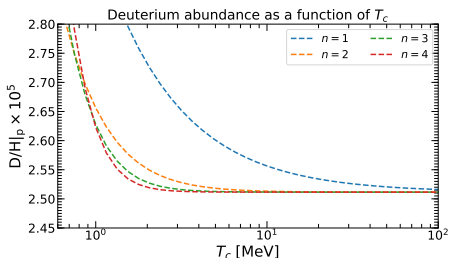
From neutrino decoupling we obtain:



# Results from BBN

consider  $\rho_{US} = \rho_{\text{rad}}$  at  $x_C = m_e/T_C$  for the new particle

Compare to current measurements (Deuterium, Helium):



error bands (gray) are current constraints on the abundances

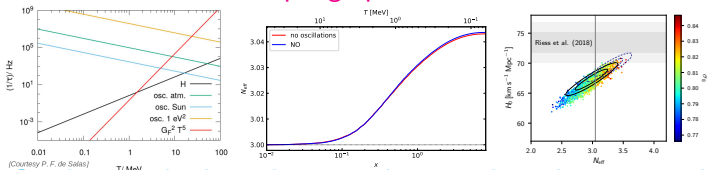
even current precision can strongly constrain  $T_C$



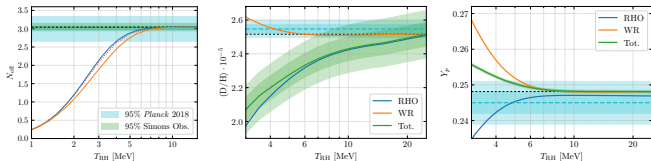
## Conclusions

# What do we learn about non-standard $\nu$ scenarios?

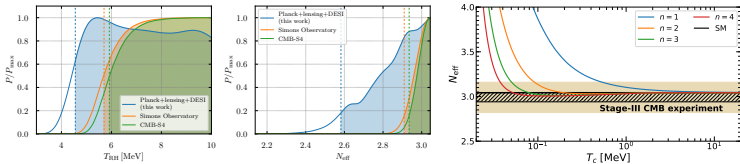
## P Neutrino decoupling: precision calculations



## D Combine multiple probes in order to reduce degeneracies!

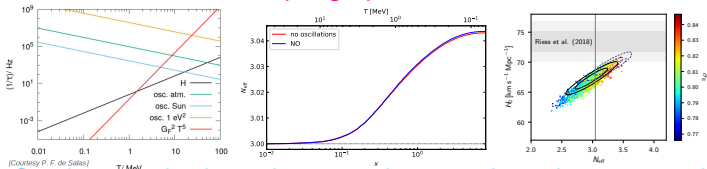


## F Future probes will have better sensitivity!

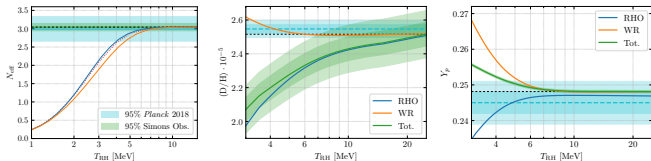


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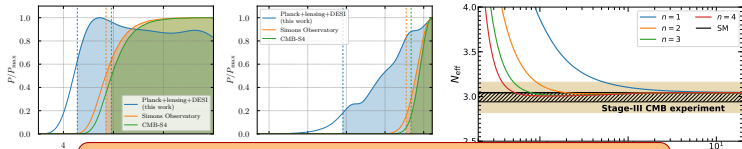
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Thanks for your attention!