

# Flavour and the Tevatron $t\bar{t}$ asymmetry

J. A. Aguilar Saavedra  
in collaboration with M. Pérez-Victoria

Departamento de Física Teórica y del Cosmos  
Universidad de Granada

FLASY2011, Valencia, July 13<sup>th</sup> 2011

This talk is mainly based on papers

- JAAS, M. Pérez-Victoria, “*Probing the Tevatron  $t\bar{t}$  asymmetry at LHC*”, arXiv:1103.2765, JHEP
- JAAS, M. Pérez-Victoria, “*No like-sign tops at Tevatron: Constraints on extended models and implications for the  $t\bar{t}$  asymmetry*”, arXiv:1104.1385, PLB
- JAAS, M. Pérez-Victoria, “*Asymmetries in  $t\bar{t}$  production: LHC versus Tevatron*”, arXiv:1105.4606
- JAAS, M. Pérez-Victoria, “*Simple models for the top asymmetry: constraints and predictions*”, arXiv:1107.0841
- JAAS, M. Pérez-Victoria, “*Shaping the top asymmetry*”, arXiv:1107.2120 (today)

## Disclaimer

This talk was intended to deal primarily with flavour aspects

In the meantime ( $\sim 2$  months), most models with non-trivial flavour are about to be excluded [ as I shall show ]

Then  overview of models, with flavour but not much

# The FB asymmetry at Tevatron

$A_{FB}$  in  $t\bar{t}$  CM frame is the top quark FB asymmetry in opening angle  $\theta$

$$A_{FB} = \frac{N_t(\cos \theta > 0) - N_t(\cos \theta < 0)}{N_t(\cos \theta > 0) + N_t(\cos \theta < 0)}$$

where  $\theta$  is the angle between the top quark momentum and the initial proton direction.

Also, since in CM frame  $N_t(\cos \theta < 0) = N_{\bar{t}}(\cos \bar{\theta} > 0)$ , it can be written as

$$A_{FB} = \frac{N_t(\cos \theta > 0) - N_{\bar{t}}(\cos \bar{\theta} > 0)}{N_t(\cos \theta > 0) + N_{\bar{t}}(\cos \bar{\theta} > 0)}$$

that is, a charge asymmetry where the initial partons stay fixed



do not confuse with  $C$ , charge conjugation symmetry

!!!

## The FB asymmetry at Tevatron

QCD tree level FB symmetric [V coupling; compare with  $A_{FB}$  at LEP]

Electroweak contributions also known as Bernreuther & Si, NPB '10  
... and NNLL corrections from soft gluon emission Ahrens et al '11

Since some time there were discrepancies but in 01/2011 they got worse: for  $m_{t\bar{t}} > 450$  GeV there are  $3.4\sigma$ !

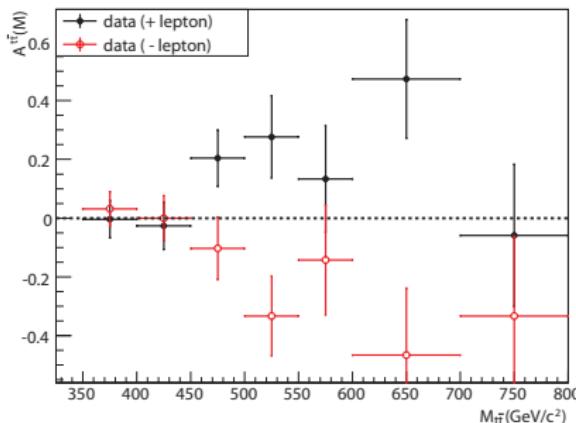
$$A_{\text{FB}}^{\text{SM}} = 0.088 \pm 0.013 \quad A_{\text{FB}}^{\text{exp}} = 0.475 \pm 0.114$$

$\rightarrow 0.11^{+1.7}_{-0.9} [06/11]$

# The FB asymmetry at Tevatron

$q\bar{q} \rightarrow t\bar{t}$  dominates at Tevatron, large  $A_{FB}$  suggests new physics here  
This is an endless source of models for theorists!

One plot to warm up ...



CDF '11

$A_{FB}$  as a function of  $m_{t\bar{t}}$

The excess does not seem only statistical

unknown systematics ...



... or new physics!

This  $A_{FB}$  excess explains a large  $O(70)$  paper excess since 01/2011

# The charge asymmetry at LHC

LHC is a  $pp$  collider, harder to define ‘forward’ and ‘backward’  
[but it can be done event by event, depending on boost of CM wrt LAB]

Alternatively, charge asymmetries can be defined:

- ★  $t$  more forward than  $\bar{t}$   
at parton level
  - ★ initial  $q$  larger momentum fraction than  $\bar{q}$
- }      →      tops larger (pseudo)rapidities  
                        in LAB frame

$$A_C = \frac{N(\Delta > 0) - N(\Delta < 0)}{N(\Delta > 0) + N(\Delta < 0)}$$

with  $\Delta = |y_t| - |\bar{y}_t|$  or  $\Delta = |\eta_t| - |\eta_{\bar{t}}|$  (taken by CMS)

# $A_{FB}$ beyond the SM

Unfortunately, building models is not easy if  $\sigma_{SM} = \sigma_{exp}$

$$\sigma_{SM} = 7.46^{+0.66}_{-0.80} \text{ pb}$$

Langenfeld et al PRD'09

$$\sigma_{exp} = 7.50 \pm 0.48 \text{ pb}$$

CDF

$$\sigma(t\bar{t}) = \sigma_{SM} + \delta\sigma_{int} + \delta\sigma_{quad} \quad \text{👉} \quad \delta\sigma_{int} + \delta\sigma_{quad} \simeq 0$$

in most models this requires a new amplitude  $A_{new} \sim -2A_{SM}$  !!!

## BUT

it is also possible that  $\sigma_{SM} < \sigma_{exp}$

$$\sigma_{SM} = 6.30 \pm 0.19^{+0.31}_{-0.23} \text{ pb}$$

Ahrens et al JHEP'10

in which case moderate contributions to  $\sigma$  and  $A_{FB}$  would be natural

Now, which can be the “new physics” for  $q\bar{q} \rightarrow t\bar{t}$ ?

[large  $A_{FB}$  suggests new physics at tree level]

- $Z'$  or  $g'$  in  $u\bar{u} \rightarrow t\bar{t}$ ,  $s$  and  $t$ -channel
- $W'$  in  $d\bar{d} \rightarrow t\bar{t}$ ,  $t$ -channel
- charge 4/3 vector boson in  $u\bar{u} \rightarrow t\bar{t}$ ,  $u$ -channel
- ...
- and also scalars!

Fortunately, the possibilities are limited by group theory. Only 18!



Lagrangian terms are  $SU(3) \times SU(2)_L \times U(1)_Y$  singlets:  
types of bosons determined by quantum numbers of quarks

### Colour:

$$3 \otimes \bar{3} = 8 \oplus 1$$

$$3 \otimes 3 = 6 \oplus \bar{3}$$

### Isospin:

$$2 \otimes 2 = 3 \oplus 1$$

$$2 \otimes 1 = 2$$

$$1 \otimes 1 = 1$$

### Hypercharge:

$$\sum Y = 0$$

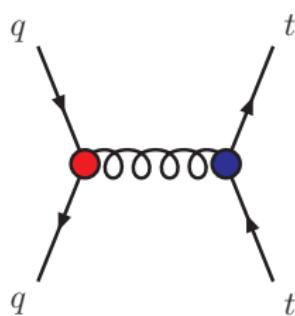
		Vectors	Scalars	
	Label	Rep.	Label	Rep.
	$\mathcal{B}_\mu$	$(1, 1)_0$	$\phi$	$(1, 2)_{-\frac{1}{2}}$
	$\mathcal{W}_\mu$	$(1, 3)_0$	$\Phi$	$(8, 2)_{-\frac{1}{2}}$
	$\mathcal{B}_\mu^1$	$(1, 1)_1$	$\omega^1$	$(3, 1)_{-\frac{1}{3}}$
	$\mathcal{G}_\mu$	$(8, 1)_0$	$\Omega^1$	$(\bar{6}, 1)_{-\frac{1}{3}}$
	$\mathcal{H}_\mu$	$(8, 3)_0$	$\omega^4$	$(3, 1)_{-\frac{4}{3}}$
	$\mathcal{G}_\mu^1$	$(8, 1)_1$	$\Omega^4$	$(\bar{6}, 1)_{-\frac{4}{3}}$
	$\mathcal{Q}_\mu^1$	$(3, 2)_{\frac{1}{6}}$	$\sigma$	$(3, 3)_{-\frac{1}{3}}$
	$\mathcal{Q}_\mu^5$	$(3, 2)_{-\frac{5}{6}}$	$\Sigma$	$(\bar{6}, 3)_{-\frac{1}{3}}$
	$\mathcal{Y}_\mu^1$	$(\bar{6}, 2)_{\frac{1}{6}}$		
	$\mathcal{Y}_\mu^5$	$(\bar{6}, 2)_{-\frac{5}{6}}$		

## Important comments

- ★ A different notation is needed because, for example, a  $Z'$  can be an  $SU(2)_L$  singlet  $\mathcal{B}_\mu$  or belong to a triplet  $\mathcal{W}_\mu$  (in SM both).
- ★ A model can have a number of particles and multiplets in any of these representations.
- ★ In most of the proposed models the contributions to  $A_{FB}$  arise from a single new particle in one of these representations
- ★ This new particle can contribute to  $q\bar{q} \rightarrow t\bar{t}$  in  $s$ ,  $t$  or  $u$  channel.  
 quite a difference !!!

