# Kaon Physics and $\chi$ PT Discussion 

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## Some Introductory Comments

- $\Delta S=2, K \Leftrightarrow \bar{K}$ matrix elements and $\Delta S=1$ matrix elements for $K \rightarrow \pi$ and $K \rightarrow \pi \pi$ transitions are being calculated in unquenched simulations with $m_{q}<m_{s}$.

What is the best strategy for obtaining the results at physical $m_{u}$ and $m_{d}$ ?

- Strategies for determining the LECs at NLO in the chiral expansion have been developed $\Rightarrow$ physical matrix elements.
P.Boucaud et al. (SPQR Collaboration)
J.Laiho and A.Soni

In order to make use of these strategies we need calculations in $\chi$ PT at unphysical kinematics. (Status ~ NLO)

- For the calculation of $K \rightarrow \pi \pi$ matrix elements we know the expressions for the finite-volume corrections (both in the centre-of-mass frame and in moving frames).
M.Lüscher; L.Lellouch and M.Lüscher; C.Lin, G.Martinelli, CTS and M.Testa K.Rummukainen and S.Gottlieb; C.Kim, CTS and S.Sharpe; N.Christ, C.Kim and T.Yamazaki


## Some Questions for Discussion

- Is (NLO, NNLO) $\chi$ PT sufficiently precise to be useful?
M.Golterman, D.Becirevic

What is the error if we fit the lattice data to $\chi \mathrm{PT}$ at NLO or NNLO?
Is it $m_{K}^{2} / \Lambda_{\chi}^{2}$ squared or cubed or ???

- What is the status of $\chi \mathrm{PT}$ calculations for such matrix elements?
J.Bijnens
- If $\chi \mathrm{PT}$ is a useful tool in principle, at what values of $m_{u}$ and $m_{d}$ does it set in?
- What are the prospects for a wider programme of kaon physics using the improved staggered formulation of lattice fermions?


## $K \rightarrow \pi \pi$ Matrix Elements of EWP Operators (Quenched)



P.Boucaud et al. (SPQR Collaboration), hep-lat/0412029

Quenched Improved Clover + Plaquette action.
$0.5 \mathrm{GeV}<m_{\pi}<1 \mathrm{GeV}$

## $K \rightarrow \pi$ Matrix Elements of EWP Operators



$N_{f}=2$ Domain Wall Fermion \& DBW2 action.

## $\Delta I=3 / 2$ Matrix Elements of EWP Operators



J.Noaki, hep-lat/0510019
$N_{f}=2$ Domain Wall Fermion \& DBW2 action.

