



# Resonance Chiral Theory approach

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# Resonance Chiral Theory

Large  $N_c$



Lagrangian  
Theory

Spectrum: Goldstones and Resonances

Interactions:

- Chiral symmetry of massless QCD
- Resonances as matter fields

**1/** [Ecker et al, 1989]

$$L_{R\chi T} = \mathcal{L}^{(2)} + L_{\text{kin}}^R + L_{\text{int}}^1(s = 0, 1)$$

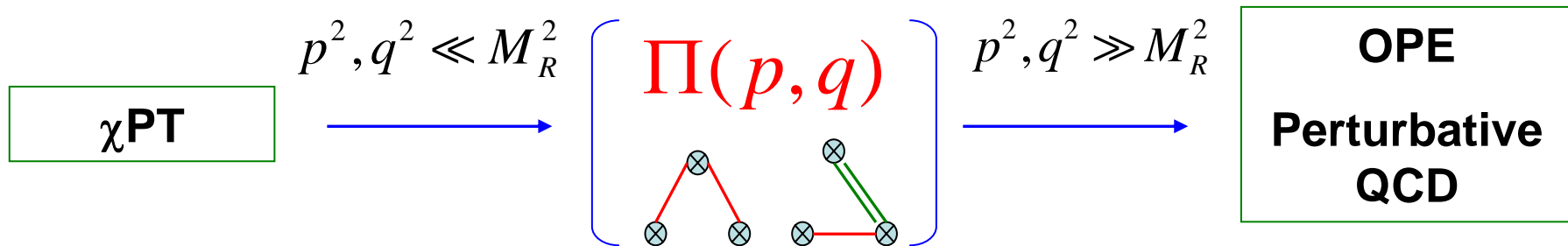
$$L_{\text{int}} \sim \langle R \chi(p^2) \rangle$$

$$L_{\text{int}}^1(s = 1) = \frac{F_V}{2\sqrt{2}} \langle V_{\mu\nu} f_+^{\mu\nu} \rangle + i \frac{G_V}{\sqrt{2}} \langle V_{\mu\nu} u^\mu u^\nu \rangle + \frac{F_A}{2\sqrt{2}} \langle A_{\mu\nu} f_-^{\mu\nu} \rangle$$

$$L_{\text{int}}^1(s = 0) = c_d \langle S u_\mu u^\mu \rangle + c_m \langle S \chi_+ \rangle + i d_m \langle P \chi_- \rangle$$

## 2/ Information on the couplings of $L_{R\chi T}$

### a) OPE of Green Functions of QCD Currents



### b) Asymptotic behaviour of form factors (Brodsky-Lepage)

Comparative features of the Resonance Chiral Theory approach

- More complex: Construction of full sets of operators (unknown couplings).
- More useful: Wide application in many settings...

- Hadronic decays of the tau lepton, decays of resonances,
- Hadronic cross-section, etc.

# LEC's in Chiral Perturbation Theory

$$L_{\chi PT} = \mathcal{L}^{(2)} + \mathcal{L}^{(4)} + \mathcal{L}^{(6)} + \dots$$

$$\mathcal{L}^{(2)} = \frac{\mathbf{F}^2}{4} \langle \mathbf{u}_\mu \mathbf{u}^\mu + \chi_+ \rangle$$

( $N_F = 3$ )

Even-intrinsic-parity  
sector only

$$\mathcal{L}^{(4)} = \mathbf{L}_1 \langle \mathbf{u}_\mu \mathbf{u}^\mu \rangle^2 + \dots = \sum_{i=1}^{10} \mathbf{L}_i \mathbf{O}_i^4$$

[Gasser & Leutwyler, 1985]

$$\mathcal{L}^{(6)} = \mathbf{C}_1 \langle \mathbf{u}_\alpha \mathbf{u}^\alpha \mathbf{h}_{\mu\nu} \mathbf{h}^{\mu\nu} \rangle + \dots = \sum_{i=1}^{90} \mathbf{C}_i \mathbf{O}_i^6$$

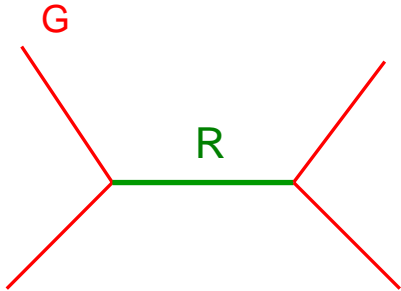
[Fearing & Scherer, 1996]  
[Bijnens, Colangelo & Ecker, 1999,2000]