## s-channel

### Example: coloured resonance $\mathcal{G}_\mu$



Requires  $\bar{u}\gamma^\mu u \mathcal{G}_\mu / \bar{d}\gamma^\mu d \mathcal{G}_\mu$  couplings  
as well as  $\bar{t}\gamma^\mu t \mathcal{G}_\mu$

couplings to  $uu$  and  $dd$  small, otherwise  
 $\mathcal{G}_\mu$  gives dijet production (unobserved)

larger coupling to  $tt$  natural in extra  
dimensions

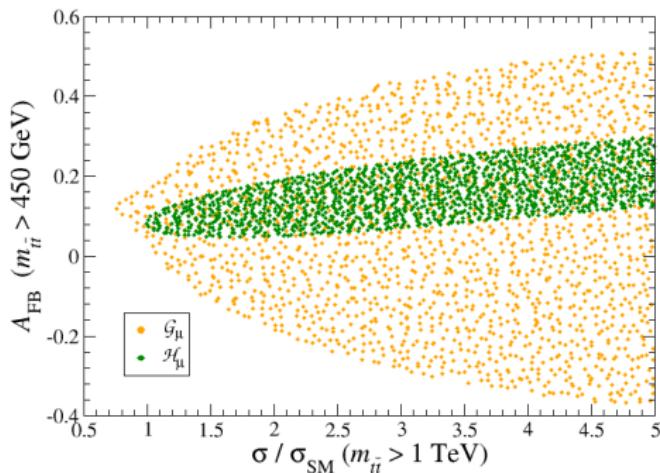
Djouadi et al. PRD '10  
Álvarez et al. JHEP '11

Barceló et al. '11

Distinctive signature: peak (bump) in the  $m_{t\bar{t}}$  distribution

Peak not seen      →      make it higher!

... but for  $M \gg \sqrt{\hat{s}}$ : enhanced  $t\bar{t}$  tail, especially at LHC



JAAS & MPV JHEP'11

Heavy  $\mathcal{G}_\mu$

Arbitrary couplings

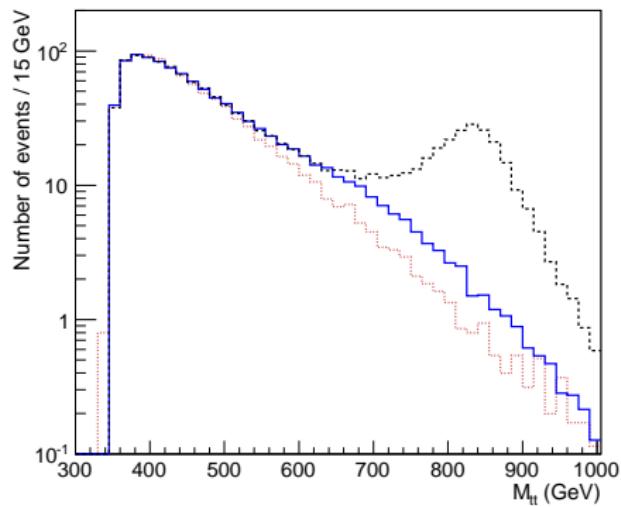
$x$  axis: tail enhancement

$y$  axis:  $A_{FB}$  at Tevatron

→  $A_{FB} = 0.3$  implies  
 $1.5 \times$  tail

# *s*-channel

... or ... peak not seen      →      make it broader!



Barceló et al. '11

$$M = 850 \text{ GeV}$$

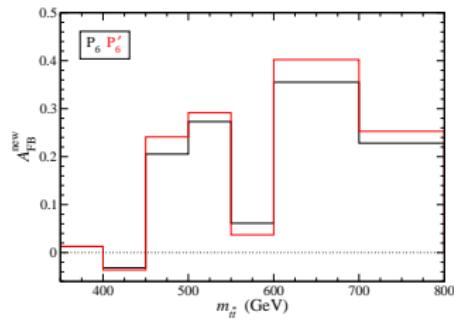
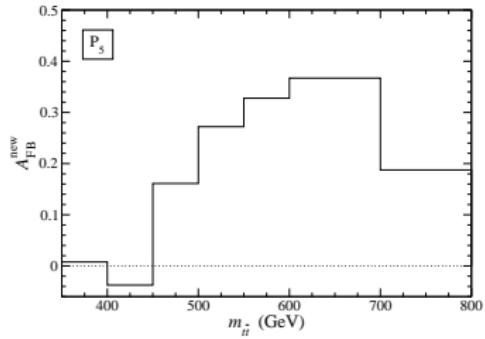
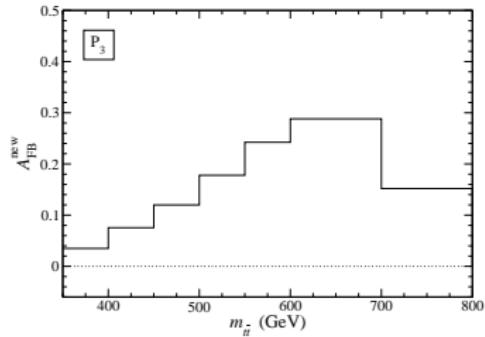
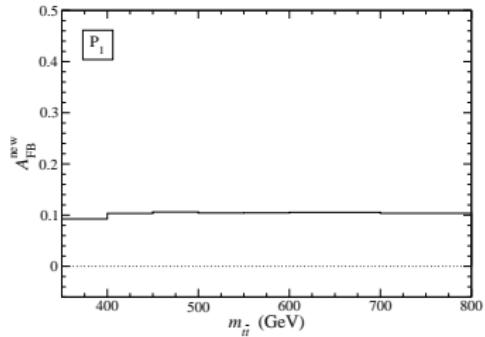
$$\Gamma = 0.7M$$

$$g_L^q = 0.3g \quad g_R^q = -0.3g$$

$$g_L^t = 0 \quad g_R^t = 4.0g$$

+ new quark  $U$

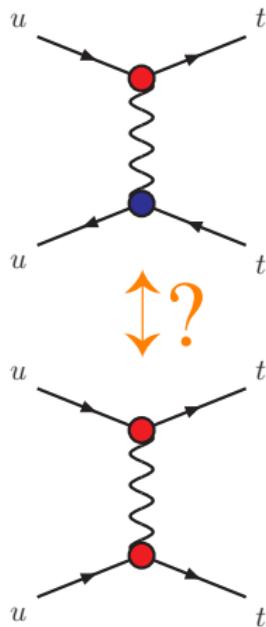
## *s*-channel gluons allow for different asymmetry profiles



JAAS & MPV 'today'

### *t*-channel

## Example: neutral vector boson $Z'$ ( $\mathcal{B}_\mu$ )



$\bar{u}\gamma^\mu t Z'_\mu = (\bar{t}\gamma^\mu u Z'_\mu)^\dagger$  provided  $Z'$  is real

In this case, a distinctive signature is  $t\bar{t}$  production at LHC     Jung et al. PRD'10

Jung et al. PRD'10  
 Cao et al. PRD'10  
 Berger et al. PRL'11

but tight limits already from Tevatron

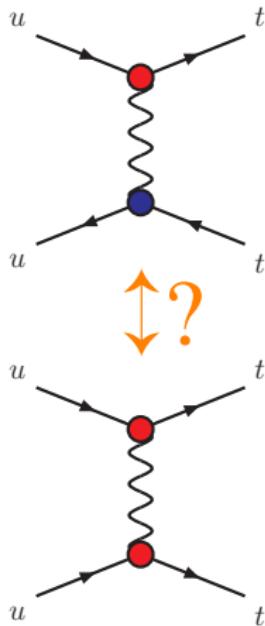
JAAS & MPV PLB'11  
CDF note 10466

and now from LHC

CMS '11

# *t*-channel

## Example: neutral vector boson $Z'$ ( $\mathcal{B}_\mu$ )



$$\bar{u}\gamma^\mu t Z'_\mu = (\bar{t}\gamma^\mu u Z'_\mu)^\dagger \text{ provided } Z' \text{ is real}$$

A *complex*  $Z'$ : two real degenerate  $Z'_1, Z'_2$  with couplings differing by  $i$

☞ like Dirac vs Majorana neutrinos!

