

$$e^{-S_{eff}} \equiv \det(D+m) e^{-S_g}$$