High-precision predictions  
within  $\chi PT$  :  $F_{\pi_{V,S}}, K_{\ell 3}, \dots$

$\mathbf{L}_i, \mathbf{C}_i ?$

## How do we get them?

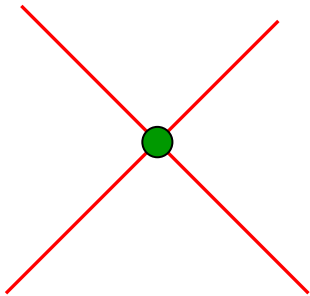
[Gasser & Leutwyler, 1984] [Donoghue et al., 1989] [Ecker et al., 1989]



$$\int [dR] \exp \left[ i \int L_{R\chi T} (R, U; \lambda_j) \right] = \exp \left[ i \int L_{\text{No Local}} (U; \lambda_j) \right]$$



$$q^2 \ll M_R^2$$



$$L_{\text{Local}} (U; \lambda_j) = L_{\text{Local}} (U, L_i, C_i)$$

# The role of Resonance Chiral Theory

$O(p^4)$  [Ecker et al, 1989]

$$L_{\text{int}} \sim \langle R \chi(p^2) \rangle$$

$$L_{R\chi T} = \mathcal{L}^{(2)} + L_{\text{kin}}^R + L_{\text{int}}^1 (s = 0, 1)$$

$$L_{\text{int}}^1 (s = 1) = \frac{F_V}{2\sqrt{2}} \langle V_{\mu\nu} f_+^{\mu\nu} \rangle + i \frac{G_V}{\sqrt{2}} \langle V_{\mu\nu} u^\mu u^\nu \rangle + \frac{F_A}{2\sqrt{2}} \langle A_{\mu\nu} f_-^{\mu\nu} \rangle$$

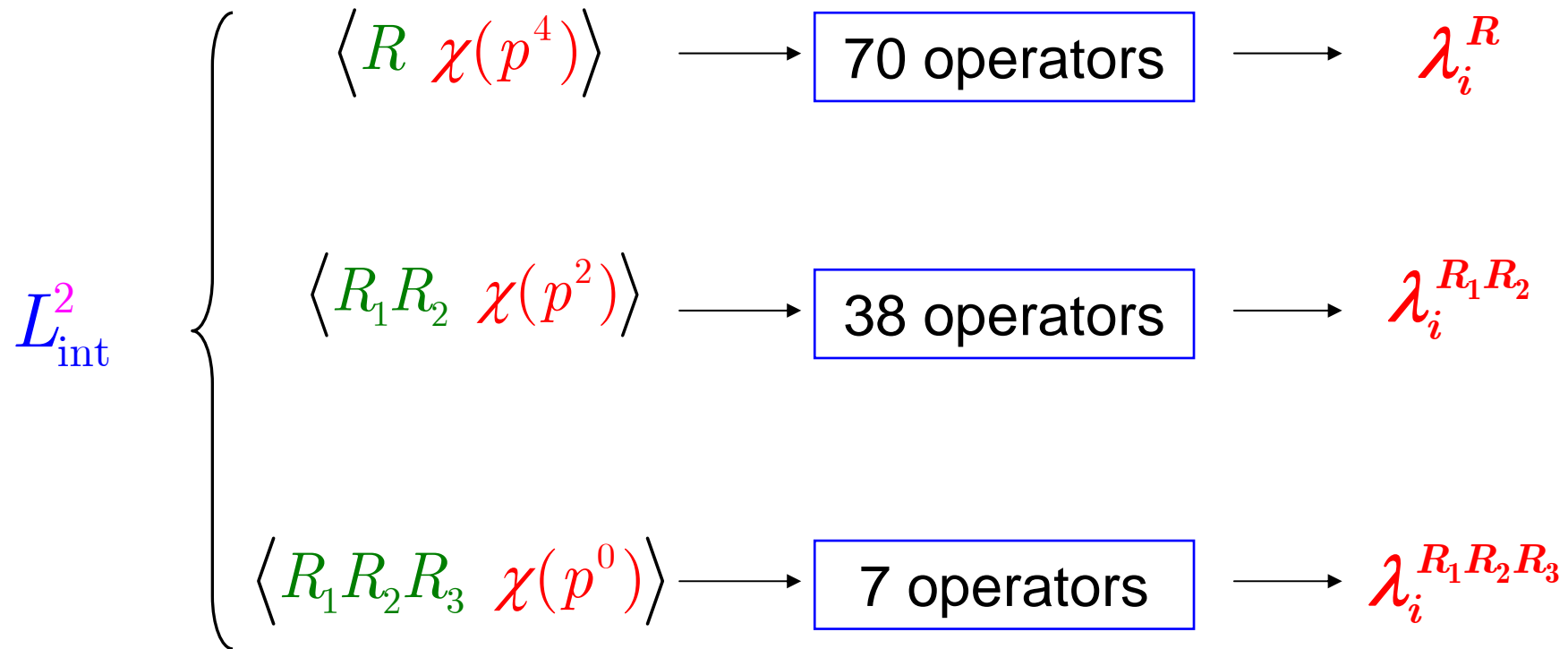
$$L_{\text{int}}^1 (s = 0) = c_d \langle S u_\mu u^\mu \rangle + c_m \langle S \chi_+ \rangle + i d_m \langle P \chi_- \rangle$$