Natural with extended flavour symmetries

Jung et al. '11

# $t$ -channel

Additional feature / problem: large  $t\bar{t}$  tail at LHC

- ① Interference  $Z' - \text{SM}$  is *negative*: it decreases  $A_{\text{FB}}$
- ② A positive contribution to  $A_{\text{FB}}$  and agreement with Tevatron  $\sigma(t\bar{t})$  require large coupling and cancellation with SM amplitude
- 👉 This implies a large  $t\bar{t}$  tail at LHC

agreement with Tevatron  $\sigma(t\bar{t})$  ✓  
positive contribution to  $A_{\text{FB}}$  ✓ }  
tail  $\leq 3 \times \text{SM}$  for  $m_{t\bar{t}} > 1 \text{ TeV}$  ✓ →  $M_{Z'} \leq 360 \text{ GeV}$

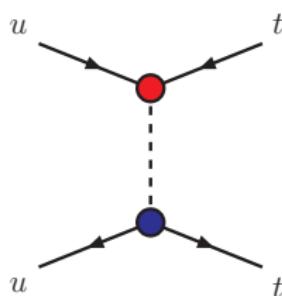
# Interlude: linear vs quadratic new physics

These two examples motivate a classification

- ‘*Linear*’ new physics: quadratic NP contributions not essential  
Coupling can go to zero keeping agreement with total  $\sigma(t\bar{t})$
- ‘*Quadratic*’ new physics: quadratic contributions essential  
Large cancellation, parameter space disconnected from SM  
 easily disfavoured (excluded) by LHC data !!!

## *u*-channel

Example: colour-sextet  $\Omega^4$  / triplet  $\omega^4$



Couplings:  $\bar{u} t^c \Omega^4 / \omega^4$ ,  $\bar{t}^c u \Omega^4 / \omega^4$

$\Omega^4$  can have      ①  $\bar{u} u^c + \bar{u}^c u$   
(but unrelated)    ②  $\bar{t} t^c + \bar{t}^c t$

① gives  $uu \rightarrow uu$  (dijet resonance)

①+② give  $uu \rightarrow tt$  (resonant  $tt$ )

explicit models avoid these ...

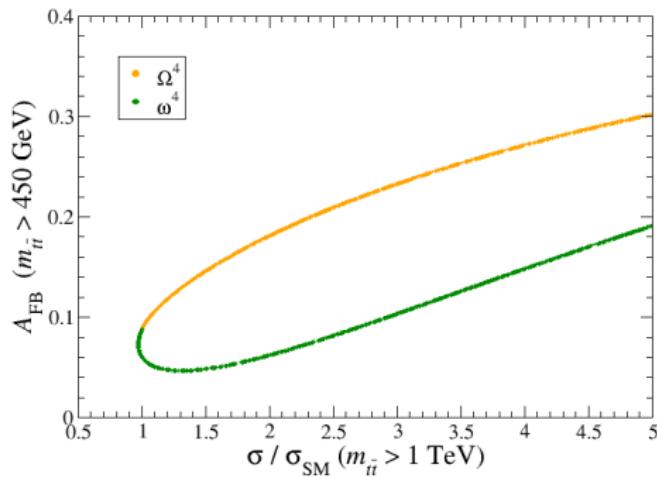
Grinstein et al. PRL '11

Ligeti et al. JHEP '11

$\omega^4$  flavour-antisymmetric couplings

# *u*-channel

Enhanced  $t\bar{t}$  tail at LHC, especially for heavy masses



JAAS & MPV JHEP'11

Heavy  $\Omega^4 / \omega^4$

Arbitrary couplings

x axis: tail enhancement  
y axis:  $A_{FB}$  at Tevatron

→  $A_{FB} = 0.3$  implies  
 $> 5 \times$  tail

## *u*-channel

### Additional feature / problem

The contribution to  $A_{FB}$  is negative for small  $\Omega^4 / \omega^4$  masses

👉 *u*-channel propagator prefers *backward* tops !!!

Numerator does not, however

Masses  $\gtrsim 220$  GeV required for positive  $A_{FB}$  at Tevatron

👉 But going to high  $m_{tt}$  you will finally ‘see’ *u*-channel propagator

... interesting ... 😊

# no-channel: effective framework

Effective operators parameterise effects of new physics at scale  $\Lambda > v$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \mathcal{L}_6 + \dots \quad \mathcal{L}_6 = \sum_x \frac{\alpha_x}{\Lambda^2} O_x$$

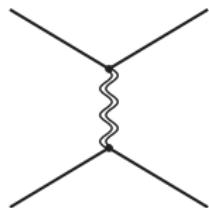
Studies done using effective operators are often referred to as ‘model independent approach’ because using them you can parameterise corrections from any decoupling heavy physics to cross sections, etc.

We don’t know the NP (if any) and we haven’t seen new resonances:  
working with effective operators is a good choice



But note that direct calculation & effective operators tell us  
that a  $Z'$  explaining  $A_{\text{FB}}$  must be light

# Heavy physics and 4F operators

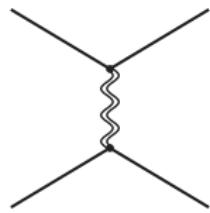


(new) heavy VB

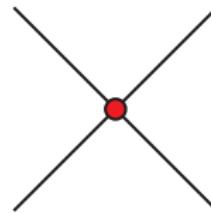
couplings  $g_{ij}$   
masses  $M$

$\left. \begin{array}{c} \text{couplings } g_{ij} \\ \text{masses } M \end{array} \right\} \quad \rightarrow \quad \text{effective operators } C, \quad \Lambda \equiv M$

# Heavy physics and 4F operators



Integrate



(new) heavy VB

4-fermion interaction

$$\left. \begin{array}{c} \text{couplings } g_{ij} \\ \text{masses } M \end{array} \right\} \quad \rightarrow \quad \text{effective operators } C, \quad \Lambda \equiv M$$

## 4F operators for $u\bar{u} \rightarrow t\bar{t}$ and $d\bar{d} \rightarrow t\bar{t}$

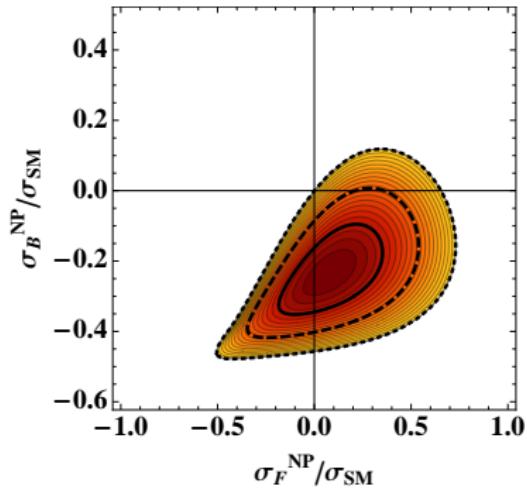
$$\begin{aligned} 1/\Lambda^2 : & O_{qq'}^{1133}, O_{qq}^{3113}, O_{uu}^{3113}, O_{ud'}^{3311}, O_{qu}^{1331}, O_{qu}^{3113}, O_{qd}^{3113} \\ 1/\Lambda^4 : & O_{qq}^{1133}, O_{qq'}^{3113}, O_{uu}^{1133}, O_{ud}^{3311}, O_{qu}^{3311}, O_{qu'}^{1331}, O_{qu'}^{3113}, \\ & O_{qu'}^{3311}, O_{qd'}^{3113}, O_{qq\epsilon}^{1331}, O_{qq\epsilon}^{3311}, O_{qq\epsilon'}^{1331}, O_{qq\epsilon'}^{3311} \end{aligned}$$

[subindices label structure ; superindices are the quark flavours]

This has been done in several places with several approximations

$$\begin{array}{ll} 1/\Lambda^2 : & \text{Jung et al. PLB'10} \\ & \text{Zhang \& Willenbrock PRD'11} \\ & \text{Degrande et al. JHEP'11} \\ & \text{[interference with SM]} \end{array} \quad \begin{array}{ll} 1/\Lambda^4 : & \text{JAAS NPB'11} \\ & \text{Delaunay et al. '11} \\ & \text{JAAS \& MPV JHEP'11} \\ & \text{[quadratic in NP]} \end{array}$$

It has been stressed that NP must interfere, either looking at data . . .



Grinstein et al PRL '11

$$\left. \begin{array}{l} \delta\sigma^F > 0 \\ \delta\sigma^B < 0 \end{array} \right\} \rightarrow \text{interference}$$

. . . and from effective operator analysis

Delaunay et al. '11

**BUT . . .** is this really a restriction?

## Interfering operators – vector bosons

del Aguila et al. JHEP'10

	$C_{qq}^{3113}$	$C_{qq'}^{1133}$	$C_{uu}^{3113}$	$C_{ud'}^{3311}$	$C_{qu}^{1331}$	$C_{qu}^{3113}$	$C_{qd}^{3113}$
$\mathcal{B}_\mu$	$- g_{13}^q ^2$	–	$- g_{13}^u ^2$	–	–	–	–
$\mathcal{W}_\mu$	$ g_{13} ^2$	$-2 g_{13} ^2$	–	–	–	–	–
$\mathcal{G}_\mu$	$\frac{1}{6} g_{13}^q ^2$	$-\frac{1}{2}g_{11}^q g_{33}^q$	$\frac{1}{6} g_{13}^u ^2$ $-\frac{1}{2}g_{11}^u g_{33}^u$	$-\frac{1}{4}g_{33}^u g_{11}^d$	$\frac{1}{2}g_{11}^q g_{33}^u$	$\frac{1}{2}g_{33}^q g_{11}^u$	$\frac{1}{2}g_{33}^q g_{11}^d$
$\mathcal{H}_\mu$	$-\frac{1}{6} g_{13} ^2$ $-g_{11}g_{33}$	$\frac{1}{3} g_{13} ^2$ $+\frac{1}{2}g_{11}g_{33}$	–	–	–	–	–
$\mathcal{B}_\mu^1$	–	–	–	$-\frac{1}{2} g_{13} ^2$	–	–	–
$\mathcal{G}_\mu^1$	–	–	–	$\frac{1}{12} g_{13} ^2$	–	–	–
$\mathcal{Q}_\mu^1$	–	–	–	–	–	–	$ g_{13} ^2$
$\mathcal{Q}_\mu^5$	–	–	–	–	$ g_{31} ^2$	$ g_{13} ^2$	–
$\mathcal{Y}_\mu^1$	–	–	–	–	–	–	$-\frac{1}{2} g_{13} ^2$
$\mathcal{Y}_\mu^5$	–	–	–	–	$-\frac{1}{2} g_{31} ^2$	$-\frac{1}{2} g_{13} ^2$	–

Trivially: all rows non-empty



All vector bosons interfere unless you don't want them to

## Interfering operators – scalars

JAAS & MPV JHEP'11

	$C_{qq}^{3113}$	$C_{qq'}^{1133}$	$C_{uu}^{3113}$	$C_{ud'}^{3311}$	$C_{qu}^{1331}$	$C_{qu}^{3113}$	$C_{qd}^{3113}$
$\Phi$	–	–	–	–	$-\frac{1}{12} g_{13}^u ^2$	$-\frac{1}{12} g_{31}^u ^2$	$-\frac{1}{12} g_{31}^d ^2$
$\omega^1$	–	–	–	$-\frac{1}{4} g_{13} ^2$	–	–	–
$\Omega^1$	–	–	–	$\frac{1}{8} g_{13} ^2$	–	–	–
$\omega^4$	–	–	$-2 g_{13} ^2$	–	–	–	–
$\Omega^4$	–	–	$ g_{13} ^2$	–	–	–	–
$\sigma$	$-2 g_{13} ^2$	$-2 g_{13} ^2$	–	–	–	–	–
$\Sigma$	$ g_{13} ^2$	$ g_{13} ^2$	–	–	–	–	–

Trivially: all rows non-empty



All scalars interfere  
unless you don't want them to

The issue is not whether NP interferes but *how* it does

- ①  $Z'$ ,  $W'$ ,  $\omega^4$ : negative, decreases  $A_{\text{FB}}$  and  $\sigma$  😞
- ②  $\Omega^4$ : positive, increases  $A_{\text{FB}}$  and  $\sigma$  😊
- ③ axi- $\mathcal{G}_\mu$ :  $\delta\sigma^F = -\delta\sigma^B$ , increases  $A_{\text{FB}}$  keeping  $\sigma$  at  $1/\Lambda^2$  😃😃😃

# Signals at LHC

Cunning physicists build models with (often light) elusive particles hard to see anywhere but in the  $t\bar{t}$  asymmetry ...

BUT

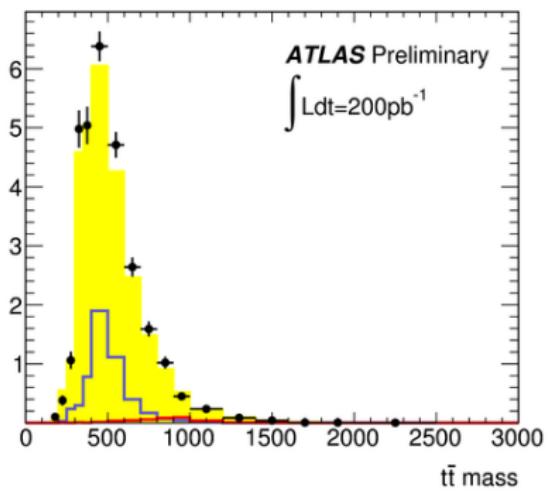
one probe from which you cannot escape is  $t\bar{t}$  production itself:

- ★ if you have something anomalous in  $t\bar{t}$  at Tevatron
- ★ something anomalous in  $t\bar{t}$  must be seen at LHC

Excellent candidate: the  $t\bar{t}$  tail:  $\left\{ \begin{array}{l} \text{not dominated by } gg \rightarrow t\bar{t} \\ \text{more sensitive to heavy physics} \end{array} \right.$

and, of course, the charge asymmetry  $A_C$  at LHC

# The $t\bar{t}$ tail at LHC is a crucial test ...



ATLAS '11

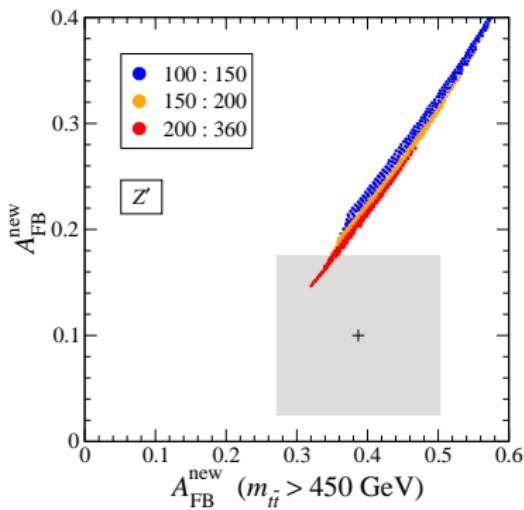
Implications of tail  $\leq 3 \times \text{SM}$

[tail  $\equiv m_{t\bar{t}} \geq 1 \text{ TeV}$ ]

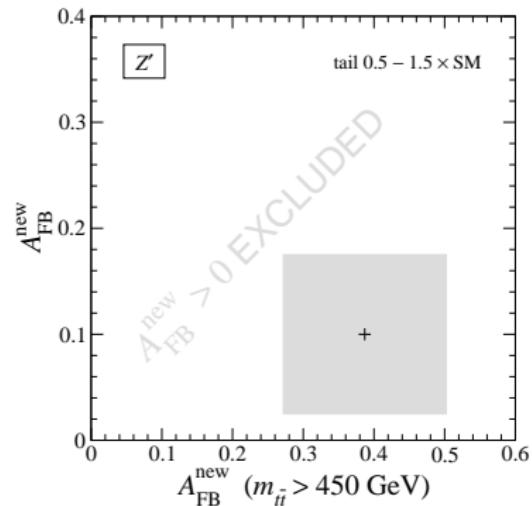
- $Z'$ :  $M \leq 360 \text{ GeV}$
- $W'$ :  $M \leq 2.2 \text{ TeV}$
- axigluon & axi-friends:  
small tail if heavy
- $\Omega^4$ : tail less constraining  
than Tevatron  $\sigma$
- $\omega^4$ :  $M \leq 1.9 \text{ TeV}$