$L_1$	$L_2$	$L_3$	$L_4$	$L_5$	.....
$\frac{G_V^2}{8M_V^2} - \frac{c_d^2}{6M_S^2}$	$\frac{G_V^2}{4M_V^2}$	$-\frac{3G_V^2}{4M_V^2} + \frac{c_d^2}{2M_S^2}$	$-\frac{c_d c_m}{3M_S^2}$	$\frac{c_d c_m}{M_S^2}$	

$O(p^6)$  [Cirigliano et al, 2005]

$$L_{\text{int}} = L_{\text{int}}^1 + L_{\text{int}}^2$$

$$R = V, A, S, P$$



e.g.

$$C_{12}^R = -\frac{c_d c_m}{2M_S^4}$$

$$C_{34}^R = \frac{1}{2} \left[ \frac{c_m(c_m - c_d)}{M_S^4} + \frac{d_m^2}{M_P^4} + 2\frac{d_m}{M_P^2} \lambda_6^P - 2\frac{c_m}{M_S^2} \lambda_8^S + 2\frac{c_d c_m}{M_S^2 M_P^2} \lambda_1^{SP} \right]$$

$$C_{88}^R = -\frac{F_V G_V}{4M_V^4} + C_{90}^R$$

$$C_{90}^R = -\frac{d_m}{M_V^2 M_P^2} \left[ \frac{F_V}{\sqrt{2}} \lambda_1^{PV} + M_V^2 \lambda_9^P \right]$$

$L_{R\chi T}$  is **NOT** QCD for arbitrary values of the couplings



QCD

$$E \ll M_\rho$$

Chiral Symmetry

$$SU_L(N_F) \otimes SU_R(N_F)$$

Chiral Perturbation Theory

$$E \gg M_\rho$$

Perturbative QCD

Asymptotic behaviour of spectral functions

Large  $N_C$

$$E \sim M_\rho$$

Resonance Chiral Theory

$$V_\mu(1^-)$$

$$A_\mu(1^{++})$$

$$\mathcal{L}_{eff}^{QCD} = \sum_i \lambda_i \mathcal{O}_i(V_\mu, A_\mu, \Pi)$$

Vector meson dominance

# Results

<VAP> [Cirigliano et al, 2004]

$$C_{78}^R = \frac{F^2}{8M_V^4 M_A^2} (3M_A^2 + 4M_V^2) - \frac{F^2}{16M_V^2 M_P^2}$$

$$C_{82}^R = -\frac{F^2}{32M_V^4 M_A^2} (4M_A^2 + 5M_V^2) - \frac{F^2}{32M_A^2 M_P^2}$$

$$C_{88}^R = -\frac{F^2}{4M_V^4} + \frac{F^2}{8M_V^2 M_P^2}$$

$$C_{90}^R = \frac{F^2}{8M_V^2 M_P^2}$$

$\pi \rightarrow \ell \nu_\ell \gamma$

$F_V^\pi(q^2)$

$K_{\ell 3}$

also  $C_{87}^R$  ,  $C_{89}^R$

<SPP> [Cirigliano et al, 2005]

$$C_{12}^R = -\frac{F^2}{8M_S^4}$$

$$C_{34}^R = \frac{3F^2}{16M_S^4} + \frac{F^2}{16} \left( \frac{1}{M_S^2} - \frac{1}{M_P^2} \right)^2$$

$$C_{38}^R = \frac{F^2}{16M_S^4} + \frac{F^2}{16} \left( \frac{1}{M_S^4} - \frac{1}{M_P^4} \right)$$

$K_{\ell 3}$

$f_+^{K^0\pi^-}(0) \Big|_{O(p^6)}$