# Example: $Z'$

tail  $\leq 3 \times \text{SM}$



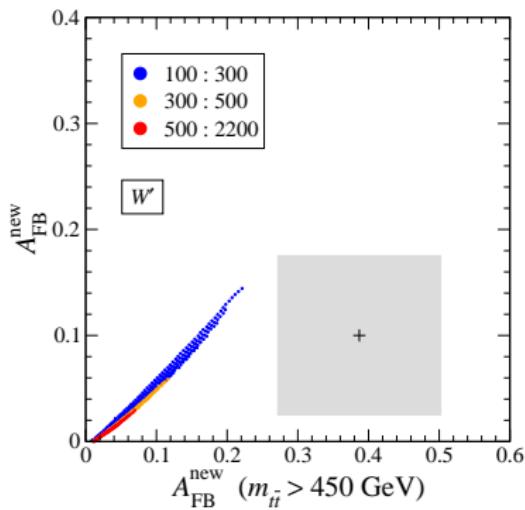
tail  $0.5 - 1.5 \times \text{SM}$



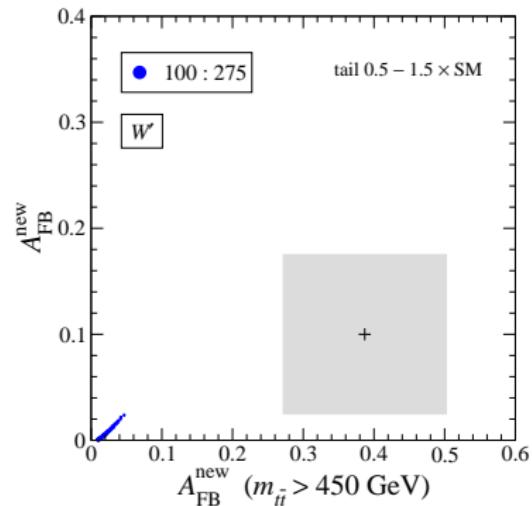
JAAS & MPV '11

# Example: $W'$

tail  $\leq 3 \times \text{SM}$



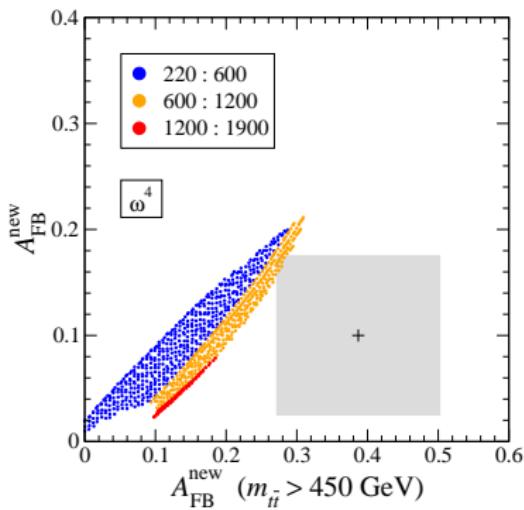
tail  $0.5 - 1.5 \times \text{SM}$



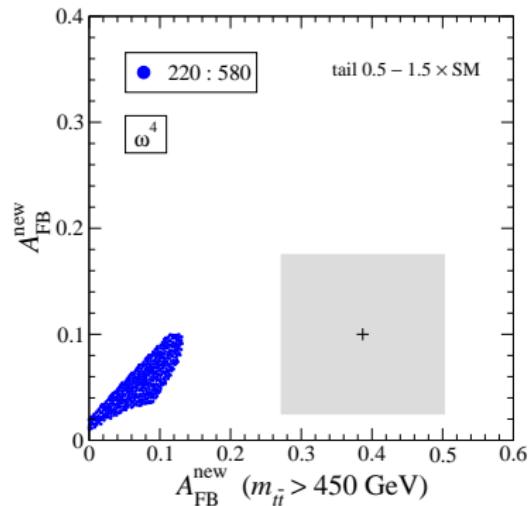
JAAS & MPV '11

# Example: $\omega^4$

tail  $\leq 3 \times \text{SM}$



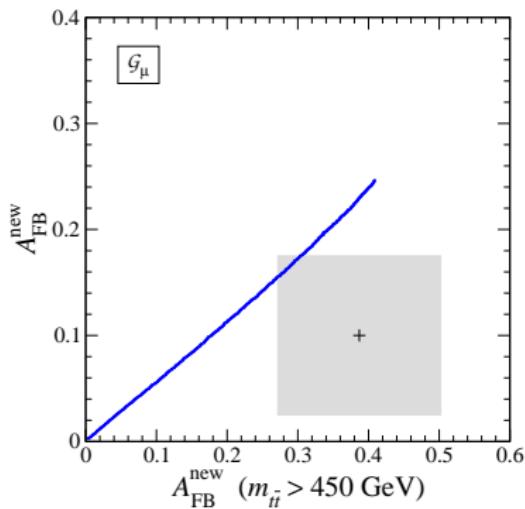
tail  $0.5 - 1.5 \times \text{SM}$



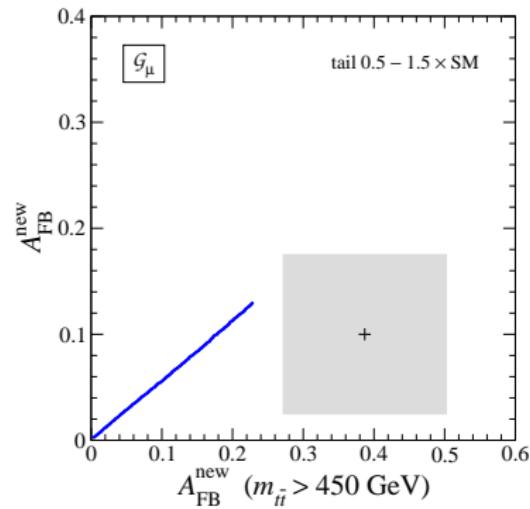
JAAS & MPV '11

# Example: heavy axigluon

tail  $\leq 3 \times \text{SM}$



tail  $0.5 - 1.5 \times \text{SM}$



JAAS & MPV '11

... and the charge asymmetry too!

CMS measurement for  $35 \text{ pb}^{-1}$

$$A_C = 0.060 \pm 0.134 \text{ (stat)} \pm 0.026 \text{ (syst)}$$

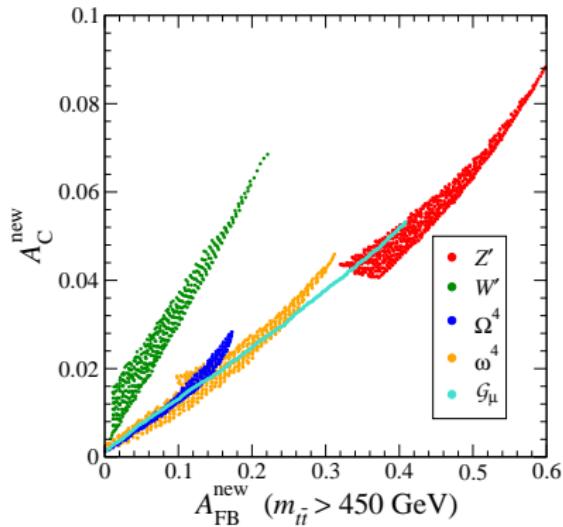
offers good hope for the (7 TeV) future:

- 40% systematics will improve with more data
- statistics much larger,  $1 \text{ fb}^{-1}$  available!

👉 comparison with Tevatron  $A_{FB}$  for model discrimination

For this, a comprehensive scan over masses and couplings is required  
[most papers only select few  $O(2)$  benchmark points]

# $A_{FB}$ at Tevatron vs $A_C$ at LHC



JAAS & MPV '11

$A_C$  inclusive

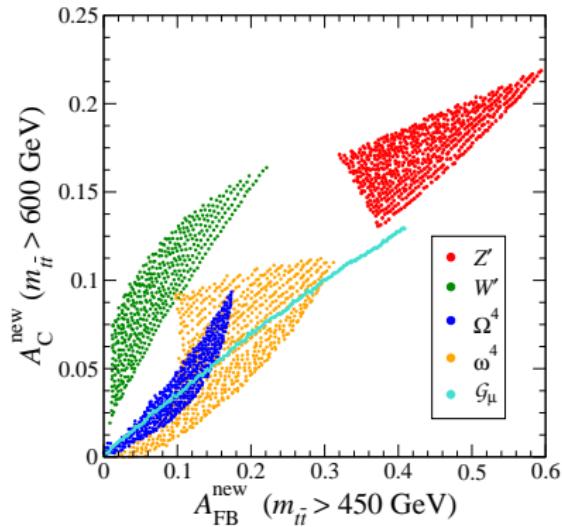
$W'$  slope  $2\times$ :  $d\bar{d} / u\bar{u}$  PDF  
enhancement at LHC

Rest of models more similar

Notice that  $A_C \geq 0.04$  for  $Z'$

Tevatron:  $A_{FB}^{\text{new}} = 0.387 \pm 0.115$

# $A_{FB}$ at Tevatron vs $A_C$ at LHC



JAAS & MPV '11

$A_C$  for  $m_{\tilde{t}\tilde{t}} > 600 \text{ GeV}$

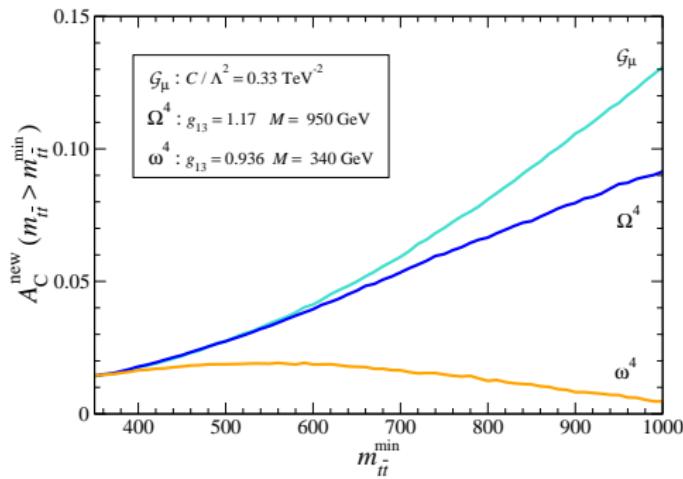
$Z'$  ( $t$  channel) gets a boost

$\Omega^4$  and  $\omega^4$  regions wider: larger differences between light and heavy scalars

Tevatron:  $A_{FB}^{\text{new}} = 0.387 \pm 0.115$

# $A_{FB}$ at Tevatron vs $A_C$ at LHC

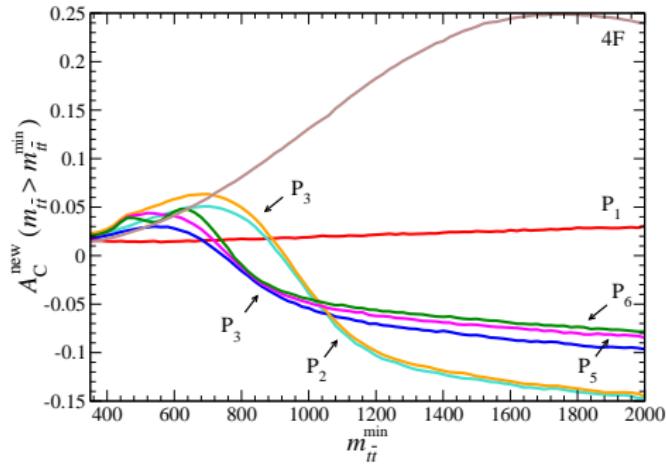
But notice that close points are not mapped close !!!



$\mathcal{G}_\mu$ : 4-fermion operators  
 $\Omega^4$ :  $M = 950 \text{ GeV}$   
 $\omega^4$ :  $M = 340 \text{ GeV}$

JAAS & MPV '11

Different Tevatron profiles  $\rightarrow$  also different at LHC



JAAS & MPV 'today'

Distinctive feature:  
Negative asymmetry  
at LHC reach!

# What about other charge asymmetries?

Other definitions in the market too ...

‘Central’ charge asymmetry

Ferrario & Rodrigo PRD’08

$$A_{\text{cen}} = \frac{N_t(|y| < y_0) - N_{\bar{t}}(|y| < y_0)}{N_t(|y| < y_0) + N_{\bar{t}}(|y| < y_0)}$$

‘Forward’ charge asymmetry

Hewett et al. ’11

$$A_{\text{fwd}} = \frac{N_t(y_0 < |y| < y_1) - N_{\bar{t}}(y_0 < |y| < y_1)}{N_t(y_0 < |y| < y_1) + N_{\bar{t}}(y_0 < |y| < y_1)}$$

with  $y_0, y_1$  some fixed (arbitrary) numbers

# What about other charge asymmetries?

## Comparison

Model	$A_C^{\text{new}}$	$A_C^{\text{new}} \times \sqrt{\sigma}$	$A_{\text{cen}}^{\text{new}}$	$A_{\text{cen}}^{\text{new}} \times \sqrt{\sigma}$	$A_{\text{fwd}}^{\text{new}}$	$A_{\text{fwd}}^{\text{new}} \times \sqrt{\sigma}$
$Z'$	0.0403	$13.0 \text{ fb}^{1/2}$	-0.0207	$-8.6 \text{ fb}^{1/2}$	0.107	$19.6 \text{ fb}^{1/2}$
$W'$	0.0536	$18.0 \text{ fb}^{1/2}$	-0.0249	$-10.8 \text{ fb}^{1/2}$	0.119	$23.5 \text{ fb}^{1/2}$
$\mathcal{G}_\mu$	0.0433	$14.2 \text{ fb}^{1/2}$	-0.0142	$-6.0 \text{ fb}^{1/2}$	0.0800	$14.3 \text{ fb}^{1/2}$
$\phi$	0.0242	$7.7 \text{ fb}^{1/2}$	-0.0074	$-3.1 \text{ fb}^{1/2}$	0.0430	$7.4 \text{ fb}^{1/2}$
$\omega^4$	0.0248	$8.3 \text{ fb}^{1/2}$	-0.0085	$-3.7 \text{ fb}^{1/2}$	0.0480	$8.8 \text{ fb}^{1/2}$
$\Omega^4$	0.0185	$6.1 \text{ fb}^{1/2}$	-0.0060	$-2.6 \text{ fb}^{1/2}$	0.0331	$6.1 \text{ fb}^{1/2}$

# What about other charge asymmetries?

## Comparison

Model	$A_C^{\text{new}}$	$A_C^{\text{new}} \times \sqrt{\sigma}$	$A_{\text{cen}}^{\text{new}}$	$A_{\text{cen}}^{\text{new}} \times \sqrt{\sigma}$	$A_{\text{fwd}}^{\text{new}}$	$A_{\text{fwd}}^{\text{new}} \times \sqrt{\sigma}$
$Z'$	0.0403	<b>13.0 fb<sup>1/2</sup></b>	-0.0207	-8.6 fb <sup>1/2</sup>	0.107	<b>19.6 fb<sup>1/2</sup></b>
$W'$	0.0536	<b>18.0 fb<sup>1/2</sup></b>	-0.0249	-10.8 fb <sup>1/2</sup>	0.119	<b>23.5 fb<sup>1/2</sup></b>
$\mathcal{G}_\mu$	0.0433	14.2 fb <sup>1/2</sup>	-0.0142	-6.0 fb <sup>1/2</sup>	0.0800	14.3 fb <sup>1/2</sup>
$\phi$	0.0242	7.7 fb <sup>1/2</sup>	-0.0074	-3.1 fb <sup>1/2</sup>	0.0430	7.4 fb <sup>1/2</sup>
$\omega^4$	0.0248	8.3 fb <sup>1/2</sup>	-0.0085	-3.7 fb <sup>1/2</sup>	0.0480	8.8 fb <sup>1/2</sup>
$\Omega^4$	0.0185	6.1 fb <sup>1/2</sup>	-0.0060	-2.6 fb <sup>1/2</sup>	0.0331	6.1 fb <sup>1/2</sup>

# What about other charge asymmetries?

## Comparison

Model	$A_C^{\text{new}}$	$A_C^{\text{new}} \times \sqrt{\sigma}$	$A_{\text{cen}}^{\text{new}}$	$A_{\text{cen}}^{\text{new}} \times \sqrt{\sigma}$	$A_{\text{fwd}}^{\text{new}}$	$A_{\text{fwd}}^{\text{new}} \times \sqrt{\sigma}$
$Z'$	0.0403	$13.0 \text{ fb}^{1/2}$	-0.0207	$-8.6 \text{ fb}^{1/2}$	0.107	$19.6 \text{ fb}^{1/2}$
$W'$	0.0536	$18.0 \text{ fb}^{1/2}$	-0.0249	$-10.8 \text{ fb}^{1/2}$	0.119	$23.5 \text{ fb}^{1/2}$
$\mathcal{G}_\mu$	0.0433	$14.2 \text{ fb}^{1/2}$	-0.0142	$-6.0 \text{ fb}^{1/2}$	0.0800	$14.3 \text{ fb}^{1/2}$
$\phi$	0.0242	$7.7 \text{ fb}^{1/2}$	-0.0074	$-3.1 \text{ fb}^{1/2}$	0.0430	$7.4 \text{ fb}^{1/2}$
$\omega^4$	0.0248	$8.3 \text{ fb}^{1/2}$	-0.0085	$-3.7 \text{ fb}^{1/2}$	0.0480	$8.8 \text{ fb}^{1/2}$
$\Omega^4$	0.0185	$6.1 \text{ fb}^{1/2}$	-0.0060	$-2.6 \text{ fb}^{1/2}$	0.0331	$6.1 \text{ fb}^{1/2}$

# What about other charge asymmetries?

## Comparison

Model	$A_C^{\text{new}}$	$A_C^{\text{new}} \times \sqrt{\sigma}$	$A_{\text{cen}}^{\text{new}}$	$A_{\text{cen}}^{\text{new}} \times \sqrt{\sigma}$	$A_{\text{fwd}}^{\text{new}}$	$A_{\text{fwd}}^{\text{new}} \times \sqrt{\sigma}$
$Z'$	0.0403	$13.0 \text{ fb}^{1/2}$	-0.0207	$-8.6 \text{ fb}^{1/2}$	0.107	$19.6 \text{ fb}^{1/2}$
$W'$	0.0536	$18.0 \text{ fb}^{1/2}$	-0.0249	$-10.8 \text{ fb}^{1/2}$	0.119	$23.5 \text{ fb}^{1/2}$
$\mathcal{G}_\mu$	0.0433	$14.2 \text{ fb}^{1/2}$	-0.0142	$-6.0 \text{ fb}^{1/2}$	0.0800	$14.3 \text{ fb}^{1/2}$
$\phi$	0.0242	$7.7 \text{ fb}^{1/2}$	-0.0074	$-3.1 \text{ fb}^{1/2}$	0.0430	$7.4 \text{ fb}^{1/2}$
$\omega^4$	0.0248	$8.3 \text{ fb}^{1/2}$	-0.0085	$-3.7 \text{ fb}^{1/2}$	0.0480	$8.8 \text{ fb}^{1/2}$
$\Omega^4$	0.0185	$6.1 \text{ fb}^{1/2}$	-0.0060	$-2.6 \text{ fb}^{1/2}$	0.0331	$6.1 \text{ fb}^{1/2}$

**Conclusion:**  $A_C$  is as good as  $A_{\text{fwd}} / A_{\text{cen}}$  for most models  
in particular for the models surviving the tail constraints

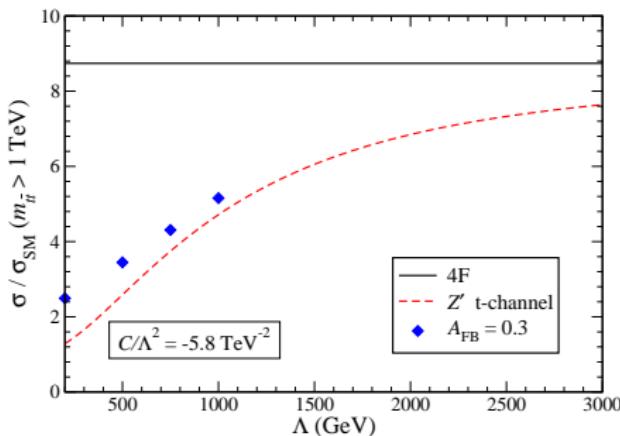
# Conclusions

- ★ I hope I have convinced you that  $A_{FB}$  is an interesting hint of NP
- ★ Both CDF and D0 have been seeing positive excesses in the last few years. This might be indeed a signal of new physics
- ★ Many models have been proposed to explain the measurement
- ★ LHC will have a word on it, through the measurement of the  $t\bar{t}$  tail and the charge asymmetry.
- ★ Strong motivation for the measurement of  $A_C$  as a function of  $m_{t\bar{t}}$

# ADDITIONAL SLIDES

# *t*-channel

High mass tail ( $m_{t\bar{t}} > 1$  TeV) vs  $Z'$  mass



tail for  $A_{FB} = 0.3$

*x* axis:  $Z'$  mass

*y* axis: tail enhancement

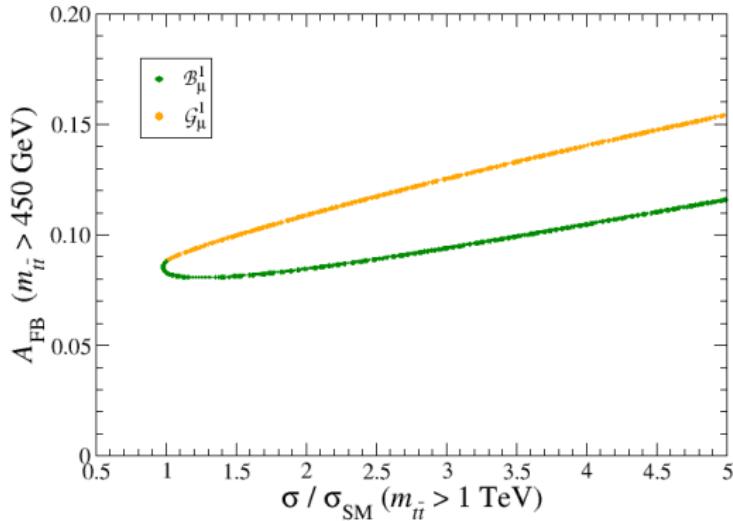
black: 4F limit

blue: exact calculation

red: fixed  $C/\Lambda^2$  ( $A_{FB} < 0.3$ )

JAAS & MPV JHEP'11

# $t$ -channel – heavy $W'$



$A_{FB} \simeq 0.3$  implies  $19\times$ ,  $25\times$  tail above 1 TeV at LHC

## Corrections up to order $1/\Lambda^4$ ?

For the range of parameters required to explain the asymmetry, quadratic corrections are important.



remember that  $A_{\text{new}} \sim A_{\text{SM}}$

However, we have to worry about consistency: dim 8 not considered!

For extra vector bosons and scalars approximation consistent because:

- for  $C$  small,  $\Lambda^4$  does not matter
- for  $C$  large,  $\text{SM} \times \text{dim 8} \sim C/\Lambda^4$  is subleading with respect to  $(\text{dim 6})^2 \sim C^2/\Lambda^4$ .

# From models to effective operators

Model X has a  $Z'_1$  (in rep  $\mathcal{B}_\mu$ ) with mass  $M_1$  and couplings

$$-(g_{13}^q \bar{u}_L \gamma^\mu t_L + g_{13}^u \bar{u}_R \gamma^\mu t_R + \dots) Z'_{1\mu} + \text{h.c.}$$

and a  $Z'_2$  (in rep  $\mathcal{B}_\mu$ ) with mass  $M_2$  and couplings

$$-(h_{13}^q \bar{u}_L \gamma^\mu t_L + h_{13}^u \bar{u}_R \gamma^\mu t_R + \dots) Z'_{2\mu} + \text{h.c.}$$

Then, you look in the tables and find the coefficients, for example

$t\bar{t}$

$$\frac{C_{uu}^{1313}}{\Lambda^2} = -\frac{(g_{13}^u)^2}{M_1^2} - \frac{(h_{13}^u)^2}{M_2^2}, \dots$$

$t\bar{t}$

$$\frac{C_{uu}^{3113}}{\Lambda^2} = -\frac{|g_{13}^u|^2}{M_1^2} - \frac{|h_{13}^u|^2}{M_2^2}, \dots$$

from which you calculate your  $\sigma$ ,  $A_{FB}$ , etc. Just add up!

## Four-fermion operators, for fans

$$O_{qq}^{ijkl} = \frac{1}{2}(\bar{q}_{Li}\gamma^\mu q_{Lj})(\bar{q}_{Lk}\gamma_\mu q_{Ll})$$

$$O_{qq'}^{ijkl} = \frac{1}{2}(\bar{q}_{Lia}\gamma^\mu q_{Ljb})(\bar{q}_{Lkb}\gamma_\mu q_{Lla})$$

$$O_{uu}^{ijkl} = \frac{1}{2}(\bar{u}_{Ri}\gamma^\mu u_{Rj})(\bar{u}_{Rk}\gamma_\mu u_{Rl})$$

$$O_{ud}^{ijkl} = (\bar{u}_{Ri}\gamma^\mu u_{Rj})(\bar{d}_{Rk}\gamma_\mu d_{Rl})$$

$$O_{ud'}^{ijkl} = (\bar{u}_{Ria}\gamma^\mu u_{Rjb})(\bar{d}_{Rkb}\gamma_\mu d_{Rla})$$

$$O_{qu}^{ijkl} = (\bar{q}_{Li}u_{Rj})(\bar{u}_{Rk}q_{Ll})$$

$$O_{qu'}^{ijkl} = (\bar{q}_{Lia}u_{Rjb})(\bar{u}_{Rkb}q_{Lla})$$

$$O_{qd}^{ijkl} = (\bar{q}_{Li}d_{Rj})(\bar{d}_{Rk}q_{Ll})$$

$$O_{qd'}^{ijkl} = (\bar{q}_{Lia}d_{Rjb})(\bar{d}_{Rkb}q_{Lla})$$

$$O_{qq\epsilon}^{ijkl} = (\bar{q}_{Li}u_{Rj}) [(\bar{q}_{Lk}\epsilon)^T d_{Rl}]$$

$$O_{qq\epsilon'}^{ijkl} = (\bar{q}_{Lia}u_{Rjb}) [(\bar{q}_{Lkb}\epsilon)^T d_{Rla}]$$

# $A_{\text{FB}}$ with effective operators

Example: corrections to  $u\bar{u} \rightarrow t\bar{t}$  in terms of the  $C$ 's

$$\begin{aligned}\delta\sigma_{\text{int}}^{F,B}(u\bar{u}) &= \frac{D_{\text{int}}^{F,B}}{\Lambda^2} \left[ C_{qq'}^{1133} + C_{qq}^{3113} + C_{uu}^{3113} \right] - \frac{\tilde{D}_{\text{int}}^{F,B}}{\Lambda^2} \left[ C_{qu}^{1331} + C_{qu}^{3113} \right] \\ \delta\sigma_{4\text{F}}^{F,B}(u\bar{u}) &= \frac{D_1^{F,B}}{\Lambda^4} \left[ \Pi(C_{qq}^{1133} + C_{qq'}^{3113}, C_{qq'}^{1133} + C_{qq}^{3113}) + \Pi(C_{uu}^{1133}, C_{uu}^{3113}) \right] \\ &\quad + \frac{\tilde{D}_1^{F,B}}{\Lambda^4} \left[ \Pi(C_{qu'}^{1331}, C_{qu}^{1331}) + \Pi(C_{qu'}^{3113}, C_{qu}^{3113}) \right] + \frac{D_2}{\Lambda^4} \Pi(C_{qu'}^{3311}, C_{qu}^{3311}) \\ &\quad - \frac{D_4}{\Lambda^4} \left[ \Pi(C_{qq}^{1133} + C_{qq'}^{3113}, C_{qu'}^{1331}, C_{qq'}^{1133} + C_{qq}^{3113}, C_{qu}^{1331}) \right. \\ &\quad \left. + \Pi(C_{qu'}^{3113}, C_{uu}^{1133}, C_{qu}^{3113}, C_{uu}^{3113}) \right]\end{aligned}$$

[ $C$ 's: operator coefficients ;  $D$ 's: numerical constants ;  $\Pi$ 's: some polynomials]

# A large asymmetry with a small $t\bar{t}$ tail

The asymmetry can be large with not too large couplings provided

$$\left. \begin{array}{l} \delta\sigma^F(u\bar{u}) = -\delta\sigma^B(u\bar{u}) \\ \delta\sigma^F(d\bar{d}) = -\delta\sigma^B(d\bar{d}) \end{array} \right\} \quad \rightarrow \quad \delta\sigma(q\bar{q} \rightarrow t\bar{t}) = 0$$

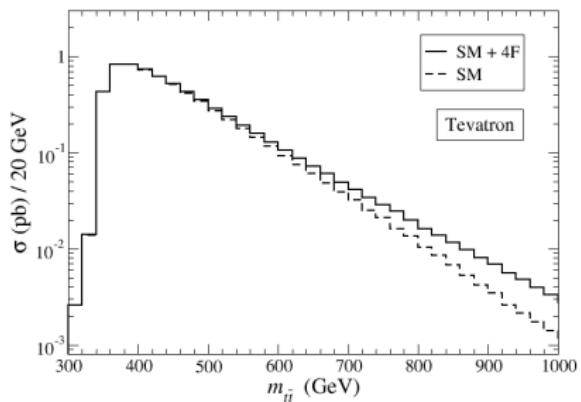
This happens at all energies provided that

$$\begin{aligned} [C_{qq'}^{1133} + C_{qq}^{3113} + C_{uu}^{3113}] &= [C_{qu}^{1331} + C_{qu}^{3113}] \\ [C_{qq'}^{1133} + 2C_{ud'}^{3311}] &= [C_{qu}^{1331} + C_{qd}^{3113}] \end{aligned}$$

Looks complicated? It's automatic for an axigluon:  $-g_{ii}^q = g_{ii}^u = g_{ii}^d$

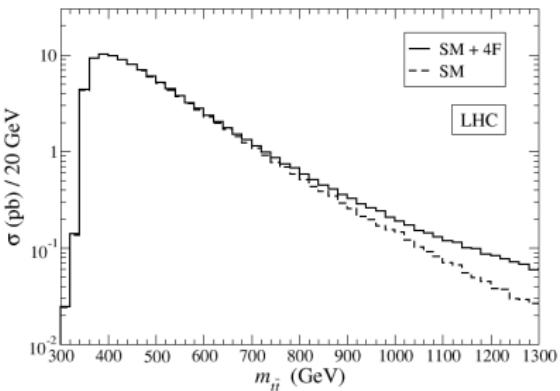
Possible in other models: necessary  $\textcolor{red}{LL+RR=LR+RL}$  for  $u\bar{u}$  and  $d\bar{d}$

## Tails corresponding to $A_{FB} = 0.366$ (best fit)



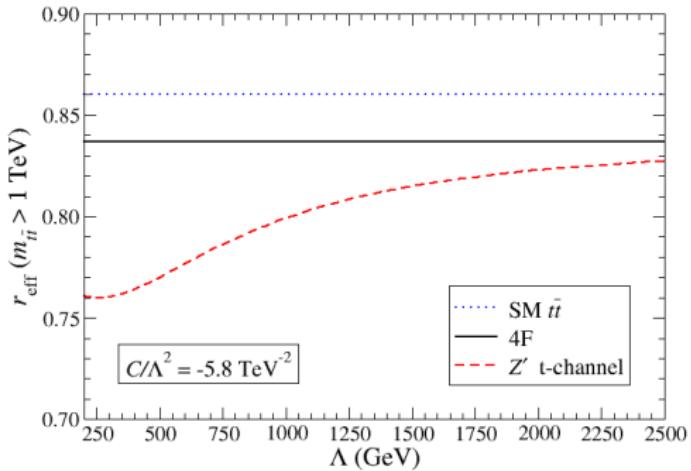
Tevatron

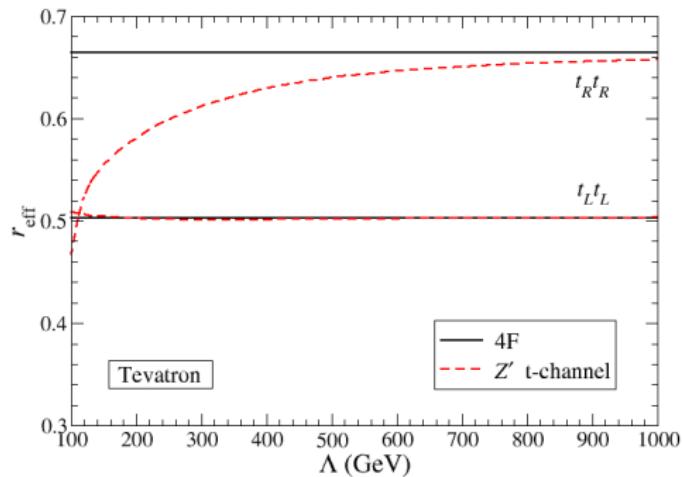
$1.5 \times$  tail above  $700 \text{ GeV}$   
(within exp. error)



LHC

$2.3 \times$  tail above  $1 \text{ TeV}$   
testable soon?

Efficiency at  $t\bar{t}$  tail

Efficiency for  $t\bar{t}$  at Tevatron

Efficiency for  $t\bar{t}$  at LHC